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The impact of tensor force on collective correlations and neutrinoless double- decay

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Abstract

The tensor force changes the nuclear shell structure, and thus may result in underlying influence the collectivity and decay properties of the nucleus. We carefully examined the impact of the monopole and multipole effects originating from the tensor force on both the collectivity and the matrix element for the neutrinoless double- $(0\)$ decay, using the generator-coordinate method with an effective interaction. To analyze the effect of the tensor force, we employed an effective Hamiltonian associated with the monopole-based universal interaction that explicitly consists of the central, tensor, and spin-orbit coupling terms. The interferences among the shell structure, quadrupole collectivity, nucleon occupancy, and $0\$ matrix elements were analyzed in detail. A better understanding of the tensor force would be of great importance in reducing the theoretical uncertainty in $0\$ nuclear matrix element calculations.

Full Text

Preamble

The impact of tensor force on collective correlations and neutrinoless double-decay* Chang-Feng Jiao1, † and Cen-Xi Yuan2, ‡ 1School of Physics and Astronomy, Sun Yat-sen University, Zhuhai 519082, China 2Sino-French Institute of Nuclear Engineering and Technology, Sun Yat-sen University, Zhuhai 519082, China

The tensor force changes the nuclear shell structure, and thus may exert underlying influence on the collectivity and decay properties of the nucleus. We carefully examined the impact of the monopole and multipole effects originating from the tensor force on both the collectivity and the matrix element for the neutrinoless double- (0) decay, using the generator-coordinate method with an effective interaction. To analyze the effect of the tensor force, we employed an effective Hamiltonian associated with the monopole-based universal



interaction that explicitly consists of the central, tensor, and spin-orbit coupling terms. The interferences among the shell structure, quadrupole collectivity, nucleon occupancy, and 0 matrix elements were analyzed in detail. A better understanding of the tensor force would be of great importance in reducing the theoretical uncertainty in 0 nuclear matrix element calculations.

Keywords: Neutrinoless double-beta decay, collective correlations, tensor force.

Introduction

The prospect of observing neutrinoless double- (0) decay is of great interest, as it would be the most feasible way to verify the Majorana nature of neutrinos, and thus demonstrate lepton-number violation [1–5]. In addition, the measurement of its half-life can provide access to the scale for the absolute neutrino mass and mass hierarchy, but it requires a reliable description of the underlying nuclear matrix elements (NMEs) governing the 0 decay [6, 7]. More practically, accurate values of NMEs are crucial for determining a definitive choice and the amount of material required in complicated and expensive -decay experiments. Because 0 decay involves unknown neutrino properties, such as the neutrino mass scale, the matrix element cannot be measured. On the other hand, it strongly depends on the underlying nuclear structures of the parent and daughter nuclei; hence, it must be calculated using nuclear structure methods. At present, NMEs obtained by various theoretical approaches differ by a factor of up to three [7, 8]. Therefore, reducing the uncertainty in matrix elements is a crucial goal for the nuclear structure community.

An important factor in diminishing the uncertainty is a better description of the ground-state (g.s.) wave functions for both parent and daughter nuclei. To achieve this goal, there are two main issues that need to be addressed: understanding the many-body correlations and the nucleon-nucleon interactions that are strongly relevant to the 0 decay NMEs. For the former issue, it was found that some collective correlations significantly influence the calculations decay matrix elements. In particular, matrix elements were suppressed when the ground states of the parent and daughter nuclei exhibited different intrinsic deformations. This suppression was originally investigated using axial quadrupole collectivity [9-12], and later extended to non-axial quadrupole [13] and octupole correlations [14]. It has also been noticed that the transition operators of decay are sensitive to pairing correlations [11, 12, 15, 16]. The 0 decay would be favored if one considers like-particle pairing fluctuations [17], but is remarkably hindered by taking into account proton-neutron (pn) pairing [18-21]. Thus, fully capturing the interplay among collective degrees of freedom is of particular importance for improving the accuracy of the 0 decay NMEs.

To unveil the interplay between collectivity and 0 NMEs, we need a nuclear structure method that can be applied to the investigation of 0 decay, and is capable of dealing with multiple collective correlations in an explicit way. The nuclear structure methods that are most commonly used in the 0 decay

matrix-element calculations are the interacting shell model (ISM) [22-30], interacting boson model (IBM) [31-33], quasiparticle random phase approximation (QRPA) [18, 19, 34-43], and generator coordinate method (GCM) [10-14, 17, 20, 44, 45]. Among them, the so-called quantum number projected GCM (PGCM) [13, 44, 45] is appealing because it can treat fluctuations in multiple collective correlations explicitly on the same footing, providing a feasible way to evaluate the interference among different correlations. It has been shown that the inclusion of quadrupole and pn-pairing correlations in GCM calculations [13, 21, 44] significantly diminishes the large deviation in the 0—decay NMEs between the previous GCM and SM predictions. This indicates that the GCM approach captures most of the correlations around the Fermi surface, which are important for 0—decay.

The other key point is to improve the nucleon-nucleon interaction. To evaluate whether an effective interaction is reasonable for 0 NME calculations, it would be of particular interest to study the influence of a specific term in the interaction. It has been shown that the tensor force has a unique and robust effect on the single-particle energies of nuclei throughout the nuclear chart, and hence, changes the occupation of nucleons associated with the shell structure [46, 47]. Consequently, the tensor force interferes with the collective motion of the nucleons. For example, occupying specific orbits would provide a larger deformation-driving effect, inducing enhanced quadrupole collectivity. Changing the level density of single-particle orbits around the Fermi surface strongly affects the pairing correlations. Recently, the tensor force has been found to contribute significantly to the low-lying Gamow-Teller distribution, and thus makes a dramatic improvement in predicting single- decay half-lives [48]. Therefore, it is very intriguing to evaluate the impact of the tensor force on collective correlations and the resulting effect on 0 decay.

To demonstrate the influence of the tensor force, the tensor term should be incorporated into the effective interaction in an explicit and separable form. We present an analysis of the influence of the tensor force on both the collectivity and the 0 decay NME for candidate nuclei 124Sn/Te, 130Te/Xe, and 136Xe/Ba [5, 49, 50], by applying a PGCM calculation in conjunction with the effective Hamiltonian arising from the monopole-based universal interaction VMU [47] plus a spin-orbit force taken from the M3Y interaction [51]. The VMU interaction consists of the central part given by a Gaussian function in addition to the - and -meson exchange tensor force, which has been very successful in studying tensor monopole effects in previous works [47]. To quantify the impact of the monopole effect associated with the tensor force, we can either include or exclude the tensor-force term in the effective Hamiltonian. This is similar to a previous study that evaluated the impact of the tensor force on single-decay [48] by including the tensor force in Skyrme density functionals and the residual interaction in the RPA. Here, we consider only the standard light left-handed Majorana neutrino exchange mass mechanism, as it is the simplest and most studied mechanism of the 0 decay process.

II. The Model

Owing to the shell closure approximation, the 0 — decay NME can be computed in terms of the matrix element of a two-body transition operator between the g.s. wave functions of the parent and daughter nuclei. Our wave functions were modified at short distances using a Jastrow-type short-range correlation (SRC) function in the parameterization of CD-Bonn [38]. A more detailed expression of the matrix element can be found in Ref. [18]. These many-body wave functions, which play a crucial role in the NME calculation, are provided by the GCM. We employed a shell-model effective Hamiltonian (Heff) in a valence space whose size is free to choose. In an isospin scheme, Heff can be written as the sum of one- and two-body operators:

$$H_{\mathrm{eff}} = \sum \epsilon_a \hat{n}_a + \sum_{a < b, c < d} V_{JT}(ab; cd) \hat{T}_{JT}(ab; cd), \quad (1)$$

where ϵ_a stands for single-particle energies, $V_{JT}(ab;cd)$ stands for two-body matrix elements (TBMEs), \hat{n}_a is the number operator for the spherical orbit a with quantum numbers (n_a, l_a, j_a) and $\hat{T}_{JT}(ab;cd) = \sum_{JMT_z} (ab)_{TT_z}^{JM}(cd)$ is the scalar two-body density operator for nucleon pairs in orbits a, b and c, d coupled to quantum numbers J, M, T, and T_z .

With the effective Hamiltonian, the first step is to generate a set of reference states $|\Phi(q)\rangle$ that are quasiparticle vacua constrained to specified expectation values $q_i = \langle O_i \rangle$ for different collective operators O_i . Large-amplitude fluctuations in multiple collective correlations should be treated by further admixing these reference states. Here we take the operators O_i which encompass the collective coordinates most important for low-lying spectra, and the 0 NMEs [21]:

$$O_1 = Q_{20}, \quad O_2 = Q_{22}, \quad O_3 = (P_0 + P_0^\dagger), \quad O_4 = (S_0 + S_0^\dagger),$$

where the operator P_0^{\dagger} (S_0^{\dagger}) creates a correlated isoscalar (isovector) protonneutron pair in a single-particle orbit. A detailed definition of collective operators can be found in Ref. [13]. We do not incorporate the fluctuations in like-particle pairing which, according to the EDF-based work of Ref. [17], slightly increases the NMEs. We can treat these fluctuations on an equal footing as those in deformation and pn pairing, but at the cost of a tremendous increase in computing time.

The constrained Hartree-Fock-Bogoliubov (HFB) equations for linear constraints are solved for the Hamiltonian with

$$\langle H' \rangle = \langle H_{\text{eff}} \rangle - \lambda_Z (\langle N_Z \rangle - Z) - \lambda_N (\langle N_N \rangle - N) - \sum_i \lambda_i (\langle O_i \rangle - q_i), \quad (3)$$

where N_Z and N_N are the proton and neutron number operators, respectively, λ_Z and λ_N are the corresponding Lagrange multipliers. The sum over i includes the quadrupole operators Q_{20} and Q_{22} , with the addition of the isoscalar or isovector proton-neutron pairing operator in Eq. (3). The λ_i represents the Lagrange multipliers that constrain the expected values of these operators to the specified quantities q_i . We solved these equations many times, constraining each time to a different point on a mesh in the space of q_i .

Once we obtain a set of HFB vacua constrained to various collective correlations, the GCM state can be composed of a linear superposition of the projected HFB vacua, given by

$$|\Psi_{NZ}^{J\sigma}\rangle = \sum_{q,K} f_{qK}^{J\sigma} |JMK;NZ;q\rangle, \quad (4)$$

where $|JMK;NZ;q\rangle \equiv \hat{P}_{MK}^{J}\hat{P}_{N}\hat{P}_{Z}|\Phi(q)\rangle$. Here, the \hat{P} 's project HFB states onto a well-defined angular momentum J and its z-component M, neutron number N, and proton number Z [52]. The weight function $f_{qK}^{J\sigma}$, where σ is simply an enumeration index, can be obtained by solving the Hill-Wheeler equations [52]:

$$\sum_{K',q'} \left[H^{J}_{KK'}(q;q') - E^{J}_{N\sigma} N^{J}_{KK'}(q;q') \right] f^{J\sigma}_{q'K'} = 0, \quad (5)$$

where the Hamiltonian kernel $H^J_{KK'}(q;q')$ and the norm kernel $N^J_{KK'}(q;q')$ are given by:

$$H^{J}_{KK'}(q;q') = \langle \Phi(q) | \hat{P}^{J\dagger}_{KK'} \hat{P}_N \hat{P}_Z H_{\text{eff}} | \Phi(q') \rangle, \label{eq:HKK'}$$

$$N^{J}_{KK'}(q;q') = \langle \Phi(q) | \hat{P}^{J\dagger}_{KK'} \hat{P}_N \hat{P}_Z | \Phi(q') \rangle. \quad (6)$$

To solve Eq. (5), we diagonalize the norm kernel N and use the nonzero eigenvalues and the corresponding eigenvectors to construct a set of "natural states". The Hamiltonian is then diagonalized in the space of these natural states to obtain the GCM states $|\Psi_{NZ}^{J\sigma}\rangle$ (see details in Refs. [53, 54]). With the lowest J=0 GCM states as the ground states of the initial and final nuclei, we can calculate the 0—decay matrix element $M^{0\nu}$.

III. Effective Hamiltonian

The nuclear interaction V can be divided into the central part (V_C) , spin-orbit part (V_{LS}) , and tensor part (V_T) , as follows:

$$V = V_C + V_{LS} + V_T. \label{eq:VC}$$



The so-called jj55-shell configuration space that comprises the proton and neutron $0g_{7/2}$, $1d_{5/2}$, $1d_{3/2}$, $2s_{1/2}$, and $0h_{11/2}$ orbitals is used for the calculations of 124 Sn-Te, 130 Te-Xe, and 136 Xe-Ba.

The monopole-based universal interaction, VMU [47], and the M3Y type spin-orbit interaction [51] (VMU+LS) are used to construct the effective Hamiltonian in the present work. VMU contains a central force in the Gaussian form (V_C) and a bare $\pi + \rho$ meson exchange tensor force (V_T) . ISM investigations, with VMU+LS mainly as the cross-shell interaction, have been performed in psd [56], sdpf [57], pf sdg regions [58], 132 Sn [59], and 208 Pb [60-62] regions. Recently, VMU+LS was used, as a unified interaction, to study the excitation energies of medium-heavy nuclei around 132 Sn and 208 Pb [63, 64]. Compared to VMU proposed in Ref. [47], the proton-proton (neutron-neutron) central forces in the present work were enhanced by 15% (5%), following the suggestions in Refs. [63, 64] to further improve the calculation accuracy of the low-lying excitation energies of medium-heavy nuclei. The constructed Hamiltonian is examined in Sec. IV along with the discussion of the corresponding results.

IV. Results and Discussion

An important probe for deformation and associated collectivity is the -ray spectroscopy of the nucleus. Figure 1 [Figure 1: see original paper] shows the low-lying level spectra of $^{124}\mathrm{Sn},\,^{124}\mathrm{Te},\,^{130}\mathrm{Te},\,^{130}\mathrm{Xe},\,^{136}\mathrm{Xe},\,$ and $^{136}\mathrm{Ba}$ obtained with or without the tensor term compared to the experimental data [55]. Although our calculated 6^+ states are overestimated, most of the low-lying states obtained by our calculations, which include the tensor term, are in reasonable agreement with the experimental spectra. The overestimation of higher spin states could be due to the fact that the GCM calculations exclude vibrational motion and broken-pair excitation, while these two excitation modes may significantly lower the excited states, especially in the nearly spherical and weakly deformed nuclei. In general, the inclusion of the tensor term significantly improved the calculated spectra. The 2_1^+ states are lowered if the tensor term is included, implying an increase in the quadrupole collectivity owing to the impact of the tensor force.

The reduced E2 transition probability, $B(E2:0_1^+\to 2_1^+)$, provides another direct probe for quadrupole collectivity. It should be noted that there was an inconsistency in the calculations for $B(E2:0_1^+\to 2_1^+)$ in this region. Using the same SVD interaction, an effective charge set of $e_{\rm eff}^n=0.88e$ and $e_{\rm eff}^p=1.88e$ was suggested for $^{124}{\rm Sn/Te}$ in Refs. [28], but a set of $e_{\rm eff}^n=0.5e$ and $e_{\rm eff}^p=1.5e$ was used for $^{130}{\rm Te/Xe}$ and $^{136}{\rm Xe/Ba}$ [27]. This inconsistency was resolved using our effective interaction. In the current work, we used the canonical effective charges $e_{\rm eff}^n=0.5e$ and $e_{\rm eff}^p=1.5e$ for all the investigated nuclei. The results are compared in Fig. 2 [Figure 2: see original paper] with the experimentally adopted values [65]. A strong agreement is obtained between the calculated and adopted values of $B(E2:0_1^+\to 2_1^+)$ with the universal effective charges, indicating an improved description of the quadrupole collectivity in these candidate nuclei. This improvement is crucial for reducing uncertainty in the calculation

of the 0 decay matrix. Similar to low-lying -ray spectroscopy, incorporating the tensor force results in the enhancement of the quadrupole collective correlation and hence provides a better agreement with the experimentally adopted values of B(E2). It should be noted that the increase in quadrupole collectivity is more significant in daughter nuclei, that is, 124 Te, 130 Xe, and 136 Ba. This leads to a larger deviation in the intrinsic deformation between the parent and daughter nuclei. The underlying physics will be discussed in more detail later in this paper.

We then computed the values of 0 decay matrix elements of ¹²⁴Sn, ¹³⁰Te, and ¹³⁶Xe. In closure approximation, the 0 matrix element of a two-body transition operator is computed between the initial and final ground states. Assuming an exchange of a light Majorana neutrino with the usual left-handed currents, the matrix element is [18]

$$M^{0\nu} = M_{GT}^{0\nu} + M_F^{0\nu} + M_T^{0\nu},$$

where GT, F, and T refer to the Gamow-Teller, Fermi, and tensor parts of the matrix elements, respectively. A detailed presentation of the forms of Gamow-Teller, Fermi, and tensor transition operators can be found in Refs. [13, 18]. Note that the tensor transition operator is unrelated to the tensor term of the effective Hamiltonian. The vector and axial coupling constants are taken to be $g_V=1$ and $g_A=1.254$, respectively. Wave functions were modified at short distances using a Jastrow short-range correlation (SRC) function with CD-Bonn parametrization [18, 38].

The results are listed in Table 1 , where the Gamow-Teller, Fermi, and tensor contributions are shown. While the Fermi parts remain almost unchanged, the Gamow-Teller parts are drastically suppressed when the tensor force is considered. The total matrix elements given by the calculation, including the tensor force, are approximately 26 to 40% smaller than those of the calculation excluding the tensor force.

The tensor part of the NME, although suppressed if the tensor force is included, is negligibly small. This is in accordance with other studies that used different nuclear structural methods [23, 33, 42]. Therefore, tensor contributions were neglected [17, 19, 37]. The small tensor contributions in the NME are mainly attributed to the fact that the tensor part is induced by high-order currents. Thus, the two-body matrix elements of the tensor 0—decay operator are much smaller than those of Gamow-Teller and Fermi matrices. Because the value is small and subtle, it is difficult to trace the origin of these numerical changes in tensor NME. The interference between the collective correlations and tensor contributions in the NME remains unclear. Further study of the tensor part of the NME is required in the future, but its negligible contribution may not affect the conclusions we present in this work.

The influence of collective correlations on 0 — nuclear matrix elements can be

evaluated by the collective wave functions of the parent and daughter nuclei. The so-called collective wave functions are defined to account for the probability density of finding the state with given expectation values of collective operators in Eq. (3). The detailed expression for the collective wave functions is given in Eq. (18-19) of Ref. [53]. Note that the sum of collective wave functions is normalized to 1. When the probability density of finding the state with the specific deformation and isoscalar pairing amplitude increases, the probability density of finding the state elsewhere would be suppressed consequently. Figure 3 [Figure 3: see original paper] shows the square of the collective wave functions against quadrupole deformation β_2 and isoscalar pn pairing amplitude. Since the cases ¹²⁴Sn and ¹³⁶Xe lack valence protons and valence neutron holes, respectively, and hence cannot change pn pairing, the squares of the collective wave functions of these two nuclei are not displayed. It can be seen that the largest peaks of collective wave functions in these nuclei are pushed, to some different extent, to the region with larger quadrupole deformations and isoscalar pairing amplitude if the tensor force is incorporated. The most apparent case is ¹³⁶Ba, where a subpeak appears at the sphericity in the calculation excluding the tensor force, but vanishes when we take the tensor force into consideration. Another interesting case occurs in ¹²⁴Te. When the tensor force is included, the increase of the collective wave functions with large quadrupole deformation and larger isoscalar pairing forms a dip in the region with near spherical deformation and intermediate isoscalar pairing.

Since 124 Sn and 136 Xe keep their characteristics of sphericity owing to the Z=50 and N=82 shell closure, respectively, the difference of deformations between all the parent and their daughter nuclei are enlarged. In addition, the collective wave functions obtained with inclusion of the tensor force spread more widely along with the isoscalar pairing, indicating stronger isoscalar pairing fluctuations. The effects of both quadrupole deformation and isoscalar pairing therefore strongly hinder the 0 matrix elements.

To unveil the underlying connection amongst tensor force, collectivity, and nuclear matrix elements for 0—decay, the HFB effective single-particle energies (ESPEs) for valence neutron and proton orbits in $^{130}\mathrm{Te}$ and $^{130}\mathrm{Xe}$ are exhibited in Fig. 4 [Figure 4: see original paper]. In this work, the HFB single-particle energies are obtained by diagonalizing the HF Hamiltonian h in the HFB equation, which is constructed with the density matrix of the HFB solution. For simplicity, only the ESPEs at spherical shapes and with isoscalar pairing amplitude $\phi=0$ are shown. Note that the ESPEs are plotted relative to the $2s_{1/2}$ orbits. The ESPE is changed by the tensor force itself, as well as by re-adjusting the one-body part of the effective interaction due to the exclusion of tensor force. By looking at relative ESPEs, one can partly remove the common change from re-adjusting the one-body part of the effective interaction and thus can check the tensor effect more directly.

Figure 4 shows that owing to the inclusion of the tensor force, all neutron (proton) valence orbits are lowered with respect to the neutron (proton) $2s_{1/2}$

orbit. Among them, the neutron and proton $0h_{11/2}$ orbits were shifted more significantly. Of particular interest, the neutron and proton $0h_{11/2}$ orbits were suppressed more drastically in $^{130}\mathrm{Xe}$ than in $^{130}\mathrm{Te}$. It is a complex many-body effect resulting from monopole interactions produced by the tensor force among all valence nucleon orbits. According to the rules discussed in Refs. [46, 66], the monopole interaction produced by the tensor force between proton $0g_{7/2}$ and neutron $0h_{11/2}$ orbit is attractive. As two more protons in $^{130}\mathrm{Xe}$ mainly occupy the proton $0g_{7/2}$ orbit, the neutron $0h_{11/2}$ orbit decreases more remarkably than that in $^{130}\mathrm{Te}$. Meanwhile, the monopole interactions between the proton $0h_{11/2}$ and neutron $0h_{11/2}$, and between the proton $0h_{11/2}$ and neutron $1d_{5/2}$ orbits are both repulsive. Because the two neutrons are mainly removed from the neutron $0h_{11/2}$ and $1d_{5/2}$ orbits in 130Xe when compared to 130Te, the repulsive effects are weakened, and thus the proton $0h_{11/2}$ orbit is pulled down more substantially. Similar results were observed for the 124Sn/Te and 136Xe/Ba.

For all investigated nuclei, the suppression of the proton $0h_{11/2}$ orbit lifts the proton Fermi surface, whereas the lowering of the neutron $0h_{11/2}$ orbit pulls the neutron Fermi surface down. The Fermi surfaces of both protons and neutrons lie closer to the $0h_{11/2}$ midshell if the tensor force is included. It should be noted that high-j orbits are expected to exhibit a large deformation-driving effect [67, 68]. Because the lowering of $0h_{11/2}$ orbit is more significant in the daughter nuclei of 0—decays, the deformation-driving effect is larger, resulting in a more remarkable enhancement of the quadrupole correlations in these nuclei.

In addition, the shift of the valence nucleon orbits induced by the tensor force would adequately affect the nucleon occupancies. The change in the groundstate nucleon occupancies in the 0 decays provides an unquestionably important constraint on the calculation of the 0 matrix element, as it directly determines which neutrons decay, which protons are created in the decay, and how their configurations are rearranged [69]. Recently, the proton occupancies and neutron vacancies of ¹³⁰Te and ¹³⁰Xe have been probed in single-nucleon transfer reactions to a level of precision corresponding to a few tenths of that of a nucleon [70, 71]. The total neutron vacancies measured are 4.16 for ¹³⁰Te and 6.26 for ¹³⁰Xe [70], the total proton occupancies are 1.89 for ¹³⁰Te and 3.95 for ¹³⁰Xe [71], which gives the total change in proton occupancies and neutron vacancies of 2.06 and 2.10, respectively. Note that, in a realistic nucleus, nucleons may occupy orbits above the valence space or unoccupied orbits frozen in the core. Therefore, the measured total proton occupancy and neutron vacancy slightly deviate from the expected values with respect to the valence space. Figure 5 [Figure 5: see original paper] shows our calculations describing the change in proton occupancies and neutron vacancies between the ground states for the 0 decay of $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$. The experimental data [70, 71] are denoted "Expt.", compared to four different calculations: current works including and excluding the tensor force (denoted "w/ tensor" and "w/o tensor" respectively), shellmodel calculations using GCN5082 interaction (denoted "SM1") [23] and SVD interaction (denoted "SM2") [27]. Notwithstanding the notable discrepancies

from the experimental values, our calculation qualitatively reproduces the two most important contributions of the valence orbits for the nucleons that switch from neutrons to protons. The largest change in proton occupancies occurs in the $0g_{7/2}$ orbit, and the second largest change occurs in the 1d orbit. Meanwhile, the largest change in neutron vacancies appears in the 1d orbit, and the second largest change is in the $0h_{11/2}$ orbit. Note that the inclusion of the tensor force improves the description of the change in occupation of nucleons. As shown in Figure 5, our calculation that excludes the tensor force overestimates the change in the neutron vacancy of the $0h_{11/2}$ orbit. Taking into account the tensor force, the neutron $0h_{11/2}$ orbit is pulled down substantially and merges into the $1d_{5/2}$ subshell. It reduces the change of neutron vacancies in the $0h_{11/2}$ orbit but enhances the change in the $1d_{5/2}$ orbit, which is in accord with the measurement.

In Table 2 , the calculated NMEs for the 0 $\,$ decay of $^{124}{\rm Sn}$ \rightarrow $^{124}{\rm Te},$ $^{130}{\rm Te}$ \rightarrow 130 Xe, and 136 Xe \rightarrow 136 Ba are compared with those given by ISM [23, 27, 28]. QRPA [19, 40, 42], IBM2 [33], GCM in conjunction with the non-relativistic energy density functional (NR-EDF) [17], and relativistic energy density functional (R-EDF) [10]. In general, our $M^{0\nu}$ values are comparable with those obtained with the ISM, the QRPA from the Tübingen and Jyväskylä groups, and the IBM2, while the NR-EDF and R-EDF provide much larger values. The significantly large NMEs can be attributed to the lack of pn pairing correlation in the density energy functionals, either non-relativistic Gogny D1S [17] or relativistic PC-PK1 [10]. As previously mentioned, the pn pairing fluctuation would remarkably suppress the NMEs of 0 decays. The QRPA from the Chapel Hill group exhibited a noticeably small NME of $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$ decay. This is because their QRPA calculation was based on a single HFB minimum, which was spherical for ¹³⁰Te and prolate for ¹³⁰Xe. The sharp deformation difference between the parent and daughter nuclei suppressed the 0 NME. Our PGCM calculations adequately addressed the fluctuations in shape and pn pairing on the same footing. This would fix the above issues and provide a reasonable description of the 0 NMEs.

Finally, it should be mentioned that we only discuss the NME of 0 decay from the ground state of the parent nucleus to that of the daughter nucleus in this work. Actually, the decay to the low-lying excited states of the daughter nucleus should also be considered if it is allowed energetically. The NME of this process is strongly quenched by the phase-space factor in the standard light left-handed Majorana neutrino exchange mechanism [72, 73]. However, a considerable contribution to the NME from this process in the non-standard mechanism cannot be ruled out. Further study of 0 decay of NME to the lowest 2_1^+ state of the daughter nucleus within the framework of PGCM would be a desirable next step in the future.

V. Summary

An analysis of the influence of the monopole effect originating from the tensor force on both the collectivity and the nuclear matrix element of the 0 is presented for candidate isotopes ¹²⁴Sn/Te, ¹³⁰Te/Xe, and ¹³⁶Xe/Ba, using the generator-coordinate method with a shell-model effective interaction. We employ an effective Hamiltonian written in terms of the monopole-based universal interaction VMU plus a spin-orbit force taken from the M3Y interaction. The so-called monopole-based universal interaction consists of central and tensor forces explicitly, and hence, could clarify the effect of the tensor force by including or excluding the tensor-force term. The monopole effect arising from the tensor force is shown to have a significant influence on the quadrupole collectivity, nucleon occupancy, and 0 matrix element, which could be interpreted by the change in the shell structure owing to the novel feature of the tensor force. A better understanding and possible refinement of the tensor force would thus be of particular importance in reducing the theoretical uncertainty in the calculation of 0 nuclear matrix elements.

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