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Xiao-Dong Nong<sup>1,2</sup> and Nan  
Liang<sup>1,2,3</sup>

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## Full Text

# Testing the Phenomenological Interacting Dark Energy Model with Gamma-Ray Bursts and Pantheon+ type Ia Supernovae

Xiao-Dong Nong<sup>1,2</sup> and Nan Liang<sup>1,2,3</sup>

<sup>1</sup> Key Laboratory of Information and Computing Science Guizhou Province, Guizhou Normal University, Guiyang 550025, China; liangn@bnu.edu.cn

<sup>2</sup> School of Cyber Science and Technology, Guizhou Normal University, Guiyang 550025, China

<sup>3</sup> Joint Center for FAST Sciences Guizhou Normal University Node, Guiyang 550025, China

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## Abstract

In this paper, we utilize recent observational data from gamma-ray bursts (GRBs) and Pantheon+ supernovae Ia (SNe Ia) samples to explore the interacting dark energy (IDE) model in a phenomenological scenario. Results from GRBs alone, SNe Ia and GRBs+SNe Ia indicate that the energy is transferred from dark energy to dark matter and the coincidence problem is alleviated. The value of  $H_0$  from GRBs+SNe Ia in the IDE scenario shows agreement with the SH0ES measurement. Considering the age estimate of the quasar APM 08279+5255 at  $z = 3.91$ , we find that the phenomenological IDE scenario can predict a cosmic age greater than that of the  $\Lambda$ CDM model, thus the cosmic age problem can be alleviated.

*Key words:* cosmology: observations –(cosmology:) dark energy –(cosmology:) cosmological parameters

## 1. Introduction

Observations of type Ia Supernovae (SNe Ia) have unequivocally demonstrated that our universe is experiencing accelerated expansion (Riess et al. 1998; Perlmutter et al. 1999; Astier et al. 2006; Hicken et al. 2009; Amanullah et al. 2010). Additional supports come from cosmic microwave background (CMB) radiation (Spergel et al. 2003, 2007; Komatsu et al. 2009, 2011) and large-scale structure (Tegmark et al. 2004; Eisenstein et al. 2005; Percival et al. 2010). However, the standard  $\Lambda$ CDM model which assumes dark energy (DE) is a cosmological constant  $\Lambda$  encounters the cosmological constant problem (Weinberg 1989; Carroll et al. 1992), encompassing the fine-tuning and cosmic coincidence issues. Moreover, the  $H_0$  tension with the discrepancy between local measurements by SNe Ia (Riess et al. 2016, 2018, 2019, 2022a, 2022b) and early Universe measurements from CMB observations (Planck Collaboration et al. 2016, 2020) under the  $\Lambda$ CDM model exceeding  $5\sigma$  represents a significant challenge in modern cosmology.

To address or mitigate the coincidence problem, many alternative dynamic models of DE have been proposed (Ratra & Peebles 1988; Caldwell et al. 1998; Armendariz-Picon et al. 2001; Bento et al. 2002; Caldwell 2002; Chiba 2002; Caldwell et al. 2003; Feng et al. 2005). The interacting dark energy (IDE) models, which involve potential interactions between DE and dark matter (DM), have also been proposed and investigated to alleviate the coincidence problem (Amendola 2000; Zimdahl et al. 2001; Chimento et al. 2003; Guo & Zhang 2005; Guo et al. 2005; Wei & Zhang 2007a, 2007b; Cai & Su 2010; Li et al. 2014; Gonzalez et al. 2019). Many studies suggest that interactions between DE and DM can lead to an increased value of  $H_0$ , potentially alleviating the tension between measurements from the Planck collaboration (within the  $\Lambda$ CDM paradigm) and the SH0ES collaboration (Kumar & Nunes 2016; Arevalo et al. 2017; Di Valentino et al. 2017; Kumar & Nunes 2017; Gonzalez et al. 2018; Yang et al. 2018; Kumar et al. 2019; Pan et al. 2019, 2020; von Marttens et al. 2019; Yang et al. 2020). Recently, Cheng et al. (2021) investigated the possible interaction between DE and weakly interacting massive particle DM using observational data in cosmology. Wang (2022) found that the combined data from Pantheon+, CMB, baryon acoustic oscillations (BAOs), and the observational Hubble data (OHD) suggest energy transfer from DE to DM at  $1.85\sigma$  confidence level; Zhao et al. (2023) used the mock Fast radio bursts to constrain the dimensionless coupling parameter in four phenomenological IDE models; Hou et al. (2023) constrained four phenomenological IDE models using the joint observation of gravitational wave (GW) and gamma-ray bursts (GRBs); Li & Zhang (2023) developed a full numerical routine to solve the background and perturbation equations of the IDE models. Li et al. (2024) simulated GW data of four detection strategies to perform cosmological analysis in four phenomenological IDE models. Halder et al. (2024) considered interaction scenarios that depend on the intrinsic nature of DE and DM, extending the unidirectional energy flow assumption to allow for bidirectional energy flow with sign shifting

interaction functions.

The IDE models can be explored phenomenologically by considering the ratio of the energy densities of dark energy to matter as  $r \equiv \rho_X \propto \rho_m a^\xi$ , where the variable  $\xi$  measures the

severity of the coincidence problem (Dalal et al. 2001). The interaction term can be obtained by  $Q = -H\rho_m(\xi + 3w_X)$  in a flat FLRW universe, where  $w_X$  represents the equation of state for DE. The condition  $\xi + 3w_X \neq 0$  denotes the interacting scenario. Chen et al. (2010) constrained the phenomenological model utilizing SNe Ia, CMB, and BAO; Cao et al. (2011) investigated observational constraints for this phenomenological interacting scenario by integrating OHD with the joint data. More recently, Zheng et al. (2022) found that the simulated GW can decrease the uncertainty associated with  $H_0$  from the joint sample in the frameworks of two typical dynamical models: the  $w_0w_a$ CDM model and this phenomenological model.

Another possible difficulty for the  $\Lambda$ CDM model is related to the age problem. This issue arises from observations of certain astrophysical objects: the quasar APM 08279+5255 at  $z = 3.91$  with a rough estimate of  $t_{\text{QSO}} = 2.0 \sim 3.0$  Gyr (Hasinger et al. 2002), and  $1\sigma$  lower age limit 1.8 Gyr (Friaça et al. 2005), which appear to be older than the universe itself according to the  $\Lambda$ CDM model. The cosmic age problem relative to the quasar APM 08279+5255 has been investigated in various studies (Sethi et al. 2005; Wei & Zhang 2007c; Cui & Zhang 2010; Yang & Zhang 2010; Chimento et al. 2013; Yu & Wang 2014; Yan et al. 2015).

The cosmic age problem of quasar APM 08279+5255 can also be investigated in interacting scenarios. Wang & Zhang (2008) showed that introducing dark energy alone does not solve the cosmic age problem when considering the quasar APM 08279+5255, suggesting that the potential interaction between dark energy and dark matter could offer a solution. Wang et al. (2010) found that 5 globular clusters and the quasar exhibit an age discrepancy with the  $\Lambda$ CDM model at a confidence level exceeding  $2\sigma$ , even when considering observational constraints from SNe Ia, BAO, CMB, and  $H_0$  measurements; considering IDE models can extend the cosmic age, however, IDE models still struggle to fully resolve the age problem. More recently, Zarandi & Ebrahimi (2022) discussed the cosmic age problem within the ghost dark energy model in the presence of three types of the sign-changeable interaction terms.

Observational data sets have played a crucial role in constraining cosmology. SNe Ia data span only up to a redshift of approximately  $z \sim 2$ , while CMB data pertain to redshifts near  $z \sim 1100$ . Therefore, cosmological data in the intermediate region could potentially provide vital understandings of the origins of the coincidence problem,  $H_0$  tension, and the cosmic age problem. GRBs are known to reach a higher maximum observable redshift, approximately  $z \sim 10$  (Cucchiara et al. 2011). Due to the scarcity of samples at low redshift, a fiducial cosmological model was necessary to presuppose for the calibration of

the GRBs luminosity relation in the early research (Dai et al. 2004; Schaefer 2007). Liang et al. (2008) introduced a cosmological model-independent method for calibrating the luminosity relations of GRBs by utilizing data from SNe Ia. On the other hand, the simultaneous method (Amati et al. 2008) has been also put forward to avoid the circularity problem by fitting the parameters of the correlation and cosmological models simultaneously. Amati et al. (2019) proposed an alternative approach for calibrating the GRB relation using OHD by the cosmic chronometers (CC) method. Therefore, GRBs data can be employed to place constraints on cosmological models without the circularity problem<sup>1</sup> (Wei 2010a, 2010b; Liang et al. 2010, 2011; Wang et al. 2016; Dainotti & Del Vecchio 2017; Demianski et al. 2017a, 2017b; Dainotti & Amati 2018; Dirirsa et al. 2019; Luongo & Muccino 2020, 2021a, 2021b; Montiel et al. 2021; Liu et al. 2022; Dainotti et al. 2023). It should be noted that the classification of GRBs is important for the calibration of GRB relations. If GRBs can be treated as standard candles, only a small fraction of GRBs can be suitable for cosmological use. See e.g., Wang et al. (2022) and Hu et al. (2021) for recent progress focused on specific GRB types to improve their standardization and enhance their utility in cosmology.

More recently, Khadka et al. (2021) made a compilation of a data set comprising 118 GRBs with the smallest intrinsic dispersion from a broader set of 220 GRBs. Liang et al. (2022) and Li et al. (2023) calibrated these GRB data using a Gaussian Process, from the Pantheon sample (Scolnic et al. 2018) or the most recent OHD by the CC method (Moresco et al. 2022). Wang et al. (2024) investigate the phenomenologically emergent dark energy model with GRBs and OHD at intermediate redshift. In this paper, our goal is to test the phenomenological interacting scenario<sup>2</sup> from cosmology-independent GRBs at redshifts ranging from 1.4 to 8.2 (Li et al. 2023) and the Pantheon+ sample, which is the most recent compilation of SNe Ia including 1701 light curves from 1550 unique data at redshifts ranging from 0.001 to 2.26 (Scolnic et al. 2022). To further explore the cosmic age problem, we incorporate the quasar APM 08279+5255 at redshift  $z = 3.91$  as an extra data point. The rest of the paper is organized as follows: Section 2 provides an overview of the phenomenological IDE model. The observational data adopted in this study are described in Section 3. Constraints from the observational data are given in Section 4. We give a brief conclusion in Section 5.

## 2. Overview of the Phenomenological Interacting Model

In this paper, we explore the possibility of DE and matter engage in an energy exchange through an interaction term

denoted as  $Q$

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<sup>1</sup>For a comprehensive review of the circularity problem in GRB cosmology, see Wang et al. (2015).

<sup>2</sup>In this work, we use  $\xi$ IDE to represent this phenomenological interaction model.

$$\begin{aligned}\dot{\rho}_X + 3H\rho_X(1 + w_X) &= -Q, \\ \dot{\rho}_m + 3H\rho_m &= Q.\end{aligned}\quad (1)$$

The phenomenological model adopts an assumption that the ratio of the dark energy to matter densities is (Dalal et al. 2001)

$$\rho_X \propto \rho_m a^\xi, \quad (2)$$

values of  $\xi = 3$  and  $\xi = 0$  are associated with the  $\Lambda$ CDM model and a self-similar solution that is free from the coincidence problem, respectively; while  $0 < \xi \leq 3$  indicates a less severe coincidence problem (Pavon et al. 2004). Considering the phenomenological model in a flat FLRW universe with  $\Omega_{X0} + \Omega_{m0} = 1$ , we can derive the interaction term,

$$Q = -H\rho_m(\xi + 3w_X)\Omega_X, \quad (3)$$

where  $\Omega_X = \frac{1 - \Omega_{m0}}{(1 - \Omega_{m0}) + \Omega_{m0}(1 + z)^\xi}$ , the case  $\xi + 3w_X = 0$  (which implies  $Q = 0$ ) corresponds to the standard cosmology without any interaction between dark energy and matter. Conversely,  $\xi + 3w_X \neq 0$  indicates the non-standard cosmology. Furthermore, when  $\xi + 3w_X > 0$  ( $Q < 0$ ), it suggests that energy is transferred from matter to DE, which tends to exacerbate the coincidence problem. Oppositely, if  $\xi + 3w_X < 0$  ( $Q > 0$ ), it indicates that the energy is transferred from DE to DM, which could potentially mitigate the coincidence problem. The  $H(z)$  function of the phenomenological model can be expressed as (Cao et al. 2011)

$$H(z) = H_0 \sqrt{(1+z)^3 [\Omega_{m0} + (1 - \Omega_{m0})(1+z)^{-\xi}]^{-3w/\xi}}. \quad (4)$$

For comparison, we also utilize the Chevallier-Polarski-Linder (CPL) model (Chevallier & Polarski 2001; Linder 2003), where dark energy is represented as evolving with redshift through the parameterization  $w = w_0 + w_a z/(1+z)$ . The  $\Lambda$ CDM model corresponds to  $w_0 = -1$ ,  $w_a = 0$ . The  $H(z)$  function of them can be expressed as

$$H(z) = H_0 \sqrt{\Omega_{m0}(1+z)^3 + (1 - \Omega_{m0})(1+z)^{3(1+w_0+w_a)} e^{-\frac{3w_a z}{1+z}}}. \quad (5)$$

To evaluate the efficacy of various models when applied to diverse data set combinations, we proceed to quantify the variances in the Akaike information criterion (AIC; Akaike 1974, 1981) and the Bayesian information criterion (BIC; Schwarz 1978), as defined by the following equations

$$\text{AIC} = 2p - 2 \ln(\mathcal{L}_{\max}), \quad (6)$$

$$\text{BIC} = p \ln N - 2 \ln(\mathcal{L}_{\max}). \quad (7)$$

where  $p$  is the number of parameters in the model,  $N$  is the sample size of the observational data combination, and  $\mathcal{L}_{\max}$  is the maximum likelihood of the model. The values of  $\Delta\text{AIC}$  and  $\Delta\text{BIC}$  for each model are given by  $\text{AIC} = \chi_{\min}^2 + 2\Delta n$ , and  $\text{BIC} = \chi_{\min}^2 + \Delta n \ln N$ . They represent the differences in AIC and BIC, respectively, when compared to the values obtained for the  $\Lambda\text{CDM}$  model.

### 3. Observational Data

The recent observations of GRB sample (Khadka et al. 2021) and the latest SNe Ia sample (Scolnic et al. 2022) are utilized in our cosmological analysis. For the GRBs sample, we follow the cosmology-independent approach in Li et al. (2023) to calibrate the Amati relation using the A118 GRB sample<sup>3</sup> using the 32 updated OHD measurements. We utilize GRB data at  $z > 1.4$  to constrain on cosmological models, the  $\chi_{\text{GRB}}^2$  function is defined as:

$$\chi_{\text{GRB}}^2 = \sum_{i=1}^N \left[ \frac{\mu_{\text{obs}}(z_i) - \mu_{\text{th}}(z_i; p, H_0)}{\sigma_{\mu_i}} \right]^2, \quad (8)$$

where  $N = 98$ ,  $\mu_{\text{th}}(z_i; p, H_0)$  represents the theoretical distance modulus of the model at redshifts  $z_i$ ,  $H_0$  is the Hubble constant,  $p$  denotes the cosmological parameter space,  $\mu_{\text{obs}}(z_i)$  and  $\sigma_{\mu_i}$  correspond to the observed value and the error, respectively.

The SNe Ia sample used in this study is the Pantheon+ sample, which comprises 1701 SNe Ia light curves observed from 1550 distinct SNe, spanning a redshift range of 0.001-2.26 (Brout et al. 2022; Scolnic et al. 2022). This data set includes major contributions from various sources, including CfA1 (Riess et al. 1999), CSP DR3 (Krisciunas et al. 2017), DES (Brout et al. 2019), PS1 (Scolnic et al. 2018), SDSS (Sako et al. 2018) and SNLS (Betoule et al. 2014). The optimal values for the cosmological parameters are derived by minimizing  $\chi_{\text{SNe}}^2$

$$\chi_{\text{SNe}}^2 = \Delta\mu C_{\text{stat}+\text{syst}}^{-1} \Delta\mu^T, \quad (9)$$

where  $\Delta\mu$  denotes the discrepancy between the observed distance modulus  $\mu_{\text{obs}}$  and its theoretical distance modulus  $\mu_{\text{th}}$ :

<sup>3</sup>We use the A118 GRB sample from the A220 GRB sample used in Khadka et al. (2021) with the higher qualities appropriate to investigate cosmology.

$$\Delta\mu = \mu_{\text{obs}}(z_i) - \mu_{\text{th}}(z_i; p, H_0). \quad (10)$$

The corresponding expression for  $\mu_{\text{th}}$  can be given by:

$$\mu_{\text{th}}(z_i; p, H_0) = m - M = 5 \log_{10} \frac{d_L(z_i; p, H_0)}{\text{Mpc}} + 25, \quad (11)$$

here,  $z_i$  indicates the peculiar-velocity-corrected CMB-frame redshift of each SNe Ia (Carr et al. 2022),  $p$  represents the cosmological parameters,  $m$  denotes the apparent magnitude of the source,  $M$  is the absolute magnitude, and  $d_L$  is the luminosity distance, defined as

$$d_L = \frac{c(1+z)}{H_0} \int_0^z \frac{dz'}{H(z')}, \quad (12)$$

**Figure 1.** Constraints on the cosmological parameters of the  $\Lambda$ CDM model (left), the CPL model (middle), and the  $\xi$ IDE model (right) with GRBs alone.

**Table 1**

Constraints on Cosmological Parameters  $\Omega_m$ ,  $h$ ,  $w_X$ ,  $\xi$ ,  $w_0$  and  $w_a$  for the  $\Lambda$ CDM Model, the CPL Model, and the  $\xi$ IDE Model Using GRBs ( $z > 1.4$ ), SNe Ia, and GRBs+SNe Ia

Parameter	$\Omega_m$	$h$	$w_X$	$\xi$	$w_0$	$w_a$	$-2 \ln \mathcal{L}_{\text{infix}}$	$\Delta\text{AIC}$	$\Delta\text{BIC}$
<b>GRBs</b>									
$\Lambda$ CDM	$0.369^{+0.070}_{-0.100}$	0.7	...	...	...	...	43.145	...	...
CPL	$0.33^{+0.17}_{-0.12}$	0.7	...	...	$-0.87^{+0.84}_{-0.40}$	$0.99 \pm 0.56$	43.212	4.067	9.238
$\xi$ IDE	$0.45^{+0.28}_{-0.20}$	0.7	$-1.56^{+1.40}_{-0.31}$	$0.2^{+2.1}_{-3.8}$	...	...	43.383	4.238	9.409
<b>SNe Ia</b>									
$\Lambda$ CDM	$0.358 \pm 0.013$	$0.7288 \pm 0.0019$	...	...	...	...	1821.892	...	...
CPL	$0.338^{+0.072}_{-0.043}$	$0.7259 \pm 0.0024$	...	...	$-0.849^{+0.129}_{-0.098}$	$0.87^{+0.85}_{-0.52}$	20.629	2.737	13.615
$\xi$ IDE	$0.42 \pm 0.23$	$0.7266 \pm 0.0023$	$-1.27^{+0.53}_{-0.34}$	$0.2^{+0.43}_{-1.40}$	...	...	1995.103	177.211	188.089
<b>GRBs+SNe Ia</b>									
$\Lambda$ CDM	$0.357 \pm 0.013$	$0.7289 \pm 0.0019$	...	...	...	...	1865.338	...	...
CPL	$0.326^{+0.071}_{-0.046}$	$0.7258 \pm 0.0024$	...	...	$-0.831^{+0.119}_{-0.091}$	$0.79^{+0.78}_{-0.56}$	1863.671	2.333	12.343

Parameter	$\Omega_m$	$h$	$w_X$	$\xi$	$w_0$	$w_a$	$-2 \ln \mathcal{L}_{\text{infix}} \Delta \text{AIC}$	$\Delta \text{BIC}$
$\xi \text{IDE}$	$0.525^{+0.289}_{-0.099}$	$0.7266 \pm 0.0022$	$-1.55^{+1.00}_{-0.57}$	$0.78^{+0.31}_{-1.10}$	...	...	2035.557243.557	254.501

where  $c$  represents the speed of light. The complete covariance matrix for Pantheon+ sample is given by Brout et al. (2022):

$$C_{\text{stat+syst}} = C_{\text{stat}} + C_{\text{syst}}, \quad (13)$$

where  $C_{\text{stat}}$  and  $C_{\text{syst}}$  refer to the statistical and systematic covariance matrices, respectively. The data sets and  $C_{\text{stat+syst}}$  can be obtained online.<sup>4</sup> The total  $\chi^2_{\text{total}}$  for the combined GRBs and SNe Ia data is given by  $\chi^2_{\text{total}} = \chi^2_{\text{GRB}} + \chi^2_{\text{SNe}}$ . The MCMC method, facilitated by the Python package emcee (Foreman-Mackey et al. 2013), is employed for the minimization of the chi-square function  $\chi^2$ .

#### 4. Constraints On Cosmological Models

Since GRB data alone cannot constrain  $H_0$  due to the degeneracy with the correlation intercept parameter, we follow previous works (Khadka et al. 2021; Liang et al. 2022) and fix  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$  for the case of GRBs alone. The results are presented in Figure 1 and summarized in Table 1. For the CPL model, the constraint on the parameter  $w_a$  using GRBs alone indicates a possible DE evolution ( $w_a \neq 0$ ) within the  $1\sigma$  confidence region. For the  $\xi \text{IDE}$  model, the constraint results for  $w_X$  and  $\xi$  suggest:  $\xi + 3w_X < 0$  with GRBs alone. This finding is consistent with recent work (Zheng et al. 2022); however, this result is different from previous studies, which

**Figure 2.** Constraints on the cosmological parameters of the  $\Lambda \text{CDM}$  model (left), the CPL model (middle), and the  $\xi \text{IDE}$  model (right), with SNe Ia and GRBs + SNe Ia.

found  $\xi + 3w_X > 0$  to be slightly preferred (Guo et al. 2007; Chen et al. 2010; Cao et al. 2011). We find that our results for the  $\Lambda \text{CDM}$  model, the  $w \text{CDM}$  model, and the CPL model using GRBs alone are compatible with the previous work of Li et al. (2023).

We also consider the joint constraints using GRBs and the Pantheon+ sample. The best-fit values, with the  $1\sigma$  confidence level for the parameters obtained from SNe Ia and GRBs + SNe Ia, are shown in Figure 2 and summarized in Table 1. We find that GRBs + SNe Ia provide stronger constraints on the parameters ( $\Omega_m, h, w_X$  and  $\xi$ ) within the frameworks of the  $\Lambda \text{CDM}$ , CPL, and  $\xi \text{IDE}$  models, while GRBs alone give weak constraints on all parameters. We find that  $\xi + 3w_X < 0$  with SNe Ia and GRBs + SNe Ia for the  $\xi \text{IDE}$  model, which is consistent with the GRBs-only case. For the value of the Hubble constant, our result

<sup>4</sup><https://github.com/PantheonPlusSH0ES/DataRelease>

with GRBs + SNe Ia for the  $\xi$ IDE model agrees with that reported by SHOES (Riess et al. 2022a), ( $H_0 = 73.01 \pm 0.99 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), at  $0.35\sigma$ . Additionally, our result is in agreement with those obtained by Hu et al. (2024), ( $H_0 = 72.83 \pm 0.23 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), and Wang (2022), ( $H_0 = 73.5^{+8.1}_{-10.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), with the  $1\sigma$  error of  $h$  reduced. For the  $\Lambda$ CDM model with SNe Ia, our result is consistent with Brout et al. (2022), ( $H_0 = 73.6 \pm 1.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), and Dahiya & Jain (2023), ( $H_0 = 73.500^{+1.013}_{-0.978} \text{ km s}^{-1} \text{ Mpc}^{-1}$ ), except for a reduced  $1\sigma$  error for  $H_0$ . This is mainly due to the application of the standardized distance modulus ( $\mu_{\text{obs}} = m - M$ ; Tripp 1998), with  $M$  being calculated from the Cepheid host-galaxy distances determined by SHOES (Riess et al. 2022b).

For the CPL model, constraints on the parameter  $w_a$  derived from SNe Ia and GRBs + SNe Ia suggest a possible DE evolution ( $w_a \neq 0$ ) within the  $1\sigma$  confidence region, which is consistent with the results obtained using GRBs alone. However, the statistical measures in Table 1 reveal that the  $\xi$ IDE model exhibits much higher  $\Delta\text{AIC}$  and  $\Delta\text{BIC}$  values when compared to the  $\Lambda$ CDM and CPL models, indicating that the  $\Lambda$ CDM model is still favored.

The age estimation of old objects at high redshifts is crucial for constraining cosmological parameters (Alcaniz & Lima 1999; Lima & Alcaniz 2000). The quasar APM 08279+5255 at redshift  $z = 3.91$  is particularly important in this regard. Its age has been estimated through chemical-evolution studies. Utilizing the Fe/O ratio derived from X-ray observations, Hasinger et al. (2002) provided a rough estimate of  $t_{\text{QSO}} = 2.0 \sim 3.0 \text{ Gyr}$ . Subsequently, Friaça et al. (2005) used a detailed chemodynamical model to obtain  $t_{\text{QSO}} = 2.1 \pm 0.3 \text{ Gyr}$  at this redshift. The age of a flat universe at redshift  $z$  can be calculated by Alcaniz et al. (2003), Jain & Dev (2006):

$$t(z) = \int_z^\infty \frac{dz'}{(1+z')H(z')}. \quad (14)$$

However, the  $\Lambda$ CDM model predicts a cosmic age of 1.63 Gyr at  $z = 3.91$  according to the 7 yr WMAP data (Komatsu et al. 2011) ( $\Omega_m = 0.272$ ,  $h = 0.704$ ), while the quasar's  $1\sigma$  lower age limit is 1.8 Gyr.

In this work, we use the estimated lower-limit ages of the quasar at  $z = 3.91$ , with  $1\sigma$  (1.8 Gyr) and  $2\sigma$  (1.5 Gyr), to examine the age problem in both the  $\Lambda$ CDM model and the  $\xi$ IDE model within the parameter space ( $\Omega_m - h$  plane) using GRBs + SNe Ia data, as shown in Figure 3. Our calculations indicate that the presence of the quasar APM 08279+5255 is incompatible with the  $\Lambda$ CDM model, which is consistent with the earlier results of Wang & Zhang (2008), Yang & Zhang (2010), and Wang et al. (2010). It can be found that the cosmic age predicted by the  $\Lambda$ CDM model with the best-fit values at  $z = 3.91$  (1.38 Gyr) deviates by  $2.4\sigma$  from the age of the quasar APM 08279+5255 (2.1 Gyr); however, the one predicted by the  $\xi$ IDE model with the best-fit values at  $z = 3.91$  (1.83 Gyr), which can be

**Figure 3.** The contours correspond to  $1\sigma$  and  $2\sigma$  confidence regions in the  $\Omega_m$ - $h$  plane with GRBs+SNe Ia for the  $\Lambda$ CDM model (left panel) and the  $\xi$ IDE model (right panel), respectively. The blue, green, and purple curves correspond to the cosmological parameters that would result in a universe age of 2.1 Gyr (the best-fit), 1.8 Gyr (the  $1\sigma$  limit), and 1.5 Gyr (the  $2\sigma$  limit) at  $z = 3.91$ , respectively. The central red dot denotes the best-fit point with GRBs+SNe Ia for the  $\Lambda$ CDM and  $\xi$ IDE models, respectively.

accommodated the quasar APM 08279+5255 at  $0.9\sigma$  confidence level. Our calculations show that the  $\xi$ IDE model can predict significantly higher cosmic ages compared to the  $\Lambda$ CDM model, thereby substantially alleviating the cosmic age problem.

## 5. Conclusion

In this study, we test the phenomenological interacting scenario (the  $\xi$ IDE model) with the A118 GRB sample calibrated from the updated OHD measurements in a cosmology-independent approach, Pantheon+ SNe Ia sample, and the age lower limit of quasar APM 08279+5255 at high- $z$ . In the scenario of the  $\xi$ IDE model, constraints of  $\xi$  and  $w_X$  derived from GRBs-only, SNe Ia-only, and GRBs+SNe Ia support  $\xi + 3w_X < 0$ , indicating that energy is transferred from dark energy to dark matter, which is consistent with previous results from Zheng et al. (2022); thus the coincidence problem is alleviated. The best-fit values of  $H_0$  obtained in the  $\xi$ IDE model deviate by  $0.35\sigma$  from SH0ES measurements (Riess et al. 2022a) using SNe Ia-only and GRBs+SNe Ia. Considering the age estimate for the quasar APM 08279+5255, our results show that the  $\xi$ IDE model can accommodate this quasar, predicting significantly higher cosmic ages in comparison to the  $\Lambda$ CDM model and thereby substantially alleviating the cosmic age problem.

The  $\Lambda$ CDM model aligns well with most astronomical observations; however, some recent observations display slight deviations from  $\Lambda$ CDM model (Perivolaropoulos & Skara 2022; Hu & Wang 2023; Carloni et al. 2024; Colgáin et al. 2024a, 2024b, 2024c; Luongo & Muccino 2024). Our analysis also indicates that the constraints for the CPL model with various data sets support the possibility of dark energy evolution ( $w_a \neq 0$ ) within the  $1\sigma$  confidence region; whereas the  $\Lambda$ CDM model remains favored when comparing  $\Delta$ AIC and  $\Delta$ BIC values.

Future work should focus on refining IDE models and exploring their implications with more precise observational data, such as the recent GRBs from Fermi data (Wang & Liang 2024) and BAOs from Dark Energy Spectroscopy Instrument (DESI) data release 1 (DESI Collaboration et al. 2024).

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