Optimized GPU-accelerated Monte Carlo program for real-time dose estimation directly using mesh-type computational phantoms

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Abstract

Mesh-type phantoms represent the latest generation of human computational phantoms, offering advantages of high resolution and adjustability for individualized radiation dosimetry. Current dosimetry computation methods, which require conversion to tetrahedral mesh models for efficient Monte Carlo simulations, still fail to meet the requirements for real-time dose calculations. Advancements in heterogeneous computing now enable significant acceleration in mesh-type phantom calculations through the utilization of both high-performance hardware and efficient algorithms. This study aims to develop a GPU-accelerated Monte Carlo simulation method that directly employs mesh-type phantoms to further enhance the speed of human dose calculations without necessitating tetrahedralization. For boundary representation polygonal models, this study redesigned and implemented the entire procedural flow of the GPU-accelerated Monte Carlo program, developing particle transport methods within the mesh-type model. All triangular facets of the mesh-type model were constructed into a tree-like acceleration structure, and the traversal access pattern was optimized. Furthermore, this study adopted an event-based transport method, transporting particles stepwise by particle type, and integrated a bias-based variance reduction technique employing geometric weights. For typical external irradiation scenarios, dose calculations from Geant4 and our GPU-based program were compared to assess computational accuracy and efficiency. Compared to benchmark simulations conducted on a single-thread CPU via Geant4, organ dose discrepancies calculated by the GPU-accelerated program generally remained within a 5% margin, while computational times were reduced by factors ranging from 500 to 50,000. To our knowledge, this study represents the first utilization of a mesh-type model for GPU-accelerated dose calculation without tetrahedralization. Simulation

time has been dramatically reduced from hours to mere seconds, offering a rapid and precise Monte Carlo method for mesh-type computational phantoms. This development supports real-time dose calculation studies using dynamic mesh-type models, providing a robust Monte Carlo simulation tool.

Full Text

Preamble

Optimized GPU-accelerated Monte Carlo program for real-time dose estimation directly using mesh-type computational phantoms

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Mesh-type phantoms represent the latest generation of human computational phantoms, offering high resolution and adjustability advantages for individualized radiation dosimetry. Current dosimetry computation methods, which require conversion to tetrahedral mesh models for efficient Monte Carlo simulations, still do not meet the requirements for real-time dose calculations. Advancements in heterogeneous computing now allow for significant acceleration in mesh-type phantom calculations by utilizing both high-performance hardware and efficient algorithms. This study aims to develop a GPU-accelerated Monte Carlo simulation method that directly utilizes mesh-type phantoms to further enhance the speed of human dose calculations without the need for tetrahedralization. For the boundary representation polygonal models, this study redesigned and implemented the entire procedural flow of the GPU-accelerated Monte Carlo program, developing particle transport methods within the mesh-type model. All triangular facets of the mesh-type model were constructed into a tree-like acceleration structure and the traversal access pattern was optimized. Moreover, this study adopted an event-based transport method, transporting particles step-by-step by particle type, and a bias-based variance reduction technique employing geometric weights was integrated. For typical external irradiation scenarios, dose calculations between Geant4 and our GPU-based program were compared to assess computational accuracy and efficiency. Compared to the benchmark simulations conducted on a single-thread CPU via Geant4, the organ dose discrepancies calculated by the GPU-accelerated program generally remained within a 5% margin, while computational times were reduced by factors ranging from 500 to 50000. To our knowledge, this study is the first to utilize a mesh-type model for GPU-accelerated dose calculation without tetrahedralization. The simulation time has been dramatically reduced from hours

to just mere seconds, offering a rapid and precise Monte Carlo method for mesh-type computational phantoms. This development supports real-time dose calculation studies using dynamic mesh-type models, providing a robust Monte Carlo simulation tool.

Keywords: GPU Monte Carlo, Mesh-type phantom, Heterogeneous, Real-time dose

INTRODUCTION

Monte Carlo (MC) simulations employing computational phantoms serve as a crucial method for human dose assessment. The boundary-represented mesh-type models, as the latest generation of computational phantoms, offer the dual benefits of flexible deformability and high resolution, which better represent the dosimetric characteristics of real human body [**?**, **?**, **?**]. Consequently, mesh-type phantoms have demonstrated significant potential in the fields of radiation therapy, radiation protection, and individual dosimetry, where more accurate models are essential for obtaining precise individual doses [**?**, **?**, **?**, **?**].

However, employing mesh models directly in MC simulations for dose calculations introduces challenges [**?**]. In MC simulations, accurately defining the relationships between particles and their surrounding geometrical structures is essential [**?**, **?**]. The mesh-type phantoms used for MC simulations are typically composed of polygonal grids, primarily based on triangular meshes [**?**]. Other polygonal mesh models can also be easily subdivided into triangular meshes. Direct use of the mesh-type phantom containing a large number of triangular facets for these computations notably reduces computational speed, with research indicating that such use increases computational time by 70 to 150 times compared to voxel models [**?**]. In response, a novel method involving tetrahedral decomposition [**?**, **?**] has been developed to expedite computations for mesh phantoms [**?**, **?**], and the resulting tetrahedral models also support posture adjustments [**?**]. While this tetrahedralization simplifies the determination of geometric relationships during particle transport, the subdivision of the mesh into tetrahedra substantially increases the internal complexity, which impedes further acceleration of computation speeds [**?**]. Thus, in fields like clinical radiotherapy, nuclear medicine, and accident dose reconstruction, where strict time constraints are crucial, the computational time of mesh-type models often exceeds acceptable limits, restricting their applicability in these critical areas [**?**, **?**].

In recent years, the rapid development of GPU hardware and continual optimization of ray-tracing software algorithms have made it feasible to directly employ boundary-represented models for dose calculations [**?**, **?**, **?**, **?**]. GPUs, with their superior floating-point computational capabilities and increased thread count, are better suited for large-scale particle simulations compared to CPUs [**?**, **?**]. Consequently, numerous GPU-accelerated programs for photon and photon-electron coupled transport have been developed, achieving significant

acceleration [?, ?, ?, ?, ?, ?]. Our group has previously developed the first GPU-accelerated MC transport program based on tetrahedral phantoms. However, due to issues with GPU thread divergence [?] and the increased internal complexity caused by tetrahedralization [?], the computational time of the tetrahedral GPU-accelerated MC program remains at the level of tens of seconds to minutes. Once the direct computation with mesh-type phantoms is achieved, bypassing the tetrahedral segmentation step and addressing the slow particle-to-geometry positioning, there is potential for further improvements in computational efficiency. To the best of our knowledge, current popular GPU MC programs have not yet implemented GPU acceleration directly based on mesh-type models. The principal challenge lies in the complexity of implementing rapid particle transport within mesh-type models on GPUs [?]. Additionally, GPU-based MC programs often face significant thread divergence issues due to the considerable variability among different particle transport processes [?, ?]. Furthermore, smaller organs tend to present larger statistical errors in dose results because of the lower probability of particle interactions [?], necessitating an increase in the number of simulation particles to achieve more accurate dosimetry, which significantly extends the simulation time.

To further enhance the computation speed for dose calculation in mesh-type phantoms, this study implemented GPU-based MC simulation program directly utilizing boundary-represented mesh models. This involved redesigning the entire procedural flow of particle transport. All triangular facets of the mesh model were organized into a tree-like acceleration structure and the traversal access pattern was optimized, significantly reducing the complexity of geometric localization and intersection calculations during particle transport. Furthermore, this study adopted an event-based transport method, conducting multiple simulations in which particles of the same type were transported for a single step during each simulation, rather than relying on a single thread to transport one particle until termination, which greatly reduced thread divergence and improved hardware utilization. The introduction of multi-GPU parallel processing further accelerated the computation speed. Additionally, we employed a biasing sampling technique based on geometric weights for variance reduction, significantly reducing statistical errors in smaller organs and decreasing the number of simulated particles. Rigorous validation of the program demonstrated precise computational outcomes and substantial acceleration, effectively addressing the challenges associated with enhancing dose calculation speed for mesh-type phantoms.

II. MATERIALS AND METHODS

This study presents the development of a program that directly utilizes a mesh-type model for GPU-accelerated MC simulations. Various optimization techniques, including event-based transport, multi-GPU parallelism, and variance reduction methods, were then implemented to further enhance the computational speed. Finally, the accuracy of the GPU program was validated, and the

effectiveness of the optimization methods in accelerating the simulations was assessed.

A. GPU-based Monte Carlo program for mesh-type phantom

1. Constructing flat acceleration structure In MC simulations, determining both the physical and geometric step sizes requires the material cross-section information at the particle' s location, as well as the distance to the boundary along the particle' s trajectory [**?**, **?**, **?**]. For mesh-type phantoms, it is necessary to traverse all triangular facets, to perform particle localization and intersection operations. The repetitive traversal operation, which must be performed for each particle transport step, is time-consuming. To enhance traversal efficiency, the implementation of acceleration structures becomes crucial [**?**, **?**, **?**]. These structures systematically organize data into layers, significantly reducing the number of searches and enhancing query efficiency. Given this context, we construct a tree-based acceleration structure for all triangular facets of the mesh-type phantom, to substantially reduce the time complexity of data traversal. Considering both time complexity and the need for dynamic updates beneficial for phantom adjustments [**?**], we choose to implement a Bounding Volume Hierarchy (BVH) tree, which is widely used in ray tracing and animation [**?**]. While the BVH acceleration structure can theoretically handle other polygonal elements, such as polygons with arbitrary shapes as leaf nodes, we primarily focus on triangular meshes due to their prevalence in human phantoms, like the ICRP' s MRCP model. Furthermore, using triangular facets simplifies classification and traversal, making it more efficient and suited to the requirements of dose calculations.

The constructing process of BVH tree begins with calculating a bounding box for all triangles, which forms the parent node [**?**]. These triangles are then divided into two groups based on a specific pattern, such as an average division by quantity. The bounding box calculation and division process continue for the two child nodes until the number of triangles in a subdivided child node falls below a specified threshold, at which point it becomes a leaf node and stores the information of the included triangles, as illustrated in figure 1 [Figure 1: see original paper]. An effective partitioning strategy is essential. When geometric objects in a scene are unevenly distributed, traditional partitioning methods may yield an unbalanced tree structure, which can reduce traversal efficiency. To optimize this process, the Surface Area Heuristic (SAH) is typically employed [**?**, **?**]. The SAH evaluates the cost of each partition by calculating the surface area of the resulting child bounding boxes. This method explores various partitioning schemes and selects the one with the lowest cost for implementation. Such optimization can significantly reduce unnecessary intersection tests between rays and bounding boxes during ray tracing, thereby enhancing overall intersection efficiency.

In mesh-type phantoms, the presence of numerous triangular facets results in a deeply nested and complex acceleration structure. This complexity presents sig-

nificant challenges for GPU computing, which is limited by stack depth [**?**]. Such constraints restrict the number of recursive calls and the depth of data structures that can be processed, adversely affecting the performance of recursive algorithms traversing these structures. To overcome this limitation, the flattening of acceleration structure becomes essential. This process involves converting the tree structure into a linear format for efficient processing on GPUs [**?**]. Our implemented "tree flattening" method is illustrated in figure 1. We record the indices of child nodes separately in the node sequence rather than creating new child nodes directly within each node. This strategy produces two sequences: one containing a list of BVH nodes that sequentially stores information for each node, and another comprising a list of triangular facets that sequentially records the geometric and material information associated with the leaf nodes. The flattening of the BVH tree structure circumvents the limited stack depth of GPUs by avoiding nested configurations. This architectural adjustment ensures that more complex phantom acceleration structures can be efficiently processed on GPUs.

2. Transport in the acceleration structure composed of numerous triangles The particle transport process within the mesh model is depicted in figure 2 [Figure 2: see original paper]. Particles are generated through sampling on the GPU and subsequently transported in a stepwise manner until termination [**?**]. As previously noted, localization and intersection operations represent the most critical and time-consuming aspects of particle transport. Localization is necessary to obtain the material information of the geometry where the particle resides, allowing for energy interpolation to derive the reaction cross-sections and sample the physical step length. The intersection operation determines the distance to the nearest geometric boundary in the direction of particle motion, thereby determining the geometric step length. By comparing the physical step lengths associated with various reactions to the geometric step length for transport, the minimum value is selected to ascertain whether a reaction occurs or the particle is transported to the boundary [**?**, **?**]. This process is repeated until the particle and its secondary particles are terminated.

Determining the relationship between particles position and mesh structures typically involves emitting a virtual ray from the particle, often aligned with the coordinate axes, as illustrated in figure 3 Figure 3: see original paper. The number of intersections and the corresponding distances are used to ascertain the current geometry and material of the particle. Generally, the geometry with an odd number of intersections that is closest to the particle is selected. Calculating the geometric step length requires determining the distance to the nearest grid boundary along the particle' s direction of motion, which also necessitates intersection operations. By integrating these two processes, both particle localization and intersection detection can be accomplished simultaneously, as shown in figure 3(b).

To further enhance the efficiency of these procedures, we pre-assign additional

information to the triangular facets of the mesh model. Specifically, we add the normal vector for each triangular facet, indicating the outward direction from the interior of the mesh geometry, and specify the materials associated with the outward and inward normal. By identify the nearest intersection point and intersecting triangle, we can determine the material in which the particle is currently located by assessing the relationship between the particle' s motion direction and the triangle' s normal direction, as depicted in figure 3(c). This approach eliminates the need to count intersections and assess the number of intersection points with the same geometry, thereby reducing computational time.

The preceding discussion focused on the transport of particles after their intersection; however, it did not detail the methods for quickly intersecting a large number of triangles based on particle position and directional information. This is where the acceleration structure we previously constructed becomes essential. We will establish an empty stack of intersection nodes, placing the first node of the flat acceleration structure node sequence at the top of this stack. Next, we will fetch the top node from the stack. If this node is not a leaf node, we will perform an intersection operation between the particle' s direction of motion and the two child bounding boxes of this node. If an intersection occurs, the corresponding child nodes of the intersecting bounding boxes will be added to the top of the stack. If the fetched node is a leaf node, we will traverse the few triangular facets within it to perform ray-triangle intersections, recording information about any intersecting triangles. This process continues until the stack is empty, at which point we select the shortest intersection distance as the geometric step length and determine the intersecting triangle. Subsequently, we will use the material information associated with the inward and outward normal to identify the material at the particle' s position. Pseudocode illustrating this more intuitively is shown in the algorithm 1.

Algorithm 1: Particle intersection and localization within acceleration structure

Input: Particle position, particle direction, and acceleration structure
Output: Result of intersection and localization

```
Push the root node onto the stack;
min distance = $\infty$;
while stack is not empty do
    node = Pop top node from stack;
    if node is a leaf node then
        for each triangle in node.triangles do
            Check if particle intersects with the triangle;
            if intersection distance < min distance
                min distance = intersection distance;
                Update intersecting triangle;
    else
        if particle intersects with the bounding box of left child node then
```

```
            Push left child node onto the stack;
        if particle intersects with the bounding box of right child node then
            Push right child node onto the stack;
end
if intersection exists then
    triangle = Get intersecting triangle;
    material = dot product(triangle.normal, particle.direction) > 0 ? triangle.inMat : triar
    geometric step length = min distance;
else
    Kill particle;
```

3. Program implementation framework Given that dosimetry simulations in the human body involve the physical processes of coupled photon-electron transport, the GPU MC program developed in this study provides a comprehensive simulation of these coupled transport processes, utilizing the same physical models and cross-sectional data previously researched by our team [**?**]. This GPU program effectively simulates the physical interactions for photons and electrons across an energy range from 0.001 MeV to 100 MeV. For photons, photoelectric absorption, Compton scattering, and pair production are considered. For electrons and positrons, the physical processes include bremsstrahlung radiation, ionization effects, multiple scattering, and positron annihilation. Furthermore, the foundational framework and initialization procedures remain consistent, requiring only the integration of the reading mesh models and construction processes for acceleration structure. On the GPU side, particle transport employs the transport method described in the previous section. The workflow of the GPU MC program for photon and electron transport using the mesh model is illustrated in figure 4 [Figure 4: see original paper]. A history-based transport method is utilized, in which each GPU thread simulates a single particle from its generation to termination [**?**, **?**]. Thus far, we have successfully developed a GPU MC program for dose calculation that directly utilizes the mesh model. The subsequent sections will focus on optimizing and enhancing this program.

B. Event-based transport method

Solving thread divergence issues GPUs contain numerous threads, which are organized into groups of 32, known as "warps" , for efficient management and scheduling. Within a warp, all 32 threads execute instructions in a lock-step manner, meaning that any instruction to be executed by any thread in the warp must be performed simultaneously [**?**, **?**]. When a branching instruction is encountered, the entire warp executes the whole branches taken by any thread. In such cases, if different threads within the warp follow distinct code branches, thread divergence occurs. Although divergence does not affect the correctness of individual thread computations, it significantly impacts code performance. This phenomenon is particularly prevalent in GPU MC simulations. Traditional MC particle transport algorithms typically rely on historical transport methods,

akin to the GPU MC program implemented in the previous section, where each thread simulates the transport of a single particle until its lifecycle concludes, as illustrated in figure 4 [Figure 4: see original paper]. However, during the simulation, the transport path lengths and times of different particles can vary significantly [**?**, **?**]. For instance, some particles may be "killed" after one single step, while others may require multiple transport steps, as shown in figure 5 [Figure 5: see original paper]. Consequently, substantial code branching often occurs when different threads within the same warp handle particles with vastly different transport characteristics, leading to severe thread divergence.

To address this issue, relevant studies have proposed an event-based transport method [**?**, **?**, **?**], which divides particle processes into distinct event types. Each GPU batch processes only one type of event at a time, and then cycles through them. This approach ensures that all GPU threads execute the same type of event simultaneously, such as performing a single step of photon geometrical transport. Once the transport is completed, the initial or generated secondary particles are reallocated to sort and consolidate the surviving particles, followed by a subsequent execution. As illustrated in figure 5, this method significantly reduces the divergence of GPU threads, thereby improving hardware utilization and computational efficiency.

Implementation method in the GPU program Building upon the GPU-based MC program developed in the previous section using the mesh-type model, we extend its functionality to implement an event-based transport method. The implementation process is illustrated in the figure 6 [Figure 6: see original paper]. We modify the previous approach of looping through the transport steps of a single particle by removing the loop for particle transport within the GPU kernel function and replacing it with a stepwise transport kernel method. To facilitate classification by particle type, we prepare an event particle library in advance, which stores the particles after each batch transport step. Furthermore, we establish multiple sequences for the different events to record particle indices in the event particle library. The division of particle transport processes for photons, electrons, and positrons allows us to invoke the GPU MC program to transport the particle type with the largest count at each step, as the reaction sampling for the same particle type is generally consistent, resulting in minimal thread divergence. Upon completion of one transport step, we categorize the current particles (if still alive) and the generated secondary particles according to their types and repeatedly invoke the GPU transport program until the number of particles in the event particle library to be simulated falls below a predetermined threshold. The event-based transport method introduces additional operations compared to the history-based approach, such as multiple GPU kernel function calls and the need for particle sorting and data synchronization, which incurs extra time costs. Consequently, when the particle count is low, continuing with the aforementioned event-based transport may reduce efficiency. Therefore, we opt to transport the remaining particles below a predetermined threshold directly using the history-based method until they are

terminated.

C. Multi-GPU parallel optimization

Due to the limitations of single GPU simulations constrained by the number of threads, we considered utilizing multiple GPUs to overcome the current acceleration limits through an increase in hardware. In the previous single GPU workflow, the CPU reads and initializes data, which is then transferred to the device, followed by the GPU executing the simulation computations, and finally, the results are returned to the host for post-processing. Simply replicating this process via multi-threading on the CPU, where each thread independently executes the full workflow using different GPUs, would result in redundant initializations. This redundancy is inefficient due to the substantial size of the phantom data and physical model cross-sections, which can significantly increase processing time and memory usage, potentially exceeding computer memory limits if many GPUs are employed. Moreover, each new simulation iteration, such as updating source term information, requires the complete re-execution of this workflow, leading to considerable delays.

To achieve more efficient multi-GPU parallelism, we transformed the executable simulation program into a library named "Simulation", followed by a restructuring of the code architecture into independently executable modules. By loading this library in the main program and creating an instance of the simulation class, different functions can be invoked through this object to operate the modules separately. This approach significantly reduces the redundancy of initialization and data transfer processes. The updated code framework is depicted in figure 7 Figure 7: see original paper. The initialization module is embedded in the constructor of the simulation class. This module is invoked automatically when a new class object is created and is responsible for initializing the physical and geometrical models. This process is executed only once and the data is subsequently transferred to the corresponding GPU. The update module can be executed independently before each simulation to modify source information and update geometric data. This module involves a smaller data volume and also requires transferring the updated data to each GPU. The final component, the GPU particle transport module, utilizes multi-threading to start particle simulation on corresponding GPUs. Considering the significant computational power discrepancies among different GPUs, a load balancing mechanism that assigns simulation particle counts based on the number of CUDA (Compute Unified Device Architecture) cores in each GPU has been incorporated in this module, as shown in figure 7(b).

D. Implementation of variance reduction in the GPU MC program

In human organ dose simulations, results are considered reliable when statistical errors are relatively small [**?**]. However, due to significant variations in the size, position, and shape of different organs, statistical errors also vary considerably. Typically, smaller organs are less likely to be reached by particles, making

these interactions rare and requiring a large number of simulated particles for accurate results [**?**]. In contrast, larger organs do not require such extensive particle simulations. By employing variance reduction techniques that increase particle transport in smaller organs, the total number of particles required for simulations can be significantly reduced, enhancing computational efficiency.

Biasing variance reduction techniques are widely used in mainstream MC simulation programs to decrease computational variance by artificially adjusting particle weights and quantities. Among these, the region importance biasing method is particularly prevalent [**?**]. The central principle of this method is to assign higher importance to regions of interest and lower importance to less critical areas. Modifications of particle numbers and weights can be achieved through strategies such as surface splitting and Russian roulette based on the importance assigned to these regions. Theoretically, optimal variance reduction can be achieved by precisely setting the bias parameters. Given the fixed structure of human models and the consistent size of internal organs, employing regional importance sampling is appropriate for addressing the disproportionate consumption of particles in obtaining accurate smaller organ dose.

Based on the foundation of this work' s GPU MC simulation program, the process to implement variance reduction techniques through regional importance method is depicted in figure 8 [Figure 8: see original paper]. This process involves assigning importance parameters to both the geometries and the particles. As particles traverse geometric boundaries, they undergo transformations like surface splitting and roulette, both of which alter the particle' s importance depending on the relative importance of the current and subsequent geometries. Surface splitting generates multiple identical particles at the same location, which are then included in the particle sequence for simulation. Roulette involves a probabilistic termination of particles, wherein a particle is eliminated if a randomly drawn number exceeds the ratio of the importance values between the upcoming and current geometries. In the tally module, energy deposition must be weighted based on the current particle' s importance.

Region importance sampling, compared to other variance reduction techniques, offers an intuitive principle and straightforward implementation. However, the key lies in the rational design of importance or weight. To this end, simulations based on actual irradiation scenarios can be conducted in advance, with iterative adjustments to region importance for achieving lower statistical errors of organ doses with fewer particles [**?**].

E. Dose calculations and efficiency assessments

To assess the accuracy and acceleration efficiency of our GPU-based program, we conducted simulations on a standard external irradiation scenario (anteroposterior, AP) using the ICRP' s Mesh-type Reference Computational Phantoms (MRCPs) [**?**]. The male phantom of MRCPs was subjected to unidirectional and parallel photon and electron beams emitted from a planar source, with a

monoenergetic energy of 10 MeV. The choice of this energy was driven by the higher potential risks associated with high-energy particles, as well as the longer computation time and more complex interactions involved. The organ materials in the simulations were defined using mass fractions of various elements, with data sourced from the ICRP Publication 145.

For benchmarking, we employed Geant4 simulations on a CPU platform, adapting the source code from the supplemental material of the 145th publication for this AP irradiation scenario [**?**]. Notably, considering the slow dose calculation speed with the mesh model on CPU, we employed the tetrahedral model for simulation [**?**, **?**]. Our computational setup included Geant4 version 10.04, utilizing the Livermore physics model with secondary electron and photon energy thresholds of 0.2 MeV and 0.002 MeV, respectively. The CPU hardware specifications included 64 GB RAM (Random Access Memory) and an Intel(R) Xeon(R) CPU E5-2660 v4 @ 2.00GHz which has 28 threads.

For the GPU program developed by this study, the mesh-type phantom, instead of the tetrahedron model, was directly employed for the same irradiation scenario simulation. To further assess GPU acceleration, we conducted tests to compare computation results and times both with and without event-based transport, variance reduction techniques, and multi-GPU configurations. These simulations were performed on an NVIDIA GeForce RTX 4090 GPU, which boasts 24 GB VRAM (Video Random Access Memory), operates on CUDA version 12.2 and features 16,384 CUDA cores. The secondary electron and photon energy thresholds and the irradiation scenario were consistent with those of the benchmark.

Due to the slower performance of CPU calculations with mesh-type models compared to tetrahedral meshes, the CPU benchmark in this study employs a tetrahedral model for comparison. In contrast, the GPU simulations directly utilize mesh-type phantoms. The simulation outcomes are the external radiation absorbed dose conversion coefficients for various organs.

In summary, we simulated five configurations: (1) CPU simulation 10^8 particles (benchmark), (2) GPU simulation 10^8 particles with history-based transport method, (3) GPU simulation 10^8 particles with event-based transport method, (4) GPU simulation 10^7 particles with event-based transport and variance reduction, and (5) GPU simulation 10^7 particles with event-based transport method, variance reduction and multi-GPU mode. The objective was to evaluate the dose calculation accuracy and the acceleration efficiency of the GPU program.

III. RESULTS AND DISCUSSION

A. Comparison of calculated dose values

Figure 9 [Figure 9: see original paper] illustrates the dose results from a CPU benchmark and four GPU simulation methodologies incorporating various optimization techniques. The bar graph in figure 9 represents the absorbed doses in

various organs per fluence of photons with 10 MeV energy under AP irradiation using different simulation methods. Given that all four GPU simulation configurations are distinct modalities of our GPU MC program, and can be selected based on specific hardware conditions and simulation requirements, it is imperative to ensure the accuracy of these four computational results. We exhibit the maximum relative deviations in organ doses calculated by the four GPU methods compared to the CPU benchmark for each organ. The accompanying line graph displays the maximum deviation. Statistical uncertainty calculations in our GPU program are conducted using batch-based method [**?**, **?**, **?**]. The statistical error for most organs across the five simulation methods is within 3%. As shown in figure 9, the results for the majority of sensitive organs are consistent across all five calculation methods, with discrepancies within 5% of the benchmark, thus confirming the accuracy of the GPU program' s calculations.

To further analyse the variations among different GPU simulation methods, particularly the effects of various optimization techniques, figure 10 [Figure 10: see original paper] employs a box-and-whisker plot to illustrate the distribution of dose deviations for all organs in a mesh-type phantom across different GPU calculation methods compared to the benchmark. Each box-and-whisker (column) in figure 10 represents the distribution of dose simulation results for a particular GPU simulation scenario, with each point indicating the relative deviation of each organ' s results from the CPU benchmark. The box region represents the range of relative deviations for the half of organs. The narrower the box-and-whisker and closer its range is to zero, the more accurate the overall simulation. Notably, to better demonstrate the impact of variance reduction optimization methods, the analysis includes simulations using only the event-based method with 10^7 particles.

The left two columns of the figure 10, which represent simulations utilizing with 10^8 particles, show that the relative deviations in dose calculations for most organs are within 3%. This consistency arises because the history-based and event-based methods do not fundamentally differ in their physical models, but rather in their transport mechanisms. A comparison of these two 10^8 particle simulations (left two box plots) with the three 10^7 particle simulations (right three box plots) demonstrates that simulations with 10^8 particles exhibit noticeably smaller relative deviations. This observation aligns with statistical principles, where a higher particle count leads to lower statistical errors and more precise calculations.

Subsequent comparisons of three GPU simulation methods, each running with 10^7 particles (the right three box plots), indicate that the range of relative dose differences for all organs narrows with the application of variance reduction techniques. The results show that applying variance reduction techniques improved the accuracy of simulations with the same particle count, demonstrating the effectiveness of the method, although the accuracy still does not reach that of simulations using 10^8 particles. Nevertheless, these differences remain within acceptable limits, but significantly reduce the number of simulation particles.

B. Comparison of computation speed

Table 1 summarizes the differences in computation times across various simulation configurations. The CPU benchmark time represents the computation time using a single-core for simulation. The term "Time ratio to benchmark" indicates the ratio of other simulation computation times to the CPU benchmark time.

It reveals that the GPU-based program for mesh-type models developed in this study, when operated without event-based transport or variance reduction techniques, reduces computation time by a substantial factor of 570 compared to the single-core CPU MC program. This improvement is due to the lack of acceleration structures or efficient intersection algorithms in conventional CPU MC programs such as Geant4, whether using mesh-type models or parametric tetrahedral models. Therefore, combining GPU hardware with software optimization algorithms to accelerate mesh-type models achieves faster acceleration than the CPU with tetrahedral models, and even more so compared to the CPU with mesh-type models. Since methods involving CPUs with mesh-type models are not mainstream, they are not compared here.

Employing optimization techniques, such as the event-based transport method, further enhances performance, achieving an additional fourfold acceleration when simulating the same number of particles, which results in a total speedup of 2000 times compared to the CPU benchmark. This improvement is primarily because the event-based transport method significantly reduces thread divergence and increases hardware utilization. However, it should be noted that the need for repetitive kernel function calls and additional operations like particle sorting may slightly decrease computational efficiency.

Furthermore, utilizing both event-based transport and variance reduction techniques with fewer particles decreases computation time by 18,000 times compared to the baseline, while the relative differences in organ doses remain within acceptable ranges. However, the implementation of variance reduction techniques, which includes operations such as particle splitting and roulette, can lead to an increase in computation time.

Further acceleration can be achieved by utilizing multiple GPUs in parallel. This approach involves synchronizing data across different devices. However, due to the varying operational conditions of each device, there can be discrepancies in runtime, which means that the overall simulation computation time does not decrease proportionally with the number of GPUs used.

Considering that the MRCP used is highly detailed, with a file size and number of triangular facets approximately an order of magnitude larger than the Chinese Reference Adult Male (CRAM) phantom developed by our team [**?**], it' s important to note that while these detailed features of MRCP are crucial for accurately representing the anatomical structure, they may not always be essential for dose estimation purposes. In fact, using the same GPU MC program

under the same conditions (10 MeV photon AP irradiation with 5 RTX 4090 GPUs, simulating 10^7 particles combined with variance reduction techniques and event-based transport), the simulation time for our CRAM phantom has already been reduced to 0.78 seconds, which can essentially be considered as achieving real-time dose calculations.

In summary, the GPU-based MC program, which incorporates various acceleration and optimization methods, can significantly shorten the computation times for human phantom dose calculations to the order of second, achieving up to a 50,000-fold reduction compared to the single-core CPU MC program.

IV. CONCLUSIONS

This study presents the first instance of a GPU-accelerated MC program that performs dose calculations directly using mesh-type models without requiring conversion processes such as tetrahedralization or voxelization. By directly processing polygonal models for dose calculations, the program leverages their flexible deformation capabilities and high resolution, yielding more accurate dosimetric outcomes. Additionally, this approach eliminates the need for tetrahedral conversion and mesh repair associated with tetrahedral mesh-type phantoms, thereby simplifying the computational workflow. By incorporating GPU acceleration for MC transport, constructing acceleration structures, enabling single-step transport based on particle type, and applying variance reduction techniques along with multi-GPU parallel optimization, the simulation time for a single phantom reduces from hours to seconds, achieving up to a 50,000-fold reduction compared to the single-core CPU MC program. Furthermore, the GPU-accelerated calculation method for mesh-type phantoms, integrated with human posture capture and deformation technologies, enables real-time human dose calculations. This capability is particularly valuable in fields requiring rapid responses, such as occupational exposures, radiotherapy, accident dose reconstruction, and individual dosimetry assessment, enhancing both accuracy and applicability under tight time constraints.

There is further potential for optimization in the program. For instance, it currently transports particles based on their type. Future implementations that transport based on different reaction types may significantly reduce thread divergence. Additionally, the geometric importance for variance reduction, currently adjusted manually based on each run' s outcomes, will be automated in future settings.

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