

Hadron multiplicities in p+p and p+Pb collisions at the LHC postprint

Authors: Wang Hong-Min, HOU Zhao-Yu, SUN Xian-Jing

Date: 2023-06-18T00:00:00+00:00

Abstract

Experiments at the Large Hadron Collider (LHC) have measured multiplicity distributions in p+p and p+Pb collisions at a new domain of collision energy. Based on considering an energy-dependent broadening of the nucleon's density distribution, charged hadron multiplicities are studied with the phenomenological saturation model and the evolution equation dependent saturation model. By assuming the saturation scale has a small dependence on the 3-dimensional root mean square (rms) radius at different energy, the theoretical results are in good agreement with the experimental data from CMS and ALICE collaboration. The predictive results in p+p collisions at $s=14$ TeV of the LHC are also given.

Full Text

Preamble

Hadron multiplicities in p+p and p+Pb collisions at the LHC

WANG Hong-Min (王宏民),^{1,†} HOU Zhao-Yu (侯召宇),² and SUN Xian-Jing (孙献静)³

¹Physics Department, Academy of Armored Forces Engineering of PLA, Beijing 100072, China

²Physics Graduate School, Shijiazhuang Railway Institute, Shijiazhuang 050043, China

³Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China

(Received December 28, 2013; accepted in revised form January 27, 2014; published online August 10, 2014)

Experiments at the Large Hadron Collider (LHC) have measured multiplicity distributions in p+p and p+Pb collisions at a new domain of collision energy.

Based on considering an energy-dependent broadening of the nucleon's density distribution, charged hadron multiplicities are studied with the phenomenological saturation model and the evolution equation dependent saturation model. By assuming the saturation scale has a small dependence on the 3-dimensional root mean square (rms) radius at different energy, the theoretical results are in good agreement with the experimental data from CMS and ALICE collaboration. The predictive results in p+p collisions at $\sqrt{s} = 14$ TeV of the LHC are also given.

Keywords: Hadron multiplicities, Negative binomial distribution, Gluon saturation

DOI: 10.13538/j.1001-8042/nst.25.040502

Introduction

Charged hadron multiplicities in relativistic heavy ion collisions are of great significance as their variables are very sensitive to the underlying mechanism involved in nuclear collisions [?]. These can provide a unique opportunity to test the predictions of quantum chromodynamics (QCD) and understand the partonic structure of the colliding nuclei. Among the variables, the pseudo-rapidity distribution and negative binomial distribution (NBD) are two important and interesting quantities to be studied on both experimental and theoretical sides in recent years [?].

The pseudo-rapidity distribution of charged hadrons is a quantity always used to investigate the particle production mechanism in high energy hadron-hadron and nucleus-nucleus collisions. Since pseudo-rapidity density is sensitive to the initial conditions of the system and the hadronic final state interactions, the study of charged hadron densities at mid-rapidity can provide relevant information on the interplay between hard parton-parton scattering processes and soft processes. The NBD is another quantity that plays a major role in describing the multiplicity distribution of produced charged particles. The NBD can describe well the multiplicity distribution in almost all inelastic high energy collision processes except for the data at the highest available collider energies. In this paper, the pseudo-rapidity distribution and the NBD in p+p and p+Pb collisions will be studied in the framework of the Color Glass Condensate.

At very high energies or small Bjorken- x , QCD predicts that high density gluons in a hadron wave function form a new state, the Color Glass Condensate (CGC). In this regime, the gluon density increases inside the hadron wave functions and becomes very large in comparison to all other parton species (the valence quarks), and the sea quarks are suppressed by the coupling α_s since they can be produced from the gluons by the splitting $g \rightarrow q\bar{q}$.

Now, CGC has become an effective theory for describing the gluon content of a high energy hadron or nucleus in the saturation regime, and many saturation models have been established [?]. These saturation models can be divided into two main kinds: the phenomenological saturation model and the evolution

equation dependent saturation model. The phenomenological saturation models, such as the Golec-Biernat and Wüsthoff (GBW) model [?], the Kharzeev, Levin, and Nardi (KLN) model [?], and the Kovchegov, Lu, and Rezaeian (KLR) model [?], are very simple and their dipole-proton scattering amplitude can be given by an analytic expression. The evolution equation dependent saturation models, such as the impact parameter dependent saturation model (IP-Sat) [?] and the running coupling Balitsky-Kovchegov (rcBK) model [?], are based on the DGLAP or the rcBK evolution equation and they are very useful at small Bjorken- x or high collision energy. Having studied charged particle multiplicity distribution with the GBW model [?], we will investigate charged hadron pseudo-rapidity distribution and the NBD with the phenomenological KLN model and the evolution equation dependent rcBK model, respectively.

In order to give an accurate theoretical analysis, the nucleon's density distribution in position space, which controls the unintegrated gluon distribution (UGD) through the saturation scale Q_s , must be considered. It should be pointed out that, due to gluon saturation, the width of the gluon distribution inside a nucleon should grow with collision energy \sqrt{s} [?]. This will lead to a broadening of the nucleon's density distribution in position space as \sqrt{s} increases. Thus, we consider an energy-dependent broadening of the Gaussian nucleon thickness function, and assume the saturation scale has a small dependence on the 3-dimensional root mean square (rms) radius at different collision energies [?].

The outline of this paper is as follows. The theoretical method is given in Sec. II and the results and discussion are given in Sec. III.

II. Method

For hadron-hadron collisions, the multiplicity per unit rapidity and per unit transverse area can be given by [?]

$$\frac{d^{2N}}{d^2b dy} = \frac{2\pi_c^{3N}}{C_F} \frac{1}{\alpha_s} \int \frac{d^2k}{k_T^2} \int d^2p \varphi(x_1, k_T^2, b) \varphi(x_2, (k_T + p_T)^2, b - r_\perp)$$

where $N_c = 3$, $x_{1,2} = (p_T/\sqrt{s}) \exp(\pm y)$, b is the impact factor and r is the transverse position of the gluon. The running coupling constant $\alpha_s(k^2) = \min\left[\frac{4\pi}{\beta_0 \ln[(k^2 + \Lambda^2)/\Lambda^2]}, 0.5\right]$ with $\beta_0 = 11 - \frac{2}{3}n_f = 9$ and $\Lambda = \Lambda_{\text{QCD}} = 0.2$ GeV.

For the unintegrated gluon distribution φ , we will use the form given by the KLN model [?] and the rcBK model [?].

In the KLN model, φ is taken to be

$$\varphi(x, k^2, b) = \begin{cases} \frac{\kappa C_F}{\pi^3 \alpha_s(Q_s^2)} \frac{Q_s^2}{k^2 + \Lambda^2}, & k \leq Q_s \\ \frac{\kappa C_F}{\pi^3 \alpha_s(Q_s^2)} \frac{Q_s^2}{k^2 + \Lambda^2}, & k > Q_s \end{cases}$$

where $C_F = (N_c^2 - 1)/(2N_c)$ and κ is a normalization factor. The unintegrated gluon distribution depends on transverse position through the saturation scale $Q_s^2(x, b) = Q_{s,0}^2 \left(\frac{x_0}{x}\right)^\lambda T_p(b)$, where $Q_0^2 = 2 \text{ GeV}^2$, $\lambda = 0.288$ [?], and $T_{p,0}$ is taken as 1 fm^{-2} . For the nucleon thickness function, the Gaussian form is used $T_p(b) = e^{-b^2/(2B)}$, where the proton width parameter B can be computed from [?] and $\sigma_{\text{in}}(\sqrt{s})$ is the inelastic scattering cross section.

In this paper, we assume the gluon saturation scale has a small dependence on the 3-dimensional rms radius of the proton [?]:

$$Q_s^2(\sqrt{s}) = Q_{s,0}^2 \left(\frac{r_{\text{rms}}(\sqrt{s})}{r_{\text{rms},0}} \right)^{1/\delta}$$

where $\delta = 0.8$ [?] and the 3-dimensional rms radius $r_{\text{rms}} = \sqrt{\langle r^2 \rangle} = \sqrt{3B}$. In Table 1 we collect a few representative values.

TABLE 1. The 3-dimensional rms radius for various collision energies. The values for σ_{in} at LHC energies were reported in Ref. [?, ?, ?]

\sqrt{s} (TeV)	σ_{in} (mb)	B (fm)	r_{rms} (fm)
------------------	---------------------------	----------	-----------------------

In the rcBK model, the unintegrated gluon distribution can be obtained from the dipole scattering amplitude via a Fourier transform:

$$\varphi(x, k) = \int \frac{d^2r}{2\pi r^2} e^{ik \cdot r} N(x, r) = \int dr J_0(rk) N(x, r)$$

where J_0 is the spherical Bessel function of the first kind. The dipole scattering amplitude in the rcBK evolution reads [?]:

$$\frac{\partial N(r, Y)}{\partial Y} = \int dr_1 K_{\text{Bal}}(r, r_1, r_2) [N(r_1, Y) + N(r_2, Y) - N(r, Y) - N(r_1, Y)N(r_2, Y)]$$

and the kernel for the running term using Balitsky' s prescription reads:

$$K_{\text{Bal}}(r, r_1, r_2) = \frac{N_c \alpha_s(r^2)}{r^2} \left[\frac{\alpha_s(r_1^2)}{\alpha_s(r^2)} \right]^\gamma \left[\frac{\alpha_s(r_2^2)}{\alpha_s(r^2)} \right]^\gamma$$

where $\gamma = 1$ and $Q_{s,0}^2$ is the initial saturation scale squared.

For the initial conditions, the GBW ansatz is used for the dipole scattering amplitude [?]:

$$N_{\text{GBW}}(r, Y = 0) = 1 - \exp \left[-\frac{r^2 Q_{s,0}^2}{4} \right]^\gamma$$

Now let us take into account the negative binomial distribution. Negative binomial distribution is a general property of multi-particle production processes regardless of the type of colliding particles, and the negative binomial probability distribution for obtaining n charged particles in the final state is given as follows:

$$P(n) = \frac{\Gamma(k+n)}{\Gamma(k)\Gamma(n+1)} \left(\frac{\bar{n}}{k}\right)^n \left(1 + \frac{\bar{n}}{k}\right)^{-n-k}$$

where the mean multiplicity \bar{n} can be calculated in the framework of CGC by integrating y in Eq. (1). The quantity k , which is the fluctuation parameter, can be estimated as a function of the saturation scale [?]:

$$k = \kappa' \frac{N_c^2 - 1}{Q_{s,p}^2(y, \sqrt{s}) \sigma_{\text{in}}(\sqrt{s})}$$

where κ' is a normalization factor. Here, in order to get an analytic expression between $Q_{s,p}$ and y , $Q_{s,p}$ is reconsidered by substituting $x_{1,2} = (Q_s/\sqrt{s})e^{\pm y}$ into Eq. (3) as in Ref. [?].

III. Results and Discussion

To evaluate the pseudo-rapidity distribution, Eq. (1) should be rewritten using the transformation:

$$y(\eta) = \frac{1}{2} \ln \left[\frac{\sqrt{m_0^2 \cosh^2 \eta + p_T^2} + p_T \sinh \eta}{\sqrt{m_0^2 \cosh^2 \eta + p_T^2} - p_T \sinh \eta} \right]$$

and the Jacobian can be correspondingly written as $J(\eta) = \frac{p_T \cosh \eta}{\sqrt{m_0^2 \cosh^2 \eta + p_T^2}}$, where m_0 is the rest mass of the particle, which corresponds to the order of the scale Λ_{QCD} .

With a χ^2 analysis of the experimental data [?], the factor κ in Eq. (2) is equal to 0.51 and 0.89 for the theory with and without considering the rms radius dependent saturation scale, respectively. In Fig. 1 [Figure 1: see original paper], the theoretical results for pseudo-rapidity distribution of charged hadrons in p+p collisions at $\sqrt{s} = 0.9$ TeV (a), 2.36 TeV (b), 7 TeV (c), and 14 TeV (d) are shown. The solid and dashed curves are the results of the KLN model with and

without considering the rms radius dependence of the saturation scale, respectively. The dotted curves are the results of the rcBK model. The experimental data comes from CMS [?, ?].

It is shown that the theoretical results of the KLN model considering the rms radius dependence are in good agreement with the experimental data. Since the effective value of Bjorken- x in the rcBK model is $10^{-12} < x < 0.01$, it is not valid at \sqrt{s} or large pseudo-rapidity. Thus, only the results at $\sqrt{s} = 7$ TeV fit well to the data with the rcBK model. The results shown in Fig. 1(d) are the predictive results for the forthcoming LHC experiment at $\sqrt{s} = 14$ TeV, and it is shown that the predictive results of the rcBK model are almost the same as those of the KLN model.

Figure 2 [Figure 2: see original paper] shows the negative binomial distribution of charged hadrons at $|\eta| < 0.5$. The symbols and lines in Fig. 2 are the same as those in Fig. 1. The experimental data comes from ALICE [?]. The agreement is seen to be quite good for the KLN model considering the rms radius dependent saturation scale at $\sqrt{s} = 0.9$ TeV and 2.36 TeV and for the rcBK model at $\sqrt{s} = 7$ TeV. Here, it should be noted that the agreement is not quite good for the theoretical results of the KLN model at $\sqrt{s} = 7$ TeV even after considering the rms radius dependent saturation scale. Thus, we will give a systematic analysis of all η regions by considering the impact factor dependence of the mean multiplicity and the quantity k in the near future.

Recently, the experimental data of charged hadron multiplicity in p+Pb collisions at $\sqrt{s} = 5.02$ TeV have been given by the ALICE collaboration [?]. In order to further test the theory, the pseudo-rapidity distribution of charged hadrons in p+Pb collisions is investigated. For the nuclear density distribution of Pb, we use the Woods-Saxon distribution [?]:

$$\rho(r) = \frac{\rho_0}{1 + \exp[(r - R)/a]}$$

where ρ_0 corresponds to the nucleon density in the center of the nucleus, R is the nuclear radius, and a is the “skin depth” .

The theoretical results are shown in Fig. 3 [Figure 3: see original paper]. The solid curve is the result of the KLN model and the dashed curve is the result that we gave in Ref. [?]. The dotted and dash-dotted curves are the results of DPMJET [?] and HIJING with the gluon shadowing parameter $s_g = 0.28$ [?], respectively. It is shown that the theoretical results of the KLN model fit well to the new experimental data.

IV. Conclusion

In summary, the pseudo-rapidity distribution and the NBD of charged hadrons in p+p and p+Pb collisions are studied with the phenomenological KLN model and the rcBK model. By considering an energy-dependent broadening of the

nucleon' s density distribution in position space and the rms radius dependence of the gluon saturation scale, it is found that the theoretical results are in good agreement with the experimental data from CMS and ALICE. The predictive results in p+p collisions at $\sqrt{s} = 14$ TeV of the LHC will be examined by the forthcoming experiment.

References

- [?] Kumar A, Srivastava P K, Singh B K, et al. arXiv: hep-ph/1306.4185.
- [?] Khachatryan V, Sirunyan A M, Tumasyan A, et al. J High Energy Phys, 2010, 02: 041.
- [?] Khachatryan V, Sirunyan A M, Tumasyan A, et al. Phys Rev Lett, 2010, 105: 022002.
- [?] Aamodt K, Abel N, Abeyssekara U, et al. Eur Phys J C, 2010, 68: 345-354.
- [?] Abelev B, Adam J, Adamova D, et al. Phys Rev Lett, 2013, 110: 032301.
- [?] Dumitru A, Kharzeev D E, Levin E M, et al. Phys Rev C, 2012, 85: 044920.
- [?] Wang H M, Liu J F, Hou Z Y, et al. Chinese Phys C, 2013, 37: 011001.
- [?] Golec-Biernat K, Wüsthoff M. Phys Rev D, 1999, 59: 014017.
- [?] Kharzeev D, Levin E, Nardi M. Nucl Phys A, 2004, 730: 448-459.
- [?] Kovchegov Y V, Lu Z, Rezaeian A H. Phys Rev D, 2009, 80: 074023.
- [?] Kowalski H and Teaney D. Phys Rev D, 2003, 68: 114005.
- [?] Albacete J L, Armesto N, Milhano J G, et al. Phys Rev D, 2009, 80: 034031.
- [?] Heinz U, Moreland J S. Phys Rev C, 2011, 84: 054905.
- [?] Armesto N, Salgado C A, Wiedemann U A. Phys Rev Lett, 2005, 94: 022002.
- [?] Kuhlman A, Heinz U, Kovchegov Y V. Phys Lett B, 2006, 638: 171-178.
- [?] Albacete J L, Dumitru A, Fujii H, et al. Nucl Phys A, 2013, 897: 1-27.
- [?] Block M M and Halzen F. Phys Rev D, 2011, 83: 077901.
- [?] Wang H M, Hou Z Y, Zhang B A, et al. Int J Mod Phys A, 2010, 25: 1009-1018.
- [?] Miller M L, Reygers K, Sanders S J, et al. Annu Rev Nucl Part S, 2007, 57: 205-243.
- [?] Roesler S, Engel R, Ranft J. arXiv: hep-ph/0012252.
- [?] Xu R, Deng W T, Wang X N. arXiv: nucl-th/1204.1998.

Note: Figure translations are in progress. See original paper for figures.

Source: ChinaXiv –Machine translation. Verify with original.