

## The Energy Sources and the Explosion Mechanism of Ca-rich Supernova PTF 10iuv (Postprint)

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### Abstract

In this paper, we perform the detailed modeling for the light curves (LCs) of PTF 10iuv which is a calcium-rich (Ca-rich) supernova (SN) to constrain the physical properties of its ejecta and the energy sources, as well as the explosion mechanism. We find that the  $^{56}\text{Ni}$  model and the  $^{56}\text{Ni}$  plus circumstellar interaction model fail to explain the LCs, while the four-element ( $^{56}\text{Ni}$ ,  $^{48}\text{Cr}$ ,  $^{52}\text{Fe}$ , and  $^{44}\text{Ti}$ ) model can account for the LCs. The ejecta mass of PTF 10iuv derived by the model ( $1.52-0.25+0.34M_{\odot}$ ) is consistent with that of the merger of a sub-Chandrasekhar mass white dwarf. The early-time LCs were mainly powered by  $^{56}\text{Ni}$  whose mass is  $0.03 M_{\odot}$ , while the contributions of  $^{48}\text{Cr}$  and  $^{52}\text{Fe}$  can be neglected. The derived  $^{44}\text{Ti}$  mass ( $0.25 M_{\odot}$ ) is 1.8 times the upper limit of the derived  $^{44}\text{Ti}$  mass of Ca-rich SN 2005E. We suggest that subtracting the contributions of the host-galaxy, which are unknown, and including the flux from other long-lived elements (e.g.,  $^{57}\text{Co}$ ,  $^{55}\text{Fe}$ ,  $^{60}\text{Co}$ ) can reduce the amount of  $^{44}\text{Ti}$ , and that this value can be regarded as an upper limit.

### Full Text

### Preamble

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### The Energy Sources and the Explosion Mechanism of Ca-rich Supernova PTF 10iuv

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## Abstract

In this paper, we perform detailed modeling of the light curves (LCs) of PTF 10iuv, a calcium-rich (Ca-rich) supernova (SN), to constrain the physical properties of its ejecta, the energy sources, and the explosion mechanism. We find that the  $^{56}\text{Ni}$  model and the  $^{56}\text{Ni}$  plus circumstellar interaction model fail to explain the LCs, while a four-element ( $^{56}\text{Ni}$ ,  $^{48}\text{Cr}$ ,  $^{52}\text{Fe}$ , and  $^{44}\text{Ti}$ ) model can successfully account for them. The ejecta mass of PTF 10iuv derived from the model ( $1.52 \pm 0.25 M_{\odot}$ ) is consistent with that expected from the merger of a sub-Chandrasekhar mass white dwarf. The early-time LCs were mainly powered by  $^{56}\text{Ni}$  with a mass of  $0.03 M_{\odot}$ , while the contributions of  $^{48}\text{Cr}$  and  $^{52}\text{Fe}$  can be neglected. The derived  $^{44}\text{Ti}$  mass ( $0.25 M_{\odot}$ ) is 1.8 times the upper limit of the  $^{44}\text{Ti}$  mass derived for Ca-rich SN 2005E. We suggest that subtracting the unknown contributions from the host galaxy and including flux from other long-lived elements (e.g.,  $^{57}\text{Co}$ ,  $^{55}\text{Fe}$ ,  $^{60}\text{Co}$ ) can reduce the required amount of  $^{44}\text{Ti}$ , and that this value should be regarded as an upper limit.

**Key words:** (stars:) supernovae: general – (stars:) supernovae: individual (PTF 10iuv) – (stars:) novae – cataclysmic variables

## 1. Introduction

Supernovae (SNe) are explosions of white dwarfs (WDs) in binary systems or aged massive stars. According to their spectra at photospheric phases, most SNe can be divided into types: Ia, Ib, Ic, Iib, and II (Filippenko 1997; a more detailed classification scheme can be found in Gal-Yam 2017). It is widely believed that type Ia SNe result from the explosions of WDs, while most other sub-types originate from the explosions of massive stars.

Over the past two decades, several dozen new optical transients classified as calcium-rich (Ca-rich) SNe or transients have been confirmed (e.g., Filippenko et al. 2003; Kawabata et al. 2010; Perets et al. 2010; Sullivan et al. 2011; Kasliwal et al. 2012; Valenti et al. 2014; Lunnan et al. 2017; De et al. 2018, 2020; Lee et al. 2019; Jacobson-Galán et al. 2020b). Although the spectra of most confirmed Ca-rich SNe at photospheric phases can also be classified as types Ia (SN 2016hnk, SN 2019ofm; Jacobson-Galán et al. 2020a; De et al. 2020), Ib (e.g., SN 2005E, SN 2005cz, SN 2007ke, PTF 10iuv, PTF 11kmb; Puckett & Dowdle 2000; Aazami & Li 2001; Filippenko et al. 2003; Puckett et al. 2003;

Pugh & Li 2003; Dimai et al. 2005; Graham et al. 2005; Chu et al. 2007; Perets et al. 2010; Kasliwal et al. 2012; Foley 2015; Lunnan et al. 2017; De et al. 2018, 2020; Jacobson-Galán et al. 2020a, 2020b; Ertini et al. 2023), Ic (SN 2012hn, SN 2018gwo, SN 2022oqm; Valenti et al. 2014; De et al. 2020; Irani et al. 2024), and Iib (iPTF15eqv, SN 2018jak, SN 2019ehk, SN 2020sbw, SN 2021M, SN 2021pb, SN 2021sjt; Cao et al. 2015; De et al. 2021; Das et al. 2023), their late-phase nebular spectra show prominent calcium (Ca) and weak oxygen (O) lines, which are distinct from those of normal SNe Ia, Ib, Ic, and Iib (see Taubenberger 2017). Additionally, there are several Ca-rich SNe whose spectral types are unknown (PTF 09dav, PTF 11bij, PTF 12bho, SN 2019bkc, SN 2019pof; Sullivan et al. 2011; Chen et al. 2020; Prentice et al. 2020).

The explosion sites of Ca-rich SNe also differ from those of normal SNe Ib and Ic. In contrast to SNe Ib and Ic, which are found in star-forming regions, almost all Ca-rich SNe occur in old environments far from the center of their (potential) host galaxies (see Taubenberger 2017 and references therein). Furthermore, most Ca-rich SNe have fast-evolving light curves (LCs), indicating that their ejecta masses ( $M$ ) are rather small, comparable to those of some ultra-stripped-envelope SNe Ic (e.g., SN 2005ek; Drout et al. 2013). Perets et al. (2010) found that the ejecta mass of SN 2005E is  $0.3 \pm 0.1 M_{\odot}$  and suggested that the ejecta originated from the ejected helium shell surrounding a WD. To our knowledge, all confirmed Ca-rich SNe are low-luminosity cases with peak absolute magnitudes between  $-14$  and  $-17.5$  mag. Assuming that the LCs of Ca-rich SNe are powered by the cascade decay of radioactive elements, these low peak luminosities imply that the total masses of synthesized radioactive elements are significantly lower than those produced by normal SNe Ib and Ic.

The features of Ca-rich SNe challenge standard SN explosion scenarios. For instance, while the progenitors of normal SNe Ib and Ic are believed to be massive stars, the progenitors of Ca-rich SNe Ib are suggested to be WDs in binary systems (Perets et al. 2010; Lyman et al. 2014; Foley 2015; Lunnan et al. 2017; Zenati et al. 2023). Furthermore, numerical simulations (Bildsten et al. 2007; Shen & Bildsten 2009; Shen et al. 2010; Waldman et al. 2011; Woosley & Kasen 2011) suggest that explosions of sub-Chandrasekhar mass WDs can reproduce some features (low peak luminosities, low ejecta masses, high abundance of Ca, etc.) of Ca-rich SNe Ib.

Although the explosion mechanisms and progenitor systems of Ca-rich SNe remain elusive, it is possible to constrain their physical parameters and infer their energy sources. Some groups (e.g., Kasliwal et al. 2012; De et al. 2018, 2020) have used the  $^{56}\text{Ni}$  cascade decay ( $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$ ) model to estimate  $M$ ,  $^{56}\text{Ni}$  masses ( $M_{\text{Ni}}$ ), and other explosion parameters. However, the assumption that the LCs of Ca-rich SNe were solely powered by  $^{56}\text{Ni}$  cascade decay is not always valid. Studies of the nucleosynthesis of SN 2005E (Perets et al. 2010) and explosions of sub-Chandrasekhar mass WDs (Bildsten et al. 2007; Shen & Bildsten 2009; Shen et al. 2010; Waldman et al. 2011; Woosley & Kasen 2011) show that other short-lived radioactive elements (e.g.,  $^{52}\text{Fe}$ ,  $^{48}\text{Cr}$ ) and

long-lived radioactive elements (e.g.,  $^{44}\text{Ti}$ ) should also be produced by Ca-rich SNe. Jacobson-Galán et al. (2021) used a radioactive model including contributions from  $^{56}\text{Co}$  and  $^{57}\text{Co}$  (from the decay of  $^{56}\text{Ni}$  and  $^{57}\text{Ni}$ ) to fit the late-time bolometric LC of Ca-rich SN 2019ehk, obtaining the  $^{56}\text{Co}$  mass and constraining the upper limit of the  $^{57}\text{Co}$  mass. In several numerical models, the  $^{56}\text{Ni}$  masses can be as low as  $10^{-7}$ – $10^{-4}$  M, which are significantly lower than the  $^{48}\text{Cr}$  masses in the same models (Waldman et al. 2011). In these models, the contribution from the cascade decay of  $^{48}\text{Cr}$  ( $^{48}\text{Cr} \rightarrow ^{48}\text{V} \rightarrow ^{48}\text{Ti}$ ) is significantly larger than that of  $^{56}\text{Ni}$  at early epochs (see, e.g., Figure 4 [Figure 4: see original paper] of Waldman et al. 2011). Additionally, the amount of  $^{44}\text{Ti}$  synthesized in explosions of sub-Chandrasekhar mass WDs can be up to  $10^{-1}$  M (Perets et al. 2010; Waldman et al. 2011; Zenati et al. 2023), 3–4 orders of magnitude larger than the mass of  $^{44}\text{Ti}$  ( $M_{\text{Ti}}$ ) from core-collapse SNe (CCSNe,  $1$ – $15 \times 10^{-5}$  M; The et al. 2006) and SNe Ia ( $0.87$ – $2.7 \times 10^{-5}$  M; Timmes et al. 1996). Although the contribution from the cascade decay of  $^{44}\text{Ti}$  ( $^{44}\text{Ti} \rightarrow ^{44}\text{Sc} \rightarrow ^{44}\text{Ca}$ ) can be neglected in early-time LCs of SNe, it can change the shapes of the LCs of some Ca-rich SNe as early as 100 days and dominate the late-time LCs (see, e.g., Figure 4 of Waldman et al. 2011).

In this paper, we perform a theoretical study of PTF 10iuv (=SN 2010et) (Kasliwal et al. 2012), one of the Ca-rich SNe observed over 200–300 days. PTF 10iuv was detected by the Palomar Transient Factory (PTF) at a redshift ( $z$ ) of 0.023 on 2010 May 31, when its r-band magnitude was 21.2 (see Kasliwal et al. 2012; Dessart & Hillier 2015; Moriya et al. 2017 and references therein). Follow-up photometric observations of PTF 10iuv were performed using Bgriz filters of the Palomar 60-inch telescope (P60), the Large Format Camera (LFC) on the Palomar 200-inch telescope (P200), and the Low Resolution Imaging Spectrometer (LRIS) on the Keck I telescope. The r-band LC peaked at 19.0 mag in 10 days and declined rapidly (1 magnitude within 12 days) (Kasliwal et al. 2012). One month later, PTF 10iuv evolved slowly at a rate of  $0.02 \text{ mag day}^{-1}$  for three months, followed by a decline rate of  $0.005 \text{ mag day}^{-1}$ .

The spectra of PTF 10iuv indicate that it is a Ca-rich SN Ib. The distance of PTF 10iuv from the nearest galaxy that might be its host galaxy is 37 kpc (Kasliwal et al. 2012). Kasliwal et al. (2012) used the input power function of the  $^{56}\text{Ni}$  cascaded decay to fit the r-band LC of PTF 10iuv, finding that the flux of late-time data is brighter than that reproduced by  $^{56}\text{Ni}$  cascaded decay. They suggested that the late-time excesses relative to the  $^{56}\text{Ni}$  input luminosity might be due to host-galaxy contamination or contributions from other radioactive elements, e.g.,  $^{44}\text{Ti}$ . However, as pointed out by Kasliwal et al. (2012), the  $^{44}\text{Ti}$  mass required would be 2 M if the late-time flux were powered solely by  $^{44}\text{Ti}$  decay.

Kasliwal et al. (2012) suggested that modeling the LCs of PTF 10iuv could better constrain models including contributions from  $^{48}\text{Cr}$ ,  $^{44}\text{Ti}$ , and  $^{52}\text{Fe}$ , since photometry in both the rising and late phases is available. However, detailed modeling has not been performed. This is the aim of our study.

In Section 2, we use the  $^{56}\text{Ni}$  model and other, more complicated models to fit the multi-band LCs of PTF 10iuv. In Section 3, we discuss the physical parameters and possible implications. In Section 4, we draw conclusions. Throughout this paper, we assume  $\Omega_m = 0.315$ ,  $\Omega_\Lambda = 0.685$ ,  $H_0 = 67.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (Planck Collaboration et al. 2014). The values of foreground Galactic reddening are from Schlafly & Finkbeiner (2011).

## 2. Modeling the Multi-band LCs of PTF 10iuv

In this section, we model the multi-band LCs of PTF 10iuv. In the photospheric phase, the bolometric luminosity of SNe is given by (see e.g., Arnett 1982; Chatzopoulos et al. 2012):

$$L(t) = e^{-t/\tau_d} \int_0^t L_{\text{input}}(t') e^{t'/\tau_d} dt'$$

where  $L_{\text{input}}(t)$  is the instantaneous power input,  $\tau_d$  is the diffusion timescale (Arnett 1982),  $\kappa$  is the optical opacity of the ejecta with values in the range of  $0.025\text{--}0.25 \text{ cm}^2 \text{ g}^{-1}$  (see, e.g., Mazzali et al. 2001),  $v_{\text{ph}}$  is the photospheric velocity of the SN,  $c$  is the speed of light, and  $M_{\text{ej}}$  is the ejecta mass. We assume that the early photosphere expansion velocity ( $v_{\text{ph}}$ ) of PTF 10iuv is a constant ( $10,000 \text{ km s}^{-1}$ ; Kasliwal et al. 2012). In the nebular phase, the bolometric luminosity of an SN is just the instantaneous power input, i.e.,  $L(t) = L_{\text{input}}(t)$ . We note that Arnett (1982) does not consider the  $\gamma$ -ray leakage effect, while all the input functions we use do account for this.

We assume that the photosphere evolution can be described by the blackbody model. As shown in Figure 1 [Figure 1: see original paper], the spectral energy distributions (SEDs) of PTF 10iuv at all epochs with photometry in at least three bands can be described by the blackbody model. This indicates that the blackbody assumption is valid at these epochs. Furthermore, we assume that the late-time temperature ( $T_f$ ) is a constant (the temperature floor; Nicholl et al. 2017).

### 2.1. The $^{56}\text{Ni}$ Model

We first use the  $^{56}\text{Ni}$  cascade decay model, which is widely adopted to model the LCs of normal SNe Ib and Ic, to fit the multi-band LCs of PTF 10iuv. The power input function ( $L_{\text{input}}(t)$ ) of  $^{56}\text{Ni}$  cascade decay is from Valenti et al. (2008). In the  $^{56}\text{Ni}$  model, the  $\gamma$  opacity ( $\kappa_\gamma$ ) and positron opacity ( $\kappa_{e^+}$ ) of the SN ejecta are set to be  $0.027$  and  $7 \text{ cm}^2 \text{ g}^{-1}$ , respectively (e.g., Cappellaro et al. 1997; Mazzali et al. 2000; Maeda et al. 2003).

The definitions, units, and prior ranges of the free parameters of the  $^{56}\text{Ni}$  model are listed in Table 1 (columns 1–4). To obtain the best-fitting values and  $1\sigma$  ranges of the parameters, we use the Markov Chain Monte Carlo (MCMC) method by executing the emcee Python package (Foreman-Mackey et al. 2013).

The fit of the  $^{56}\text{Ni}$  model is shown in Figure 2 [Figure 2: see original paper]; the corresponding corner plot is presented in the upper panel of Figure A1. The medians,  $1\sigma$  ranges, and best-fitting values of the parameters are listed in Table 1 (column 5). We find that the  $^{56}\text{Ni}$  model fails to fit the LCs of PTF 10iuv, since the flux of the long plateau (138.8–290.3 days after the first data point) in the r-band is higher than that produced by the  $^{56}\text{Ni}$  model.

Assuming that the flux of the last two data points is from the host galaxy and subtracting it from all r-band data (as in Kasliwal et al. 2012), we find that the  $^{56}\text{Ni}$  model can fit the r-band LC of PTF 10iuv well (see Figure 2 [Figure 2: see original paper]); the corresponding corner plot is presented in the lower panel of Figure A1; the medians,  $1\sigma$  ranges, and best-fitting values of parameters are listed in column 6 of Table 1). However, the derived  $M_{\text{ej}}$  is  $4.22^{+0.35}_{-0.73} \text{ M}$ ; though this is lower than the value ( $6.862^{+0.898}_{-0.350} \text{ M}$ ) derived by the same model for the multi-band LCs of PTF 10iuv, it is significantly larger than  $2.8 \text{ M}$ , which is twice the Chandrasekhar mass and can be regarded as the upper limit for any WD-WD binary system. This indicates that PTF 10iuv might be a CCSN from the explosion of a massive star.

However, almost all confirmed CCSNe are not found in elliptical galaxies. This, together with the fact that the distance between PTF 10iuv and its potential host galaxy (which is an elliptical galaxy) is very large (37 kpc), and that the spectra of PTF 10iuv are different from those of typical SNe Ib, disfavors the scenario that PTF 10iuv is a CCSN. A larger value of  $M_{\text{ej}}$  would reduce  $M_{\text{ej}}$ , but the larger leakage effect would result in a worse fit. This indicates that the assumption that the late-time flux was from the host galaxy cannot alleviate the problem of the  $^{56}\text{Ni}$  model for fitting the LCs of PTF 10iuv. To fit the LCs of PTF 10iuv, more complicated models must be constructed. We no longer consider the possibility of host-galaxy contamination below.

## 2.2. The Four-element Model

The second possibility for the late-time excesses of the LCs of PTF 10iuv is that they originated from the cascade decay of  $^{44}\text{Ti}$ , a long-lived radioactive element. In this scenario, the late-time LCs were mainly powered by  $^{44}\text{Ti}$  and  $^{56}\text{Ni}$ . As demonstrated by observations and numerical simulations, other radioactive elements (e.g.,  $^{52}\text{Fe}$ ,  $^{48}\text{Cr}$ ,  $^{44}\text{Ti}$ ) should also be produced by Ca-rich SNe, and their contributions might exceed that of  $^{56}\text{Ni}$  cascade decay at some epochs.

The numerical simulations of Waldman et al. (2011) include seven radioactive elements. To reduce the number of free parameters, we neglect contributions from three elements ( $^{57}\text{Ni}$ ,  $^{51}\text{Mn}$ , and  $^{49}\text{Cr}$ ), and generalize the  $^{56}\text{Ni}$  model to one including four elements ( $^{56}\text{Ni}$ ,  $^{52}\text{Fe}$ ,  $^{48}\text{Cr}$ , and  $^{44}\text{Ti}$ ). In this model, we expect that the early-time LCs are mainly powered by  $^{56}\text{Ni}$ ,  $^{48}\text{Cr}$ , and  $^{52}\text{Fe}$ , while the late-time LCs are mainly powered by  $^{44}\text{Ti}$ .

The power input function of the four-element model includes contributions from

$^{56}\text{Ni}$ ,  $^{52}\text{Fe}$ ,  $^{48}\text{Cr}$ , and  $^{44}\text{Ti}$ . The input function of  $^{44}\text{Ti}$  is from Equation (1) of Timmes et al. (1996); the value of  $\kappa_\gamma$  for  $^{44}\text{Ti}$  is fixed at  $0.04 \text{ cm}^2 \text{ g}^{-1}$  (Timmes et al. 1996; Seitenzahl et al. 2014). The input functions of  $^{52}\text{Fe}$  and  $^{48}\text{Cr}$  are from equation (16) of Seitenzahl et al. (2014), with  $\kappa_\gamma$  fixed at  $0.027 \text{ cm}^2 \text{ g}^{-1}$  (Waldman et al. 2011). The values of the half-life ( $t_{1/2}$ ), the total energy radiated in gamma-rays  $Q_\gamma$ , and the total energy liberated in the form of particles  $Q_{\text{th}}$  for  $^{52}\text{Fe}$ ,  $^{48}\text{Cr}$ , and  $^{44}\text{Ti}$  are from Tables 3 and 4 of Dessart et al. (2014). The lifetime ( $\tau$ ) of  $^{48}\text{Cr}$  and  $^{44}\text{Ti}$  can be calculated accordingly. The definitions, units, and prior ranges of the free parameters of the four-element model are listed in Table 2 (columns 1–4).

We find that the four-element model can fit the LCs of PTF 10iuv (see Figure 3 [Figure 3: see original paper]). The medians,  $1\sigma$  ranges, and best-fitting values of the parameters are listed in Table 2 (column 5); the corresponding corner plot is presented in Figure A2. The derived parameters of the four-element model are  $M_{\text{ej}} = 1.52_{-0.25}^{+0.25} \text{ M}$ ,  $M_{\text{Ni}} = 0.032_{-0.002}^{+0.002} \text{ M}$ ,  $M_{\text{Ti}} = 0.244_{-0.018}^{+0.018} \text{ M}$ ,  $M_{\text{Cr}} = 0.0004_{-0.0004}^{+0.045} \text{ M}$ ,  $M_{\text{Fe}} = 0.045_{-0.045}^{+0.001} \text{ M}$ ,  $\kappa = 0.086_{-0.013}^{+0.068} \text{ cm}^2 \text{ g}^{-1}$ ,  $T_{\text{floor}} = 3405.491_{-83.315}^{+3748.707} \text{ K}$ ,  $t_{\text{shift}} = -0.894_{-0.155}^{+1.617} \text{ days}$ . The value of  $\chi^2/\text{dof}$  is 1.831. Using the best-fitting parameters, we can reproduce the theoretical bolometric LC of PTF 10iuv and derive the rise time  $t_p$  (13.90 days) and the peak luminosity  $L_p$  ( $8.15 \times 10^{41} \text{ erg s}^{-1}$ ). The derived kinetic energy  $E_k$  ( $E_{\text{ej}}$ ) of PTF 10iuv is  $4.31 \times 10^{50} \text{ erg}$ .

### 2.3. The $^{56}\text{Ni}$ Plus CSI Model

Another promising scenario that can account for the late-time excesses in photometry involves interaction between the ejecta and the circumstellar medium (CSM). In this scenario, the SN ejecta collide with the CSM, producing forward and reverse shocks that convert a fraction of the kinetic energy of the ejecta to ultraviolet (UV)-optical-infrared (IR) radiation. The circumstellar interaction (CSI) provides additional energy sources for the SNe and increases their luminosity. The details of the CSI model can be found in Wang et al. (2019), which is based on Chevalier (1982), Chevalier & Fransson (1994), and Chatzopoulos et al. (2012). We assume that the photosphere expanded at early-time epochs. The density profile of the CSM can be described by  $\rho_{\text{CSM}} = qr^{-s}$ , where  $q = \rho_{\text{CSM},1} r_1^s$ ,  $r_1$  is the innermost radius of the CSM, and  $\rho_{\text{CSM},1}$  is the density of the CSM at  $r_1$ . The CSM is a shell or a stellar wind when  $s = 0$  or  $s = 2$ .

The fit using the four-element model shows that the early-time LCs are mainly powered by the cascade decay of  $^{56}\text{Ni}$ , and the contributions of other radioactive species can be neglected. Therefore, we assume that the early-time LCs were powered by the cascade decay of  $^{56}\text{Ni}$ , while the late-time LCs were mainly powered by the CSI triggered a few days after the explosion. The contributions of other radioactive elements are neglected. The definitions, units, and prior ranges of the free parameters for the  $^{56}\text{Ni}$  plus CSI model are listed in Table 3 (columns 1–4).

We find that the  $^{56}\text{Ni}$  plus CSI model can fit the LCs of PTF 10iuv (see Figure 4 [Figure 4: see original paper]). The medians,  $1\sigma$  ranges, and best-fitting values of the parameters for the cases of  $s = 0$  and  $s = 2$  are listed in Table 3 (columns 5 and 6); the corresponding corner plots are presented in Figures A3 and A4. The derived parameters of the  $^{56}\text{Ni}$  plus CSI model for the case of  $s = 0$  ( $s = 2$ ) are  $M_{\text{ej}} = 2.102_{-0.334}^{+0.035}$  M ( $0.782_{-0.325}^{+0.036}$  M),  $M_{\text{Ni}} = 0.490_{-0.054}^{+0.057}$  M ( $0.640_{-0.074}^{+0.161}$  M),  $M_{\text{CSM}} = 0.555_{-0.270}^{+0.162}$  M ( $0.408_{-0.108}^{+0.023}$  M),  $\rho_{\text{CSM},1} = 42.794_{-10.008}^{+46.001} \times 10^{-15}$  g cm $^{-3}$  ( $1.280_{-0.642}^{+0.642} \times 10^{-15}$  g cm $^{-3}$ ),  $t_{\text{diff}} = 92.470_{-1.546}^{+10.008}$  days ( $38.085_{-1.634}^{+83.315}$  days),  $\epsilon = 0.333_{-0.013}^{+0.068}$  ( $0.162_{-0.023}^{+0.013}$ ),  $r_1 = 0.086_{-0.013}^{+0.068}$  ( $0.057_{-0.013}^{+0.013}$ ),  $\kappa = 0.025_{-0.013}^{+0.068}$  cm $^2$  g $^{-1}$  ( $0.025_{-0.013}^{+0.013}$  cm $^2$  g $^{-1}$ ),  $T_{\text{floor}} = 3332.641_{-83.315}^{+3748.707}$  K ( $3759.749_{-83.315}^{+3748.707}$  K), and  $t_{\text{shift}} = -1.546_{-0.155}^{+1.617}$  days ( $-1.634_{-0.155}^{+1.617}$  days). The values of  $\chi^2/\text{dof}$  for the two cases are 2.419 and 1.938, respectively.

The  $M_{\text{CSM}}$  derived is 0.3 or 0.4 M. As shown in Dan et al. (2011), for a 0.5 and 1.2 M WD system, only 3% of the mass of the secondary star (i.e., 0.015 M) is ejected from the merger. This fraction can be enhanced to 10% (i.e., 0.05 M; Guerrero et al. 2004). The amount of CSM derived here is at least 10 times that from these two values, indicating that this model is disfavored. Moreover, the absence of H $\alpha$  emission lines in the nebular phases (Kasliwal et al. 2012) indicates that the CSM must be hydrogen-poor. Assuming that the CSM originated from a helium-rich companion via accretion or merger, the interaction between the ejecta and this amount of helium-rich CSM would produce helium emission lines. However, Kasliwal et al. (2012) do not report helium emission lines in the spectra. These findings suggest that it is difficult for the  $^{56}\text{Ni}$  plus CSI model to account for the LCs of PTF 10iuv.

### 3. Discussion

#### 3.1. The Nucleosynthesis and Main Energy Sources of PTF 10iuv

The derived  $M_{\text{ej}}$  of PTF 10iuv using the  $^{56}\text{Ni}$  model is  $6.898_{-0.350}^{+0.898}$  M (for multi-band fit) or  $4.22_{-0.73}^{+0.35}$  M (for r-band fit). Both values are significantly larger than the total masses of a WD-WD binary system, favoring the massive star explosion scenario. However, Section 2.1 demonstrates that the massive star scenario is disfavored. Additionally, the  $^{56}\text{Ni}$  plus CSI model is also disfavored. Therefore, we no longer discuss these two models.

The derived  $M_{\text{Ni}}$  is 0.031 M, twice the value (0.016 M) derived by Kasliwal et al. (2012). The derived  $M_{\text{Fe}}$  and  $M_{\text{Cr}}$  are 0.046 M and 0.001 M, respectively. The masses of  $^{56}\text{Ni}$  and  $^{48}\text{Cr}$  are roughly consistent with the numerical results of models CO.55HE.2 and CO.6HE.2 in Waldman et al. (2011) (see the last columns of their Table 2). However, the models in Waldman et al. (2011) suppose that only the helium shells are ejected, while our derived  $M_{\text{ej}}$  favors the scenario in which the carbon-oxygen (CO) WD is also blown up.

Although the derived  $M_{\text{Fe}}$  is slightly larger than  $M_{\text{Ni}}$ , the contribution of  $^{52}\text{Fe}$  is significantly lower than that of  $^{56}\text{Ni}$ . This is because the lifetimes of  $^{52}\text{Fe}$  (0.498

days) and  $^{52}\text{Mn}$  (0.022 days) are significantly shorter than those of  $^{56}\text{Ni}$  (8.764 days) and  $^{56}\text{Co}$  (111.424 days). The contribution of  $^{48}\text{Cr}$  is also significantly lower than that of  $^{56}\text{Ni}$ , due to its low yield (0.001 M, which is 1/30 times  $M_{\text{Ni}}$ ) and short lifetimes of  $^{48}\text{Cr}$  (1.296 days) and  $^{48}\text{V}$  (23.044 days). Therefore, the early-time LCs of PTF 10iuv were mainly powered by the cascade decay of  $^{56}\text{Ni}$ . For comparison, the numerical simulation using CO.45HE.2 shows that the early-time LCs of SN 2005E were mainly powered by cascade decay of  $^{48}\text{Cr}$ , rather than  $^{56}\text{Ni}$ ,  $^{52}\text{Fe}$ , or any other radioactive element (see Figure 4 of Waldman et al. 2011).

The fact that the early-time LCs of PTF 10iuv were mainly powered by  $^{56}\text{Ni}$  indicates that the  $^{56}\text{Ni}$  model can also account for the early-time LCs of PTF 10iuv (but cannot fit the late-time LCs). Nevertheless, the four-element model is necessary, since the  $^{56}\text{Ni}$  model cannot constrain the masses of other radioactive species.

In the four-element model, the late-time LCs of PTF 10iuv were mainly powered by  $^{44}\text{Ti}$  and  $^{56}\text{Ni}$ . The contributions from  $^{48}\text{Cr}$  and  $^{52}\text{Fe}$  can be neglected. The  $^{44}\text{Ti}$  mass of the four-element model is  $0.250_{-0.018}^{+0.018}$  M, which is about 1/8 the  $^{44}\text{Ti}$  mass (2 M) estimated by Kasliwal et al. (2012). This discrepancy might arise because Kasliwal et al. (2012) assumed that all late-time flux was from the cascade decay of  $^{44}\text{Ti}$  (in the scenario where the late-time flux was from  $^{44}\text{Ti}$ ), while our model includes the contribution from  $^{56}\text{Ni}$ , which can reduce the required  $M_{\text{Ti}}$ .

The derived  $M_{\text{Ti}}$  is about 1.65–2 times the upper limit (0.14 M) of the numerical simulations performed for SN 2005E (Perets et al. 2010), or at least 50 times the  $^{44}\text{Ti}$  values (which are of order  $10^{-3}$ – $10^{-5}$  M) listed in Table 5 of Woosley & Kasen (2011). Subtracting the unknown host-galaxy contamination can reduce the inferred  $^{44}\text{Ti}$  mass. Additionally, including flux from other long-lived elements (e.g.,  $^{57}\text{Co}$ ,  $^{55}\text{Fe}$ ,  $^{60}\text{Co}$ ) might also reduce the required amount of  $^{44}\text{Ti}$ . It is reasonable to regard the derived  $^{44}\text{Ti}$  mass as an upper limit and assume that the real  $^{44}\text{Ti}$  mass is (significantly) lower than the value derived by the model.

In general, high values of  $M_{\text{Ti}}$  are required to explain the excesses relative to the LCs powered by  $^{56}\text{Ni}$  and other short-lived radioactive elements at 100–200 days. Another example is the numerical modeling performed by Waldman et al. (2011), which shows that 1.65 M of  $^{44}\text{Ti}$  is needed to explain the bolometric LC of SN 2005E 20–70 days after explosion ( $0.033 \times 50$ , see model a of Figure 5 [Figure 5: see original paper] in Waldman et al. 2011 and the caption).

### 3.2. The Ejecta Mass and Implications for Explosion Mechanisms

The derived  $M_{\text{ej}}$  from the four-element model is  $1.52_{-0.25}^{+0.25}$  M. Kasliwal et al. (2012) suppose that the rise time  $t_r$  and photospheric velocity  $v$  are 12 days and  $7600 \text{ km s}^{-1}$ , respectively, where the latter is the average photospheric velocity of PTF 10iuv. Using the relation  $M_{\text{ej}} \propto vt_r^2$  and comparing the  $M_{\text{ej}}$  and

$v$  of PTF 10iuv to those of SNe Ia, they find that  $M_{\text{ej}}$  of PTF 10iuv is 0.46 M. By replacing  $7600 \text{ km s}^{-1}$  with the  $10,000 \text{ km s}^{-1}$  adopted here, the derived  $M_{\text{ej}}$  is 0.61 M, which is about half of the lower limit of our derived value.

Our derived  $M_{\text{ej}}$  is consistent with the ejecta mass expected from the merger of sub-Chandrasekhar WDs. Furthermore, it is larger than those of the ejected helium shells in the helium detonation scenario. This indicates that the explosion of the sub-Chandrasekhar WDs assumed to be the progenitor of PTF 10iuv left no remnant. For comparison, the numerical simulations for the bolometric LC of SN 2005E (Waldman et al. 2011) suggest that only the helium shell accreted from the companion was ejected, while the CO WD survived after the explosion.

#### 4. Conclusions

In this paper, we model the LCs of PTF 10iuv, constraining the physical properties of its ejecta, the energy sources, and the explosion mechanisms. We find that the  $^{56}\text{Ni}$  model and the  $^{56}\text{Ni}$  plus CSI model cannot account for the photometry of PTF 10iuv, while the four-element ( $^{56}\text{Ni}$ ,  $^{48}\text{Cr}$ ,  $^{52}\text{Fe}$ , and  $^{44}\text{Ti}$ ) model can successfully fit the LCs.

In the four-element model, the early-time LCs of PTF 10iuv were mainly powered by  $^{56}\text{Ni}$ , and the contributions of  $^{48}\text{Cr}$  and  $^{52}\text{Fe}$  can be neglected. To explain the late-time LCs, 0.25 M of  $^{44}\text{Ti}$  is required. This value is rather high and can be regarded as the upper limit of the real  $^{44}\text{Ti}$  mass. We suggest that subtracting the unknown contributions from the host galaxy and including flux from some long-lived elements ( $^{57}\text{Co}$ ,  $^{55}\text{Fe}$ ,  $^{60}\text{Co}$ ) can reduce the required amount of  $^{44}\text{Ti}$ . Therefore, the derived  $^{44}\text{Ti}$  mass can be regarded as an upper limit. The derived  $M_{\text{ej}}$  of the four-element model is  $1.52_{-0.25}^{+0.25}$  M, consistent with the ejecta mass expected from the merger of sub-Chandrasekhar WDs.

We caution that one of the assumptions of our modeling is that the SEDs of PTF 10iuv at all epochs can be described by a blackbody function. We cannot verify whether this assumption is correct at late-time epochs, since data are available in only one band (r-band). The modeling for a late-time r-band LC would be invalid if the late-time SEDs deviate from the blackbody function. This is the main caveat of our work. Additionally, possible host galaxy contamination prevents us from obtaining more accurate results.

Late-time multi-band photometric observations and detailed modeling of the LCs can provide more stringent constraints on the precise values of  $^{44}\text{Ti}$  mass in Ca-rich SNe. We expect that further observations of the late-time LCs of Ca-rich SNe and modeling of these observations can constrain their nucleosynthesis, energy sources, and explosion mechanisms.

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## Appendix

Figures A1–A4 display the corner plots of the fits for the LCs of PTF 10iuv using the  $^{56}\text{Ni}$  model, the four-element model, and the  $^{56}\text{Ni}$  plus CSI model, respectively.

**Figure A1.** The corner plots of the  $^{56}\text{Ni}$  model for the multi-band LCs (upper panel) and r-band LC (lower panel, where the late-time flux has been subtracted) of PTF 10iuv. The solid vertical lines represent the best-fitting parameters, while the dashed vertical lines represent the medians and the  $1\sigma$  bounds of the parameters.

**Figure A2.** The corner plot of the four-element model for the multi-band LC of PTF 10iuv. The solid vertical lines represent the best-fitting parameters, while the dashed vertical lines represent the medians and the  $1\sigma$  bounds of the parameters.

**Figure A3.** The corner plot of the  $^{56}\text{Ni}$  plus CSI model ( $s = 0$ ). The solid vertical lines represent the best-fitting parameters, while the dashed vertical lines represent the medians and the  $1\sigma$  bounds of the parameters.

**Figure A4.** The corner plot of the  $^{56}\text{Ni}$  plus CSI model ( $s = 2$ ). The solid vertical lines represent the best-fitting parameters, while the dashed vertical lines represent the medians and the  $1\sigma$  bounds of the parameters.

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