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# Efficient Revocable Identity-Based SM9 Signature Algorithm Postprint

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### Abstract

SM9-IBS is an identity-based signature algorithm industry standard published by China in 2016. Although identity-based signature algorithms reduce the complexity of system management of user public keys, they suffer from the difficult problem of key revocation. Furthermore, the special structure of SM9 makes existing techniques not fully applicable. To this end, a revocable SM9 identity-based signature algorithm is proposed, enabling rapid revocation and update operations of user signing privileges. The algorithm introduces a complete subtree, with which the key center generates temporary signing keys for each legitimate user; only signatures generated using this key can be successfully verified. In terms of security, the algorithm is proven to satisfy existential unforgeability under adaptive chosen-message and identity attacks in the random oracle model. In terms of efficiency, when the number of system users is large and the number of revoked users is small during the key update phase, the time overhead for the key center to update user signing keys is far less than the update technique of Boneh et al.

#### Full Text

## Preamble

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## Efficient Revocable SM9 Identity-Based Signature Algorithm

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Abstract: SM9-IBS is an industry standard for identity-based signature algorithms issued by China in 2016. Although identity-based signature algorithms reduce the complexity of public key management, they face the challenge of key revocation. Moreover, SM9's special algebraic structure makes existing revocation techniques inapplicable. This paper proposes an efficient revocable SM9 identity-based signature algorithm that enables rapid revocation and updating of user signing privileges. The algorithm introduces a complete subtree through which the Key Generation Center (KGC) generates temporary signing keys for each legitimate user, ensuring only signatures produced with these keys pass verification. Security-wise, the algorithm is proven existentially unforgeable under adaptive chosen message and identity attacks in the random oracle model. In terms of efficiency, when the system has many users but few revoked ones, the KGC's time overhead for updating user signing keys is significantly lower than Boneh et al.'s update technique.

**Keywords:** identity-based cryptosystem; SM9 signature algorithm; key revocation; complete subtree

## 1.1 Symbol Description

In this paper, if S is an algorithm, then  $s \leftarrow S$  denotes executing algorithm S with output s; if S is a set, then  $s \leftarrow S$  denotes uniformly random selection of an element s from set S. A||B represents concatenation of two bit strings A and B.

In the SM9 algorithm:

- a)  $H_v(\cdot)$  is a cryptographic hash function that takes arbitrary bit strings as input and outputs v bits.
- b)  $H_2(\cdot)$  is a cryptographic function that takes as input a cryptographic hash function  $H_v(\cdot)$ , a bit string Z, and an integer p, and outputs an integer in  $\mathbb{Z}_p^*$ .

## 1.2 Bilinear Mapping

Let  $\mathbb{G}_1$ ,  $\mathbb{G}_2$ , and  $\mathbb{G}_T$  be cyclic groups of prime order p, with  $g_1$  and  $g_2$  as generators of  $\mathbb{G}_1$  and  $\mathbb{G}_2$  respectively. A bilinear map  $e:\mathbb{G}_1\times\mathbb{G}_2\to\mathbb{G}_T$  must satisfy the following properties:

- a) Bilinearity: For any  $\alpha, \beta \in \mathbb{Z}_p^*$ ,  $e(g_1^{\alpha}, g_2^{\beta}) = e(g_1, g_2)^{\alpha\beta}$ .
- b) Non-degeneracy:  $e(g_1, g_2) \neq 1_{\mathbb{G}_T}$ .
- c) Computability: For any  $h_1 \in \mathbb{G}_1$  and  $h_2 \in \mathbb{G}_2$ , there exists an efficient polynomial-time algorithm to compute  $e(h_1, h_2)$ .



# 1.3 Hardness Assumption

This section introduces the q-Strong Diffie-Hellman (q-SDH) problem, upon which the SM9 signature algorithm's security against existential forgery under adaptive chosen message and identity attacks (EU-CMIA) relies, as proposed in [?]. Let  $e: \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$  be a bilinear map, with  $g_1$  and  $g_2$  as generators of  $\mathbb{G}_1$  and  $\mathbb{G}_2$  respectively, where groups  $\mathbb{G}_1$ ,  $\mathbb{G}_2$ , and  $\mathbb{G}_T$  have prime order p.

The q-SDH problem in bilinear groups is defined as follows:

**Definition 1 (q-SDH Problem).** Given q+1 group elements  $(g_1, g_1^a, g_1^{a^2}, \dots, g_1^{a^q}, g_2, g_2^a)$  where  $a \in \mathbb{Z}_p^*$  is unknown, find a pair  $(c, g_1^{1/(a+c)})$  with  $c \in \mathbb{Z}_p^*$ . If the probability of solving the q-SDH problem in polynomial time is negligible, the q-SDH assumption holds.

# 1.4 SM9-IBS Identity-Based Signature Algorithm

The SM9 identity-based signature algorithm (SM9-IBS) consists of four (probabilistic) polynomial-time algorithms: system parameter generation, user key extraction, signature generation, and verification. We briefly review the SM9-IBS algorithm below.

- a) System Setup: The KGC first runs the algorithm SM9.Setup $(1^{\lambda})$  on input security parameter  $\lambda$  to generate a bilinear group  $(p, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T, e, g_1, g_2)$ . Then it selects a random  $s \in \mathbb{Z}_p^*$  as the master secret key. The system master public key and master secret key are  $mpk = (g_1, g_2, g_2^s, H_2(\cdot))$  and msk = s respectively. The system master public key serves as the default input for other algorithms (omitted for brevity).
- **b) User Key Extraction:** For a user with identity id, the KGC computes the signing private key as  $ds_{id} = g_1^{s \cdot H_2(H_v(id))}$ , where  $H_2(H_v(id)) \in \mathbb{Z}_p^*$ . The signer's public key is id and private key is  $ds_{id}$ .
- c) Signing: A signer with identity id signs message M as follows:
- 1. Select random  $r \in \mathbb{Z}_p^*$  and compute  $w = g_2^r$ .
- 2. Compute  $h = H_2(H_v^r(M|id), w)$ .
- 3. If  $h = 0 \pmod{p}$ , return to step 1.
- 4. Compute  $l = (r h) \cdot s^{-1} \pmod{p}$ .
- 5. Compute  $S = ds_{id}^l$ .

The signature on M is  $\sigma = (h, S)$ .

- d) Verification: Upon receiving signer's identity id, message M, and signature  $\sigma = (h, S)$ , the verifier:
- 1. Computes  $w' = g_2^h \cdot e(S, g_2^{s \cdot H_2(H_v(id))})$ .
- 2. Computes  $h' = H_2(H_v(M||id), w')$ .
- 3. Accepts the signature if h' = h; otherwise rejects.



Note 1: To improve signing and verification efficiency, the fixed value  $e(g_1, g_2)$  computed in the original SM9-IBS algorithm can be included in the system public key, reducing one bilinear pairing operation in both signing and verification while adding one  $\mathbb{G}_T$  element to the system public key.

The EU-CMIA security model for identity-based signature algorithms is similar to traditional signature schemes, except that besides trivial queries, the adversary can adaptively choose any identity to obtain its signing key and any message to obtain its signature. See [?] for details.

Under this model, we have:

**Theorem 1 (Security of SM9-IBS** [?]). In the random oracle model, if the q-SDH problem is hard, then SM9-IBS satisfies EU-CMIA security.

### 2.1 RIBS Definition

Figure 1 illustrates the system model of revocable identity-based signature (RIBS), which involves four entities:

- a) Key Generation Center (KGC): Generates system master public key mpk and master secret key msk, creates long-term signing keys  $ds_{id}$  for users with identity id, generates update key sets  $uk_t$ , maintains user revocation list RL, and manages a full binary tree Tree corresponding to all user identities.
- b) Data Signer (DS): Computes digital signature  $\sigma$  on original message M.
- c) Storage Server (SS): Stores user signatures.
- d) Signature Verifier (SV): Verifies the validity of received signatures  $\sigma$ .
- **Definition 2 (RIBS Definition).** A RIBS algorithm consists of eight (probabilistic) polynomial-time algorithms: system parameter generation, user registration, update node generation for non-revoked users, update key generation, temporary signing key generation, signing, verification, and user revocation.
- a) Setup( $1^{\lambda}$ ): Executed by the KGC. Takes security parameter  $\lambda$  as input and outputs system master public key mpk and master secret key msk. The KGC maintains an initially empty revocation list RL and a full binary tree Tree corresponding to all user identities.
- b) Register(msk, id): Executed by the KGC. Takes master secret key and user identity id as input, adds id to Tree, and outputs the user's long-term signing key  $ds_{id}$ .
- c) KUNode(Tree, RL, t): Executed by the KGC. Takes identity tree Tree, revocation list RL, and time t as input, and outputs the set of nodes KUNodes for which update keys need to be generated.



- d) UpdateK(msk, t, KUNodes): Executed by the KGC. Takes master secret key msk, time t, and non-revoked node set KUNodes as input, and outputs update key set  $uk_t$ , broadcast to system users via public channel.
- e) **TempK**( $ds_{id}$ ,  $uk_t$ ): Executed by the data signer. Takes user's long-term signing key  $ds_{id}$  and update key set  $uk_t$  as input. If the user is not revoked, it outputs a temporary signing key  $ts_{id,t}$  (containing user identity id, update time t, and corresponding update node information  $\theta$ ); if revoked, it outputs  $\bot$ .
- f)  $\operatorname{Sign}(M, ts_{id,t})$ : Executed by the data signer. Takes message M and user temporary signing key  $ts_{id,t}$  as input, computes signature  $\sigma$  on M (containing time period and update node information), and sends  $(M, \sigma)$  to the storage server.
- g) Verify( $id, M, \sigma$ ): Executed by the signature verifier. Takes signer's identity id, message M, and signature  $\sigma$  as input, and outputs verification result (1 for valid, 0 for invalid).
- h) Revoke(id, t, RL): Executed by the KGC. Takes revoked user identity id, time period t, and revocation list RL as input, adds (id, t) to RL, and returns the updated list.

# 2.2 Security Model

To characterize the key revocation mechanism, we describe existential unforgeability under adaptive chosen message and identity attacks (EU-CMIA) through a game between adversary and challenger. In this model, the adversary can query any user's long-term signing key. When a user's key is compromised (queried by the adversary) and revoked by the KGC at time t, the scheme's security ensures the adversary cannot generate a valid signature for that user at time t.

**Definition 3 (EU-CMIA Security of RIBS).** Let  $\mathcal{A}$  be any probabilistic polynomial-time adversary and  $\mathcal{C}$  be a challenger. The security experiment  $\operatorname{Exp}^{\operatorname{EU-CMIA}}_{\operatorname{RIBS},\mathcal{A}}(1^{\lambda})$  is defined as:

- a) Setup: Challenger runs Setup $(1^{\lambda})$  to generate master public key mpk and master secret key msk, initializes empty key revocation list RL and full binary tree Tree, and sends mpk to  $\mathcal{A}$ .
- b) Queries:  $\mathcal{A}$  can adaptively make polynomially many queries:
  - Long-term signing key query: When  $\mathcal{A}$  queries user id's long-term signing key, challenger runs Register(msk,id) to generate key  $ds_{id}$  and returns it, adding id to set  $L_1$ .
  - Update key query: When  $\mathcal{A}$  queries update key for time t, challenger first runs KUNode(Tree, RL, t) to get update node set  $KUNodes_t$ , then



runs  $\mathrm{UpdateK}(msk,t,KUNodes_t)$  to obtain update key set  $uk_t,$  and returns it.

- Signature query: When  $\mathcal{A}$  queries signature on message M for identity id at time t, challenger first checks if id was revoked at or before t (assuming  $\mathcal{A}$  always queries update key for time t first). If not revoked, challenger uses  $ds_{id}$  and  $uk_t$  to generate temporary signing key  $ts_{id,t}$ , then signs M to get  $\sigma$  and returns it, adding (id, t, M) to set  $L_2$ .
- Revocation query: When  $\mathcal{A}$  queries revocation of identity id at time t, challenger adds (id, t) to revocation list RL.
- c) Forgery:  $\mathcal{A}$  outputs a forged signature  $(M^*, \sigma^*)$  for challenge identity  $id^*$  and time  $t^*$ , satisfying: If  $id^*$  was not revoked at or before  $t^*$ , then  $id^* \notin L_1$ . If  $id^*$  was revoked at or before  $t^*$ , then  $(id^*, t, M^*) \notin L_2$  for any  $t \leq t^*$ .
- d) Output: If the forged signature passes verification,  $\mathcal{A}$  wins and challenger returns 1; otherwise returns 0.

 $\mathcal{A}$ 's success probability is  $\Pr[\operatorname{Exp}^{\operatorname{EU-CMIA}}_{\operatorname{RIBS},\mathcal{A}}(1^{\lambda})=1]$ . The RIBS algorithm is EU-CMIA secure if this probability is negligible in  $\lambda$ .

# 2.3 Algorithm Design

This section presents a revocable SM9 identity-based signature algorithm using complete subtree coverage (denoted CS-SM9-RIBS).

- a) Setup(1<sup>\(\lambda\)</sup>): On input security parameter \(\lambda\): 1. KGC runs bilinear group generation to get  $(p, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T, e, g_1, g_2)$ . Assume each user identity is n bits long. KGC initializes a full binary tree Tree of height n+1 and empty revocation list RL. 2. KGC selects random  $s \in \mathbb{Z}_p^*$  and computes  $P_{pub} = g_2^s$ . The master public key is  $mpk = (g_1, g_2, P_{pub}, H_2(\cdot))$  and master secret key is msk = s.
- b) Register(msk, id): For user registration request with identity id: 1. KGC uses SM9 key extraction to generate signing key:  $ds_{id} = g_1^{s \cdot H_2(H_v(id))}$ . 2. KGC assigns a leaf node matching id, adds id to Tree, and sends  $ds_{id}$  to the user.
- c) **KUNode**(Tree, RL, t): On input identity tree Tree, revocation list RL, and time t: 1. Let X and Y be empty sets. For each non-leaf node  $\theta$  in Tree, let  $\theta_l$  and  $\theta_r$  be its left and right children. Let Path(id) be the set of nodes on the path from root to leaf node for identity id. 2. For each  $(id, t') \in RL$  with  $t' \leq t$ , add Path(id) to X. 3. For each node  $\theta \in X$ : if  $\theta_l \notin X$ , add  $\theta_l$  to Y; if  $\theta_r \notin X$ , add  $\theta_r$  to Y. 4. If  $Y = \emptyset$ , set  $Y = \{\text{root}\}$ . 5. Output KUNodes = Y.

Figures 2 and 3 show examples of update node selection. In these examples, the binary tree has height 4 (identity length = 3 bits). Blue nodes represent current update nodes; dashed nodes represent revoked users. Figure 2 shows no revocation ( $KUNodes = \{\text{root}\}$ ). Figure 3 shows user with identity "3" revoked, yielding  $KUNodes = \{00, 010, 1\}$ .

- d) UpdateK(msk, t, KUNodes): On input master secret key msk, time t, and update node set KUNodes: 1. KGC computes update identity set  $\{UID||t|\theta\}_{\theta \in KUNodes}$  where  $UID||t|\theta$  concatenates time and node information. 2. For each identity in the set, KGC uses SM9 key extraction to generate key  $ds_{UID||t|\theta}$ . 3. The update key set is  $uk_t = \{ds_{UID||t|\theta}\}_{\theta \in KUNodes}$ , broadcast via public channel.
- e)  $\mathbf{TempK}(ds_{id}, uk_t)$ : On input user's long-term signing key  $ds_{id}$  and update key set  $uk_t$ : 1. If user is not revoked, there exists a unique common node  $\theta \in Path(id) \cap KUNodes$ . User finds corresponding update key  $ds_{UID||t|\theta}$  and defines temporary signing key as  $ts_{id,t} = (ds_{id}, ds_{UID||t|\theta}, \theta)$ . If revoked, output  $\bot$ . 2. Return  $ts_{id,t}$ .
- f)  $\operatorname{Sign}(M, ts_{id,t})$ : On input message M and temporary signing key  $ts_{id,t}$ : 1. If  $ts_{id,t} = \bot$ , abort. 2. Recover  $ds_{id}$  and  $ds_{UID||t|\theta}$  from  $ts_{id,t}$ , let  $M' = M||t||\theta$ . 3. Generate first signature component:  $\sigma_1 \leftarrow \operatorname{SM9.Sign}(ds_{id}, M')$ . 4. Generate second signature component:  $\sigma_2 \leftarrow \operatorname{SM9.Sign}(ds_{UID||t|\theta}, M')$ . 5. Output final signature  $\sigma = (\sigma_1, \sigma_2, \theta)$ .
- g) Verify $(id, M, \sigma)$ : On input signer's identity id, message M, and signature  $\sigma = (\sigma_1, \sigma_2, \theta)$ : 1. Check if node  $\theta$  is on Path(id). If not, return 0. 2. Compute  $M' = M||t||\theta$  and verify  $\sigma_1$  using SM9.Verify with identity id:  $b_1 \leftarrow \text{SM9.Verify}(id, M', \sigma_1)$ . If  $b_1 = 0$ , return 0. 3. Verify  $\sigma_2$  using SM9.Verify with update identity  $UID||t|\theta$ :  $b_2 \leftarrow \text{SM9.Verify}(UID||t|\theta, M', \sigma_2)$ . If  $b_2 = 0$ , return 0. 4. Return 1 if all checks pass.
- h) Revoke(id, t, RL): On input revoked user identity id, time period t, and revocation list RL: 1. If  $(id, t') \in RL$  for some  $t' \leq t$ , return RL. 2. Otherwise, add (id, t) to RL and return the updated list.

**Correctness:** For signature  $\sigma = (\sigma_1, \sigma_2, \theta)$  on message M generated by  $\mathrm{Sign}(M, ts_{id,t})$ ,  $\sigma_1$  is a valid SM9 signature under identity id, so step (b) of verification succeeds. If user id is not revoked at time t, by the update node selection algorithm, there exists a common node  $\theta \in Path(id) \cap KUNodes$ , so step (a) passes. Since  $\sigma_2$  is a valid SM9 signature under identity  $UID||t|\theta$ , step (c) succeeds. Thus, CS-SM9-RIBS satisfies correctness.

## 3 Security Analysis

Theorem 2 (Security of CS-SM9-RIBS). Let  $\mathcal{A}$  be any probabilistic polynomial-time adversary attacking the EU-CMIA security of CS-SM9-RIBS with success probability  $\epsilon$ . Then there exists another probabilistic polynomial-time algorithm  $\mathcal{B}$  that can forge an SM9-IBS signature with the same probability  $\epsilon$ .

**Proof.** We construct a simulator  $\mathcal{B}$  that uses  $\mathcal{A}$  as a subroutine to forge an SM9-IBS signature in the EU-CMIA model.  $\mathcal{B}$  simulates  $\mathcal{A}$ 's environment as



follows:

- a) Setup:  $\mathcal{B}$  queries the SM9-IBS challenger to obtain challenge master public key  $mpk = (g_1, g_2, P_{pub}, H_2(\cdot))$  and sends mpk to  $\mathcal{A}$ .  $\mathcal{B}$  initializes empty revocation list RL, full binary tree Tree, and empty sets  $L_1$  and  $L_2$ .
- b) Queries:  $\mathcal{B}$  answers  $\mathcal{A}'$  s queries as:
  - Long-term signing key query: For query on identity id,  $\mathcal{B}$  forwards id to the SM9-IBS challenger to obtain  $ds_{id}$  and returns it, adding id to  $L_1$ .
  - Update key query: For time t,  $\mathcal{B}$  computes  $KUNodes_t$  using KUNode(Tree, RL, t). For each  $\theta \in KUNodes_t$ ,  $\mathcal{B}$  queries the challenger for key  $ds_{UID||t|\theta}$  and returns the set  $uk_t = \{ds_{UID||t|\theta}\}_{\theta \in KUNodes_t}$  to  $\mathcal{A}$ , adding all  $UID||t|\theta$  to  $L_2$ .
  - Signature query: For query (id, t, M),  $\mathcal{B}$  first checks if id was revoked at or before t (assuming  $\mathcal{A}$  queries update keys first). If revoked, return  $\bot$ . Otherwise,  $\mathcal{B}$  uses  $ds_{UID||t|\theta}$  to generate  $\sigma_2$ . For  $\sigma_1$ , if  $id \in L_1$ , use  $ds_{id}$ ; otherwise query the challenger for signature on  $M||t||\theta$  under identity id. Return  $\sigma = (\sigma_1, \sigma_2, \theta)$ .
  - Revocation query: For revocation of id at time t,  $\mathcal{B}$  adds (id, t) to RL.
- c) Forgery:  $\mathcal{A}$  outputs forged signature  $(M^*, \sigma^*)$  for challenge identity  $id^*$  and time  $t^*$ .
- **d) Output:** If  $\sigma^*$  is a valid CS-SM9-RIBS signature, then: If  $id^* \notin L_1$ ,  $\mathcal{B}$  outputs  $(M^*||t^*||\theta^*,\sigma_1^*)$  as a forgery for SM9-IBS. If  $id^* \in L_1$ , then  $id^*$  must have been revoked before  $t^*$ . By the update node generation algorithm,  $KUNodes_{t^*}$  contains no nodes on  $Path(id^*)$ , so  $\mathcal{B}$  never queried the challenger for  $ds_{UID||t^*||\theta^*}$ . Thus  $\mathcal{B}$  can output  $(M^*||t^*||\theta^*,\sigma_2^*)$  as a forgery.

 $\mathcal{B}$  perfectly simulates  $\mathcal{A}$ 's environment. If  $\mathcal{A}$  successfully forges a CS-SM9-RIBS signature,  $\mathcal{B}$  forges an SM9-IBS signature with the same probability.

### 4 Performance Analysis

Currently, besides directly applying Boneh-Franklin's generic revocation approach to SM9-IBS, no published revocation algorithms exist for SM9-IBS. However, excellent revocation algorithms exist for other identity-based signatures [?, ?]. This section compares performance theoretically and experimentally among: (1) our CS-SM9-RIBS, (2) original SM9-IBS [?], and (3) BF-SM9-RIBS (Boneh-Franklin approach).

**Table 1** summarizes theoretical performance comparisons. We use symmetric bilinear pairings where group order is prime p. N and R denote total users and revoked users; "E" and "P" denote group exponentiation and pairing operations

(ignoring other operations). "-" indicates non-existence; "0" indicates negligible cost.

In BF-SM9-RIBS, users store only per-period temporary keys generated by the KGC. The update strategy concatenates identity id with time period t as id||t to generate temporary signing keys sent via secure channels, yielding O(N-R) update complexity that grows linearly with user count. Our CS-SM9-RIBS uses complete subtree technology, requiring only  $O(\log(N/R))$  update keys on average, transmittable over public channels.

**Table 1: Performance Comparison** 

Metric	SM9-IBS	BF-SM9-RIBS	CS-SM9-RIBS
System public key size	2  p	2  p	2  p
System private key size	p	p	p
Long-term key size	_	0	p
Update key size	-	(N-R)  p	$(\log(N/R))  p  $
Temporary key size	p	p	2  p
Long-term key time	_	0	1E
Update key time	-	(N-R)E	$(\log(N/R))E$
Temporary key time	-	0	0
User revocation time	-	0	0
Signing time	1P + 2E	1P + 2E	2P + 4E
Verification time	1P + 2E	1P + 2E	2P + 4E
Key update channel	-	Secure	Public
Revocation support	No	Yes	Yes

Both BF-SM9-RIBS and CS-SM9-RIBS support revocation while preserving SM9-IBS parameters. BF-SM9-RIBS requires no long-term key storage and has single-element temporary keys, but suffers high update complexity and needs secure channels. CS-SM9-RIBS stores one long-term key; its temporary key contains two group elements but includes the long-term key without extra storage. Signature size, signing time, and verification time are double that of SM9-IBS due to the additional signature operation for revocation.

**Experimental Setup:** We implemented simulations on a 2.4GHz Intel i5-9300H CPU with 16.0GB RAM, Windows 10, using the JPBC library with Type-F elliptic curves. **Table 2** shows average execution times (excluding negligible operations and one-time setup). For update key generation with N=100 users and no revocations, BF-SM9-RIBS generates 100 keys while CS-SM9-RIBS generates only 1.

Table 2: Average Execution Time Comparison

Algorithm	User Registration	Update Key Gen.	Temp Key Gen.	Signing	Verification
SM9- IBS [?]	0.006s	-	-	0.043s	0.478s
BF- SM9- RIBS [?]	0.006s	0.685s	0.042s	0.006s	0.467s
CS- SM9- RIBS (Sec 2.3)	0.006s	0.006s	0.088s	0.852s	0.478s

For deeper comparison, we measured update key generation with N up to 8192 and R varying from 0 to 100 (random positions). **Figure 4** shows CS-SM9-RIBS's update time remains under 15 seconds, while BF-SM9-RIBS takes about 45 seconds when N=8192.

Comparison with International Schemes: Table 3 compares CS-SM9-RIBS with other revocable IBS schemes [?, ?]. Except [?] (based on trilinear maps), others use standard bilinear maps. CS-SM9-RIBS has smaller temporary keys and signatures than most schemes. Its signing time requires one more exponentiation than [?], but [?]'s update complexity grows linearly with N. [?] depends only on R but relies on less mature trilinear maps. Overall, CS-SM9-RIBS demonstrates clear performance advantages.

Table 3: Comparison with Other Revocable IBS Algorithms

Scheme	Temp Key Size	Verification Time	Update Key Time
[?]	3  p	3P + 3E	O(N-R)E
[?]	2  p	2P + 4E	$(\log(N/R))E$
[?]	2  p	1P + 3E	O(N-R)E
[?]	2  p	3P	O(R)E
CS-SM9-RIBS	2  p	2P + 4E	$(\log(N/R))$ E

## 5 Conclusion

This paper proposes a revocable SM9 identity-based signature algorithm addressing SM9's key revocation problem. Using a complete subtree, it achieves efficient user privilege control and key revocation/update. Theoretical and experimental analyses show CS-SM9-RIBS outperforms BF-SM9-RIBS in key update efficiency. Future work includes reducing the doubled signing/verification time overhead.

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Note: Figure translations are in progress. See original paper for figures.

 $Source:\ China Xiv-Machine\ translation.\ Verify\ with\ original.$