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Full Text

Thermal Evolution of the Central Compact Object in HESS J1731–347 as Evidence for a Color-Flavor-Locked Strange Star

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Key words: stars: neutron – stars: individual (XMMU J173203.3–344518) – stars: evolution – dense matter

1. Introduction

The study of compact stars has been an important subject of modern astrophysics since the discovery of pulsars in 1967. Observations over the past few decades have shown a diverse population of these objects, with masses ranging from the canonical 1.4 M to relatively massive 2 M stars (Lattimer 2021). However, recent observations of the central compact object (CCO) XMMU J173203.3–344518 (hereafter XMMU J1732) in the supernova remnant HESS J1731–347 (Doroshenko et al. 2022) present a significant challenge to this established paradigm, exhibiting properties that lie well outside the traditionally expected range for neutron stars.

X-ray spectral analysis reveals an unusually high effective surface temperature and the age of the remnant is estimated to be between 2 and 6 kyr (Cui et al. 2016). Especially, the derived gravitational mass and radius (Doroshenko et al. 2022) place XMMU J1732 in a previously unexplored region of the mass–radius diagram. Its mass is significantly below the theoretical minimum (1.17 M) predicted for neutron stars formed through iron core collapse (Suwa et al. 2018), suggesting that existing nuclear matter equations of state (EoSs) may require revisions. Several works discussed possible models for this low mass compact object, including strange star models (Horvath et al. 2023; Sagun et al. 2023; Di Clemente et al. 2024), neutron stars containing a core of dark matter (Sagun et al. 2023; Liu et al. 2025), and hybrid stars undergoing phase transitions to exotic matter (Laskos-Patkos et al. 2024). Additionally, some studies have suggested that XMMU J1732 could be the lightest known neutron star (Zhang et al. 2024). However, these models often face challenges in simultaneously reproducing the observed low mass, relatively small radius, and high surface temperature, without the need for additional, carefully adjusted mechanisms.

The strange quark matter hypothesis (Witten 1984), particularly the color-flavor-locked (CFL) phase (Alford et al. 1999; Alford 2001; Alford et al. 2008), offers a compelling alternative model. At sufficiently high densities, strange quark matter may exist as the CFL phase, characterized by Cooper pairing of quarks across all flavors and colors. This pairing results in a self-bound configuration where the mass scales with the radius as $M \propto R^3$ (Li et al. 1999), in contrast to traditional neutron stars. This self-bound strange star allows for stable, sub-solar-mass configurations. Moreover, the CFL phase modifies microphysical processes, suppressing neutrino emission and specific heat, which significantly influences the thermal and rotational evolution of the star (Alford et al. 2008; Zheng et al. 2006). Therefore, the CFL strange star scenario could naturally explain the observed mass–radius relationship.

Furthermore, including r-mode heating within the CFL phase strange star offers a self-consistent explanation for the observed high surface temperature and low mass–radius. R-mode oscillations, driven by gravitational wave emission via the Chandrasekhar-Friedman-Schutz (CFS) instability (Chandrasekhar 1970;

Friedman & Schutz 1978; Andersson 1998), are a particularly promising heating mechanism for rapidly rotating compact objects. The instability is driven by the Coriolis force. In the CFL phase, the suppressed shear and bulk viscosities allow r-modes to reach higher saturation amplitudes, facilitating efficient dissipation and heating (Andersson et al. 2002; Zheng et al. 2006). This makes r-mode a potentially dominant heating source in CFL strange stars, especially at the early stage.

In this study, we present a comprehensive investigation of XMMU J1732 within the CFL strange star framework, incorporating r-mode heating. Our primary objectives are to address the following key questions: (1) Can the CFL phase EoS simultaneously account for the observed mass-radius relationship and thermal properties of XMMU J1732? (2) What constraints do the observed properties place on the microscopic parameters of strange quark matter? (3) How does r-mode heating in the CFL phase contribute to maintaining the observed high surface temperature? To solve these questions, we combine numerical modeling of stellar structure (using the Tolman–Oppenheimer–Volkoff equations) with detailed calculations of thermal evolution and r-mode instability. By incorporating the latest observational constraints and carefully evaluating theoretical uncertainties in the CFL phase parameters, we aim to develop a more comprehensive understanding of the observed properties of XMMU J1732.

This paper is organized as follows: Section 2 presents the theoretical framework and methodology. Section 3 describes our numerical results and their implications for XMMU J1732. Finally, Section 4 is the conclusion and discussion.

2.1. Color-Flavor-Locked Phase in Strange Stars

Strange stars in the CFL phase exhibit unique properties due to the formation of Cooper pairs among quarks of all flavors and colors near the Fermi surface. This pairing mechanism fundamentally alters both the EoS and the transport properties of strange quark matter. Recent studies suggest the observed temperature of XMMU J1732 could be explained if it is a strange star in the CFL phase (Horvath et al. 2023; Sagun et al. 2023).

In the CFL phase, the grand canonical potential is modified by the pairing gap, Δ (Weissenborn et al. 2011; Zhou et al. 2018):

$$\Omega = \Omega_{\text{free}} - (3\Delta^2 b^2)/(\pi^2) + B_{\text{eff}}$$

where $_b$ is the baryon chemical potential, and the unpaired contribution, $\Omega_{\{\text{free}\}}$, is given by:

$$\Omega_{\text{free}} = -(\text{u}^4 + \text{d}^4 + \text{s}^4 + \text{e}^4)/(12\pi^2) \times (1 - a_4)$$

where the first term represents the ideal Fermi gas contributions from each particle species ($i = u, d, s, e$). The second term includes perturbative QCD corrections through the dimensionless parameter a_4 that characterizes the strength

of these corrections (Alford et al. 2005). The effective bag constant, B_{eff} , accounts for non-perturbative QCD effects.

Specific values for the strange quark mass (m), B_{eff} , a_4 , and the CFL pairing gap (Δ) are discussed in Section 3.1.

2.2. R-mode Instability in CFL Phase Strange Stars

R-mode oscillation is a non-radial oscillation in rotating stars driven by the Coriolis force and can be amplified by gravitational radiation through the CFS mechanism (Chandrasekhar 1970; Friedman & Schutz 1978; Andersson 1998). In the CFL phase of quark matter, r-modes are particularly significant due to the drastically reduced viscosity. The temporal evolution of these modes is governed by two coupled equations for the r-mode amplitude, α , and the stellar angular velocity, Ω (Owen et al. 1998; Zheng et al. 2006):

$$\begin{aligned} d\alpha/dt &= - (1/\tau_{\text{GR}} + 1/\tau_v + 1/\tau_m) \alpha \\ d\Omega/dt &= - (2\Omega Q/\tau_{\text{GR}}) \alpha^2 \end{aligned}$$

where τ_{GR} , τ_v , and τ_m represent the timescales for gravitational radiation, viscous damping, and magnetic braking, respectively. The parameter Q quantifies the coupling between r-mode oscillations and bulk rotation, where J and \tilde{I} are the normalized angular momentum and moment of inertia, respectively (Ho & Lai 2000). In this work, we calculate J and \tilde{I} self-consistently using the EoS presented in Section 2.1.

In the CFL phase, electron-electron scattering dominates the viscous dissipation, as other processes are exponentially suppressed by the pairing gap. This reduction in viscosity has important implications for r-mode and thermal evolution of the star.

The r-mode saturation amplitude, α_{sat} , is another key but highly uncertain parameter. While early theoretical studies proposed values near unity (Andersson 1998), more recent nonlinear analyses have significantly lowered these estimates. Mode coupling calculations suggest α_{sat} values in the range 10^{-4} – 10^{-2} , whereas turbulent dissipation models indicate even smaller values, down to 10^{-6} – 10^{-3} (Bondarescu et al. 2009). The value of α_{sat} strongly influences both the spin-down rate and thermal evolution of the star (Atta & Basu 2025).

2.3. Thermal Evolution with R-mode Heating

The thermal evolution of XMMU J1732 follows the energy balance equation (Zheng et al. 2006):

$$C dT/dt = -L - L\gamma + H_{\text{sv}}$$

where C is the total specific heat, L_{γ} represents the neutrino luminosity, L_{γ} is the surface photon luminosity, and $H_{\{sv\}}$ denotes the heating rate due to shear viscosity. In the CFL phase, pairing effects significantly suppress the specific heat, C (Blaschke et al. 2000):

$$C = c_q T^3 \exp(-\Delta/(k_B T_c)) \times (\Delta/(k_B T))^2$$

where T_c is the critical temperature for the CFL phase transition, Δ is the pairing gap, and c_q is a constant related to the specific heat of unpaired quark matter. These parameters influence both microscopic processes and macroscopic evolution timescales.

Within strange quark matter, three primary neutrino emission processes are typically considered: direct Urca, modified Urca, and quark bremsstrahlung (Iwamoto 1982). The corresponding neutrino emission rates per unit volume are (Zheng et al. 2006):

$$\begin{aligned} \text{direct} & 8.8 \times 10^{33} \alpha_c (_b/_b_0)^{(1/3)} Y_e^{(1/3)} T_9^6 \text{ erg cm}^{-3} \text{ s}^{-1} \\ \text{modified} & 1.7 \times 10^{20} \alpha_c (_b/_b_0)^{(2/3)} Y_e^{(2/3)} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1} \\ \text{brems} & 1.4 \times 10^{19} \alpha_c (_b/_b_0) T_9^6 \text{ erg cm}^{-3} \text{ s}^{-1} \end{aligned}$$

where α_c is the strong coupling constant, $_b$ is the baryon number density, $_b_0$ is the nuclear saturation density, Y_e is the electron fraction, and T_9 is the temperature in units of 10^9 K (8.6×10^4 eV).

The CFL pairing gap, Δ , plays a crucial role in both the cooling and heating processes. It exponentially suppresses direct Urca by a factor of $\exp(-\Delta/(k_B T))$ and modified Urca and quark bremsstrahlung by $\exp(-2\Delta/(k_B T))$ (Blaschke et al. 2000) and it modifies the shear viscosity by $\Delta^2/(_q k_B T^3)$. Therefore, Δ is a critical parameter for determining the long-term thermal evolution of the star. The observed properties of XMMU J1732 need a careful treatment of these modified cooling rates and shear viscosity. While the effective bag constant, $B_{\{eff\}}$, and the perturbative QCD correction, a_4 , influence the stellar structure and, consequently, the r-mode coupling strength, Q , their impact is secondary (Zheng et al. 2006; Zhou et al. 2018). Over long timescales ($t > 10^4$ yr), initial conditions become less significant, except when considering r-mode heating (Zheng et al. 2006; Zhou et al. 2018).

The relationship between the surface temperature T_s and the internal temperature T is given by Gudmundsson et al. (1983):

$$T_s = T \times (g_{s,14})^{(1/4)} \times (R_6)^{(-1/4)}$$

where $g_{s,14}$ is the surface gravity in units of 10^{14} cm s $^{-2}$:

$$g_{s,14} = (GM/R^2) / (10^{14} \text{ cm s}^{-2})$$

where R_6 is the stellar radius in units of 10 km. Equation (10) is based on models of heat transport in neutron star envelopes composed primarily of iron (Gudmundsson et al. 1983). Although the envelope composition in a CFL

strange star may differ (e.g., potentially containing a crust of normal matter or electrons), this relation remains a widely used and reasonable approximation for connecting internal and surface temperatures. While deviations could arise from detailed envelope physics specific to CFL stars, such effects are not expected to alter the overall conclusions regarding the necessity of an internal heating mechanism.

The observed high temperature of the CCO XMMU J1732 at its young age (2–6 kyr) requires ongoing heating beyond standard cooling. Several heating mechanisms have been proposed for compact stars, but most are not compatible with the properties of XMMU J1732. Fallback accretion is disfavored by the lack of infrared excess and the predominantly thermal X-ray spectra observed in CCOs (Wang et al. 2007; de Luca 2008). Deep crustal heating requires a past accretion episode, which is absent in these isolated objects (Brown 1999), and is primarily relevant for recycled millisecond pulsars or low mass X-ray binaries. Internal ohmic dissipation is also likely inefficient due to the relatively low surface magnetic fields inferred for CCOs ($B \sim 10^{10}\text{--}10^{11}$ G) (Gotthelf et al. 2013; Viganò et al. 2013; Halpern & Gotthelf 2015).

This makes internal heating from rotational energy dissipation, particularly via the r-mode instability (Andersson 1998; Zheng et al. 2006), the most plausible mechanism. R-mode heating is intrinsic to rapidly rotating young neutron stars and is expected to be especially efficient in the CFL phase (Andersson et al. 2002). This process naturally connects thermal emission to the dense matter EoS and aligns with the non-detection of pulsations. We therefore adopt r-mode heating as the primary mechanism driving the thermal evolution of XMMU J1732. The heating rate due to shear viscosity is given by:

$$H_{\text{sv}} = (2E_c \alpha^2) / \tau_{\text{sv}}$$

where E_c is the canonical energy of the r-mode.

In the CFL phase, viscous dissipation from quark reactions is exponentially suppressed due to the pairing gap. As a result, shear viscosity from electron-electron scattering becomes the dominant damping mechanism (Zheng et al. 2006), with the damping timescale given by:

$$\tau_{\text{sv}} = 0.33 (\mu_e / \mu_q)^4 (h / \mu_q) (k_B T / \mu_q)^{-5}$$

where μ_e and μ_q are the electron and quark chemical potentials, respectively.

3.1. Model Parameters and Physical Constraints

Our numerical analysis of the thermal evolution of XMMU J1732 requires a careful selection of both microscopic and macroscopic parameters. The microscopic parameters describe the physical properties of CFL strange quark matter, while the macroscopic parameters govern the star's initial conditions and its subsequent evolution. These parameters are chosen based on theoretical constraints,

alignment with recent astrophysical observations, and consistency with the measured properties of XMMU J1732 itself (Doroshenko et al. 2022), including its estimated age of 2–6 kyr (Cui et al. 2016).

The microscopic parameters determine the EoS and transport characteristics of matter in the CFL phase (Section 2.1). However, not all of them significantly influence long-term thermal evolution (Section 2.3). Wang et al. (2019) showed that, for a given mass, variations in CFL EoS parameters have only a limited effect on r-mode instability. Accordingly, we fix the strange quark mass $m_s = 93$ MeV, the effective bag constant $B_{\text{eff}} = 144.3$ MeV, and the perturbative QCD correction parameter $a_4 = 0.55$. We adopt $m_s = 93$ MeV, in agreement with recent lattice QCD results and the Particle Data Group compilations (Group et al. 2022). For the effective bag constant, we choose a value that ensures absolute stability of strange quark matter while reproducing the mass-radius relation of XMMU J1732 and satisfying the two-solar-mass constraint from observed pulsars. We use $a_4 = 0.55$, consistent with prior spin-based constraints (Zhou et al. 2018), NICER data (Li et al. 2021), and the upper bound inferred from GW190814 (Oikonomou & Moustakidis 2023). These parameters have only a moderate impact on global stellar properties such as mass, radius, and moment of inertia. Therefore, we fix them in our analysis to focus on the effects of the pairing gap and initial spin.

The CFL pairing gap Δ is the most uncertain microphysical parameter and plays a key role in determining both the neutrino emissivity (Equations (7)–(9)) and viscous damping, which together control the effectiveness of r-mode heating. Theoretical estimates of Δ span a wide range, and current observational constraints remain highly model dependent (Miller et al. 2019; Riley et al. 2019; Li et al. 2021; Kurkela et al. 2024). A primary goal of this study is to investigate how variations of Δ affect thermal evolution. Therefore, we explore values from 5 MeV (weak pairing) to 200 MeV (strong pairing), covering the whole range of physically plausible scenarios.

Figure 1 [Figure 1: see original paper] presents mass–radius relations for CFL strange stars using the EoS parameters discussed above. Results are shown for $\Delta = 5$ MeV and $\Delta = 200$ MeV, representing the lower and upper limits of our parameter space. For comparison, we include two representative hadronic EoSs (DDME2 and SKI6) with mass–radius constraints for PSR J0030+0451, PSR J0437–4715 and PSR J0740+6620. The observational constraints for XMMU J1732 and GW170817 are also shown. As seen in Figure 1, the CFL strange star model naturally accommodates the mass–radius properties of XMMU J1732. The inferred mass and radius lie within the predicted parameter space. This supports the hypothesis that XMMU J1732 could be a CFL strange star rather than a conventional neutron star. A special feature of the CFL model is the scaling relation $M \propto R^3$, which arises from the self-bound nature of strange quark matter, in contrast to the more intricate behavior associated with hadronic EoSs. The pairing gap Δ affects both the shape of the mass–radius curve and the maximum mass supported by the star. A larger pairing gap exponentially

suppresses neutrino cooling and increases shear viscosity, which is proportional to $\Delta^2/(_q k_B T^3)$ in the CFL phase. These effects strongly influence the star's thermal history. One of our key objectives is to constrain Δ by comparing the model predictions with the observed thermal state of XMMU J1732. The electron chemical potential $_e$ is not a free parameter but is calculated self-consistently for each EoS set by enforcing charge neutrality and chemical equilibrium within the CFL phase. For the considered parameter range, we obtain $_e = 180$ MeV.

The macroscopic parameters define the initial state and overall properties of the star. We use the observed mass, radius and redshifted surface temperature of XMMU J1732 as constraints. The initial temperature is set to $T_0 = 10^{10}$ K (8.6×10^5 eV), representative of a newly formed hot neutron star. The initial r-mode amplitude is chosen as $\alpha_0 = 10^{-10}$, which is small enough to avoid influencing early evolution while allowing us to trace the growth of r-modes (Zheng et al. 2006). We assume a magnetic field strength of $B = 10^{11}$ G, consistent with estimates for CCOs (Halpern & Gotthelf 2015; Gotthelf et al. 2024). Although magnetic effects are not explicitly included in our simulations, they could influence r-mode damping through magnetic braking or enhanced viscous dissipation (Ho & Lai 2000; Rezzolla et al. 2000; Glampedakis et al. 2006; Wang & Dai 2017).

The initial spin period P_0 of a newborn compact star is uncertain and likely depends on its formation mechanism (Faucher-Giguere & Kaspi 2006; Lorimer 2008). The initial period of PSR B0531+21 (Crab) is estimated to be 19 ms (Lyne et al. 1993) (see also Sun et al. 2024 for recent discussion). Huang et al. (2022) showed that explaining the temperature of PSR B0950+08 with rotochemical heating would require an unrealistically short $P_0 \leq 17$ ms. In addition, Du et al. (2024) analyzed young pulsars in supernova remnants (correcting for beaming bias) and concluded that the initial spin distribution peaks near 50 ms. These studies support a wide distribution of initial periods. To examine the influence of initial rotation on the r-mode heating, we consider P_0 ranging from 1 to 20 ms.

Table 1 summarizes the full set of parameters used in this study, grouped into microscopic EoS inputs, observational constraints, simulation initial conditions, and derived r-mode quantities. These parameters form the basis for our modeling of r-mode instability, thermal evolution, and quasi-equilibrium states. The normalized angular momentum $J = 0.033$, calculated self-consistently from the EoS, determines the strength of r-mode coupling and directly influences the results shown in Figures 3–5. The parameters m_s , $B_{\{eff\}}$ and a_4 define the stellar structure, while Δ primarily controls neutrino emission rate and the early thermal evolution, as shown in Figure 3(a) [Figure 3: see original paper].

3.2. R-mode Instability Window of XMMU J1732

To evaluate the conditions under which r-mode oscillations become unstable in XMMU J1732, we analyze the r-mode instability window. This window is defined by the competition between gravitational radiation, which drives r-mode growth, and viscous dissipation, which suppresses it (Andersson et al. 2002). The onset and extent of the instability window are sensitive to the star's internal temperature and the properties of the CFL phase, particularly the pairing gap Δ .

Shear viscosity plays a dominant role in damping r-modes and is strongly affected by Δ . A larger pairing gap enhances the shear viscosity, thereby reducing the growth rate of r-modes. To quantify this behavior, we compute the r-mode instability window for several pairing gap values ($\Delta = 5, 10, 50, 100, 150$, and 200 MeV), using the EoS described in Section 2.1. The relevant timescales are the gravitational radiation timescale $\tau\{GR\}$ and the shear viscosity timescale $\tau\{sv\}$.

Figure 2 [Figure 2: see original paper] shows the spin evolution and r-mode instability window for XMMU J1732. Panel (a) shows spin evolution curves for different pairing gap values (Δ ranging from 5 to 200 MeV) with an initial spin period of $P_0 = 1$ ms. The error bar indicates the age constraint (2–6 kyr) and the corresponding predicted spin period range (6–9 ms). The results indicate that the spin-down rate is only weakly dependent on Δ , suggesting that the loss of angular momentum via r-mode emission is relatively insensitive to the pairing gap across the explored parameter range. From the same figure, we estimate the current spin period of XMMU J1732 to be in the range $P = 6$ –9 ms, consistent with its inferred age and assuming r-mode driven spin evolution.

Using the model parameters listed in Table 1, we calculate the r-mode instability windows for CFL strange stars across different Δ . Figure 2(b) shows the instability windows along with corresponding spin evolution curves. The shaded regions represent the temperature-frequency parameter space where r-modes are unstable and can grow. The close overlap of the instability boundaries for different Δ indicates that the r-mode instability window is only weakly sensitive to the pairing gap. This weak dependence arises because the dominant damping mechanism, shear viscosity, is primarily controlled by electron-electron scattering. Its temperature dependence, T^{-5} , does not vary significantly with Δ within the parameter range we considered, as shown in Equation (13). In contrast, bulk viscosity is strongly suppressed in the CFL phase and plays a negligible role in r-mode damping (Alford et al. 2008). The detailed shape of the instability window also depends on the EoS.

The error bar in Figure 2(b) indicates the internal temperature inferred from the observed surface temperature, highlighting the connection between observable quantities and internal properties of the star. The critical frequency ω_c delineates the transition between stable and unstable regimes. If the stellar spin frequency is below ω_c , viscous damping dominates, and r-modes are suppressed.

Conversely, if the spin frequency exceeds ω_c , gravitational wave emission drives r-mode growth, resulting in angular momentum loss and heating. Thus, ω_c is an essential quantity in evaluating the influence of r-mode activity on the thermal and rotational evolution of the star.

To provide a useful tool for further analysis and comparison, we derive a semi-analytical expression for the critical frequency ω_c as a function of internal temperature T :

$$\omega_c = 280.4 \text{ Hz} - 29.8 \log_{10}(T/10^8 \text{ K})$$

This empirical fit is based on numerical results shown in Figure 2(b) and is valid over the temperature range $T \in 10^7\text{--}10^9 \text{ K}$. The fitting accuracy is typically within 10% across this range. From the observed redshifted surface temperature of XMMU J1732, we obtain a critical frequency of $\omega_c = 280.4 \text{ Hz}$. The corresponding r-mode heating rate is estimated to be $H_{\text{sv}} = 1.27 \times 10^{34} \text{ erg s}^{-1}$, which is consistent with the observed thermal luminosity of $10^{33} \text{ erg s}^{-1}$ (Doroshenko et al. 2022). This consistency supports the interpretation that r-mode heating is the dominant mechanism sustaining the observed surface temperature of XMMU J1732.

3.3. Thermal Evolution of XMMU J1732

Figure 3 [Figure 3: see original paper] presents the thermal and r-mode amplitude evolution for $P_0 = 1 \text{ ms}$ and $\alpha_{\text{sat}} = 10^{-2}$. Panel (a) shows thermal evolution curves for six different values of the pairing gap, with and without r-mode heating. The pairing gap significantly affects the cooling behavior during the first 100 yr by modulating neutrino emissivity. Beyond this stage, when photon emission becomes the dominant cooling mechanism, the surface temperature curves corresponding to different Δ values converge. At an age of 4 kyr, the spread in surface temperature predictions across the full range $\Delta = 5\text{--}200 \text{ MeV}$ is less than approximately 15% for a fixed saturation amplitude α_{sat} .

As shown in Figure 3(a), in the absence of r-mode heating (lower set of curves), the star cools rapidly and fails to reproduce the observed surface temperature. When r-mode heating is included (upper set of curves), the model successfully reproduces the observed temperature range of XMMU J1732. During the early evolutionary state ($t < 100 \text{ yr}$), cooling is dominated by neutrino emission, which is highly sensitive to the pairing gap Δ . At later times, photon emission becomes the dominant cooling mechanism, and the dependence on Δ decreases to below 5%.

The thermal evolution of XMMU J1732 can be explained by r-mode heating, where the heating power is governed by the saturation amplitude α_{sat} . A higher α_{sat} corresponds to more efficient dissipation of rotational energy, resulting in a higher internal temperature and slower cooling. The appearance of a temperature plateau in the r-mode heated curves reflects a quasi-equilibrium

state, where heating from r-modes balances surface photon emission. The equilibrium temperature is thus set by the magnitude of α_{sat} .

Figure 3(b) shows that the r-mode amplitude reaches its saturation value within a few years after the star's birth and remains nearly constant thereafter. Figure 4 [Figure 4: see original paper] shows how α_{sat} determines the balance between r-mode heating and surface photon cooling. We adopt $\Delta = 100$ MeV as our reference value, representative of a moderate pairing scenario. Since thermal evolution becomes nearly insensitive to Δ after 100 yr (with variations less than 5%), this choice is sufficient to constrain α_{sat} . The observed temperature range provides limits on α_{sat} , yielding bounds of approximately 8×10^{-3} – 1.4×10^{-2} for $P_0 = 1$ ms.

We also test the effects of different initial spin periods. Figure 5 [Figure 5: see original paper] shows that for $P_0 > 18$ ms, r-mode heating becomes ineffective as the star quickly spins down below the critical frequency, stabilizing the r-mode. Consequently, sustaining the observed temperature requires a relatively rapid initial rotation ($P_0 < 18$ ms). Based on this constraint, we examine models with $P_0 = 1, 13$, and 18 ms.

Figure 5(b) shows the spin evolution for various P_0 corresponding to the stable regime below the critical period (from Equation (14)). Stars born with $P_0 > 18$ ms quickly cross into the stable regime and cease r-mode heating (as shown in Figure 5(a)). In contrast, shorter initial periods provide a larger rotational energy reservoir, enabling prolonged heating.

Using the observational constraints on surface temperature and age, we estimate the current spin period of XMMU J1732 by scanning across $\Delta = 5$ –200 MeV. The resulting ranges for spin period and equilibrium temperature are summarized in Table 2.

3.4. Quasi-Equilibrium Temperature and Constraints on R-mode Parameters

In the CFL phase, neutrino emission is significantly suppressed due to quark pairing. As the star evolves and the r-mode amplitude reaches its saturation value, the system enters a quasi-equilibrium state in which the thermal evolution is governed by the balance between r-mode heating and surface photon emission. This balance determines the quasi-equilibrium surface temperature of the star and can be written as:

$$H_{\text{sv}} = L_{\gamma}$$

where the surface photon luminosity is given by:

$$L_{\gamma} = 4\pi R^2 \sigma T_{\text{s}}^4 (1 - 2GM/(Rc^2))$$

where σ is the Stefan-Boltzmann constant and $r_g = 2GM/c^2$ is the gravitational radius.

Substituting the expressions for $H_{\{sv\}}$ (Equation (12)) and L_{γ} (Equation (16)), and the shear viscosity timescale $\tau_{\{sv\}}$ due to electron-electron scattering (Equation (13)), and using $J = 0.033$, the known parameters $M = 1.53 \times 10^{33}$ g, $R = 1.04 \times 10^6$ cm, $e/q = 0.1$ (calculated from the EoS in Section 3.1), we derive the following relation for the redshifted surface temperature as a function of the r-mode saturation amplitude and angular velocity:

$$T_{s,\infty} = 2.1 \times 10^6 \text{ K} \times (\alpha_{\{sat\}}/10^{-2})^{(1/4)} \times (\Omega/10^3 \text{ s}^{-1})^{(1/2)}$$

This expression reveals that a larger r-mode amplitude and/or a higher spin rate result in stronger r-mode heating, leading to an increased equilibrium surface temperature. This relationship is illustrated in Figure 4.

Using the observed surface temperature $T_{s,\infty} = 2 \times 10^6$ K for XMMU J1732, we find:

$$\alpha_{\{sat\}} \Omega^2 = 10.8 \text{ rad s}^{-3}$$

Expressing the angular velocity in terms of the spin period ($\Omega = 2\pi/P$), we derive a direct relation between the r-mode saturation amplitude and the spin period:

$$\alpha_{\{sat\}} = 0.27 \times (P/10 \text{ ms})^2$$

Equation (19) provides a quantitative link between the thermal and rotational evolution of the star. As discussed in Section 3.3, we consider a range of initial spin periods, which lead to different constraints on $\alpha_{\{sat\}}$. *The inferred values are broadly consistent with theoretical expectations from nonlinear mode coupling models, which predict saturation amplitudes in the range $\alpha_{\{sat\}} = 10^{-4}$ – 10^{-2}* (Bondarescu et al. 2009). This range reflects the complex nonlinear interactions among fluid modes that naturally limit the amplitude of r-mode oscillations to values well below unity. The consistency between our model predictions and theoretical estimates supports the role of r-mode heating as the mechanism sustaining the thermal luminosity of XMMU J1732.

Moreover, Equation (19) provides a testable prediction. A future detection of coherent pulsations from XMMU J1732 would allow a direct measurement of its spin period, and allow empirical validation of the inferred $\alpha_{\{sat\}}-P$ relation. Confirmation of this relation would further support the r-mode heating scenario and strengthen the case for interpreting XMMU J1732 as a CFL strange star. Conversely, a significant discrepancy would imply the need to revise either the assumed saturation mechanism or the underlying microphysical properties of the dense matter phase.

4. Conclusions and Discussion

In this work, we present a detailed thermal evolution model for the central compact object XMMU J1732, located in the supernova remnant HESS J1731–347. Our model includes r-mode heating in a self-consistent CFL phase strange star. This approach extends earlier studies that mainly focused on mass–radius constraints. We directly connect the thermal properties of XMMU J1732 to microscopic parameters that govern the CFL phase and r-mode instability. This allows for a more complete understanding of this unusual object. Our thermal evolution model, which includes r-mode heating in a CFL strange star, successfully explains the observed high temperature and low mass of XMMU J1732. This makes it a strong alternative to standard neutron star models.

Our results suggest that r-mode heating is the main internal heat source in young compact stars with CFL quark matter cores. We constrain the r-mode saturation amplitude α_{sat} to be between 8×10^{-3} and 1.4×10^{-2} for an initial spin period of 1 ms. This range agrees with theoretical predictions from mode coupling studies (Bondarescu et al. 2009). We also constrain the initial spin period P_0 to be less than about 18 ms. If the star had spun more slowly at birth, it would have cooled too quickly through r-mode emission to match the observed thermal properties. Our model predicts a current spin period of 6–9 ms for XMMU J1732. This rapid rotation is consistent with the lack of detected pulsations, which may result from unfavorable viewing geometry or weak pulsed emission (Lorimer 2005; Faucher-Giguere & Kaspi 2006; Wu et al. 2021).

The predicted rapid spin of XMMU J1732 sets it apart from other CCOs. Only four CCOs have currently measured spin periods and period derivatives, and all of them rotate much more slowly, with periods around 0.1 s (Halpern & Gotthelf 2015; Gotthelf et al. 2024). This difference may reflect variations in initial spin periods, saturation amplitudes, magnetic fields, or the EoS. Finding a rapidly rotating CCO would have important implications for our understanding of CCO evolution and the physics of dense matter. Future comparisons of thermal and spin properties across the CCO population will be important for addressing these questions.

While our model provides a self-consistent explanation for XMMU J1732, it relies on several simplifying assumptions. We assume spherical symmetry and a uniform internal temperature. These assumptions can affect thermal transport, potentially introducing deviations in the equilibrium temperature estimate. Detailed studies of anisotropic temperature distributions in neutron stars with magnetic fields (Geppert et al. 2004; Aguilera et al. 2008) have shown that surface temperature variations of 10%–15% are typical when comparing 2D models to spherically symmetric ones. Potekhin et al. (2015) further confirmed that internal temperature gradients can modify the overall thermal evolution by similar amounts. Since r-mode heating is distributed throughout the star, rather than confined to localized regions, the impact of these simplifications on our main conclusions is expected to be limited to corrections of this magnitude.

We have also considered the effect of magnetic fields. For XMMU J1732, the inferred field strength is $B \sim 10^{11}$ G, typical of CCOs. The results in Wang & Dai (2017) suggest that such fields modify r-mode damping timescales by less than 5%. Including magnetic effects would improve quantitative accuracy but is unlikely to change the qualitative results. Future studies incorporating magnetic damping mechanisms (Rezzolla et al. 2000; Ho & Lai 2000; Glampedakis et al. 2006) and improved modeling of the EoS of CFL phase quark matter will further refine the results.

Future observations will be the key factor in testing and refining our model. Continued efforts to detect radio emission or place tighter constraints on the pulsed fraction are important for confirming the predicted rapid rotation. High-precision timing observations with next-generation facilities offer a promising way for achieving these goals and potentially measuring the spin period directly. Although the direct detection of gravitational waves from r-mode remains a significant challenge, future advances in detector sensitivity (e.g., with third-generation detectors like Cosmic Explorer and Einstein Telescope) might eventually make this possible, providing a direct probe of the r-mode mechanism and the internal dynamics of these compact objects.

In conclusion, our results support the identification of XMMU J173203.3–344518 as a rapidly rotating CFL strange star heated by r-mode dissipation. This model explains the unusual properties of the object, constrains key parameters such as the r-mode amplitude and initial spin period, and offers a new path to study dense matter in extreme environments. These findings show that r-mode may play an important role in the early thermal and spin evolution of compact stars and emphasize the need for continued observational and theoretical investigations to understand the nature of these kinds of compact objects.

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