

# Pseudogap phase and duality in a holographic fermionic system with dipole coupling on a Q-lattice (postprint)

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## Abstract

We classify the different phases by the “pole-zero mechanism” for a holographic fermionic system which contains a dipole coupling with strength  $p$  on a Q-lattice background. A complete phase structure in  $p$ space can be depicted in terms of Fermi liquid, non-Fermi liquid, Mott phase and pseudo-gap phase. In particular, we find that in general the region of the pseudo-gap phase in  $p$  space is suppressed when the Q-lattice background is dual to a deep insulating phase, while for an anisotropic background, we have an anisotropic region for the pseudo-gap phase in  $p$  space as well. In addition, we find that the duality between zeros and poles always exists regardless of whether or not the model is isotropic.

## Full Text

### Preamble

#### The Pseudo-Gap Phase and Duality in Holographic Fermionic Systems with Dipole Coupling on Q-Lattice

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## Abstract

We classify different phases using the “pole-zero mechanism” for a holographic fermionic system with dipole coupling of strength  $p$  on a Q-lattice background. A complete phase structure in the  $p$ -parameter space can be described in terms of Fermi liquid, non-Fermi liquid, Mott phase, and pseudo-gap phase. In particular, we find that the region of the pseudo-gap phase is generally suppressed when the Q-lattice background is dual to a deep insulating phase. For an anisotropic background, the pseudo-gap phase region in  $p$ -space becomes anisotropic as well.

In addition, we find that the duality between zeros and poles persists regardless of whether the model is isotropic or not.

**Keywords:** Holographic Q-lattice, “pole-zero mechanism” , Fermionic system  
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## Introduction

A general theoretical framework for quantum phases and phase transitions in strongly correlated electron systems, such as cuprates and other oxides, has not yet been established. The AdS/CFT correspondence [1–3] provides a powerful alternative approach to address these strongly correlated problems and gain insight into the fundamental principles underlying these complex electron systems.

Indeed, exotic states of matter including Fermi liquid, non-Fermi liquid, Mott phase, and pseudo-gap phase have been identified using AdS/CFT correspondence [4–11]. By adding a probe fermion to an RN-AdS background, a non-linear dispersion relation emerges [5], indicating a non-Fermi liquid phase. Additionally, the low-energy behavior of fermionic systems on RN-AdS backgrounds is controlled by the AdS near-horizon geometry [6]. Later studies extensively investigated fermionic systems on Gauss-Bonnet, Lifshitz, and hyperscaling violation geometries [12–21]. Furthermore, dipole coupling between the gauge field and Dirac field can model the Mott phase [8, 9], with extended studies exploring dipole coupling effects in more general geometries [22–28].

Recently, the “pole-zero mechanism” has been used to detect a pseudo-gap phase in holographic fermionic systems with dipole coupling in both RN-AdS and Schwarzschild-AdS black holes [10, 11]. Remarkably, a duality between zeros and poles was observed in these systems [10], which should interest experimental condensed matter physicists, although this phenomenon has not yet been experimentally verified. In this paper, we investigate the pseudo-gap phase and duality in a holographic fermionic system with dipole coupling on Q-lattice geometry.

Motivated by Q-balls [29], a Q-lattice model in a holographic framework was first constructed in [30], where translational symmetry was broken in both spatial directions and a metal-insulator transition was observed through optical conductivity studies. Subsequent work explored various aspects of this framework [31–

37]. In [35], we studied a holographic fermionic system with dipole coupling on Q-lattice geometry and found that a Mott gap opens when the dipole coupling parameter  $p$  exceeds a critical value  $p_c$ . Interestingly, the Mott gap opens more readily when the Q-lattice background is dual to a deep insulating phase rather than a metallic phase. Here, we probe the pseudo-gap phase in this system using the “pole-zero mechanism” and examine how lattice parameters affect pseudo-gap formation.

Our paper is organized as follows. Section II provides a brief review of holographic Q-lattice geometry and the Dirac equation. Section III presents our main results on quantum phase classification for isotropic Q-lattice geometry, focusing on the pseudo-gap phase and lattice parameter effects. Section IV extends this analysis to anisotropic Q-lattice geometry. Finally, Section V concludes with a discussion.

## II. Holographic Q-Lattice Geometry and the Dirac Equation

We introduce the holographic Q-lattice model that breaks translational symmetry in both spatial directions and demonstrate how to simplify the Dirac equation over a specific Q-lattice background. For detailed discussions, see [30, 34, 35].

The action with Q-lattice structure in both spatial directions is:

$$S = \int d^4x \sqrt{-g} \left[ R + 6 - \frac{1}{4} F^2 - |\partial\phi_1|^2 - m_1^2 |\phi_1|^2 - |\partial\phi_2|^2 - m_2^2 |\phi_2|^2 \right]$$

where  $F = dA$ , and  $\phi_1$  and  $\phi_2$  are complex scalar fields simulating the lattices. The equations of motion are:

$$R_{\mu\nu} = g_{\mu\nu} \left( -3 + \frac{1}{4} (|\phi_1|^2 + |\phi_2|^2) \right) + \frac{1}{2} (F_{\mu\rho} F_{\nu}{}^\rho - \frac{1}{4} g_{\mu\nu} F^2) + \frac{1}{2} (\partial_\mu \phi_1 \partial_\nu \phi_1^* + \partial_\mu \phi_2 \partial_\nu \phi_2^*)$$

$$(\nabla^2 - m_1^2)\phi_1 = 0, \quad (\nabla^2 - m_2^2)\phi_2 = 0, \quad \nabla_\mu F^{\mu\nu} = 0$$

To find solutions, we use the ansatz:

$$ds^2 = -g_{tt}(z)dt^2 + g_{zz}(z)dz^2 + g_{xx}(z)dx^2 + g_{yy}(z)dy^2$$

$$\phi_1 = e^{ik_1 x} \varphi_1(z), \quad \phi_2 = e^{ik_2 y} \varphi_2(z), \quad A = A_t(z)dt$$

with:

$$g_{tt}(z) = \frac{(1-z)P(z)}{z^2Q(z)}, \quad g_{zz}(z) = \frac{1}{z^2(1-z)P(z)Q(z)}$$

$$g_{xx}(z) = V_1(z), \quad g_{yy}(z) = V_2(z), \quad A_t(z) = \mu(1-z)a(z)$$

$$P(z) = 1 + z + z^2 - \frac{\mu^2 z^3}{12}, \quad Q(z) = \exp\left(\int_0^z \frac{\varphi_1^2(s) + \varphi_2^2(s)}{2s(1-s)P(s)} ds\right)$$

where  $k_1$  and  $k_2$  are wave-numbers along the  $x$  and  $y$  directions, making  $\phi_{1,2}$  periodic with lattice constants  $2\pi/k_{1,2}$ . We set  $m_{1,2}^2 = -5/4$  to avoid violating the AdS BF bound near the horizon.

This ansatz yields five second-order ODEs for  $V_1, V_2, a, \varphi_1, \varphi_2$  and one first-order ODE for  $Q$ . Numerical solutions impose regular boundary conditions at the horizon  $z = 1$  and the following conditions at the conformal boundary:

$$Q(0) = 1, \quad V_1(0) = V_2(0) = 1, \quad a(0) = 1$$

We focus on standard quantization where the scalar fields have asymptotic behavior:

$$\varphi_{1,2} = \lambda_{1,2} z^{\Delta_{1,2}^-} + \dots$$

with UV behavior corresponding to Q-lattice deformation with amplitude  $\lambda_{1,2}$ , where  $\Delta_{1,2}^\pm = 3/2 \pm \sqrt{9/4 + m_{1,2}^2}$  is the scaling dimension of the dual operator. The Hawking temperature is:

$$T = \frac{3P(1)Q(1)}{4\pi}$$

Thus, each Q-lattice solution is specified by five dimensionless quantities:  $T/\mu$ ,  $\lambda_1/\mu^{\Delta_1^-}$ ,  $\lambda_2/\mu^{\Delta_2^-}$ ,  $k_1/\mu$ , and  $k_2/\mu$ . For simplicity, we abbreviate these as  $T$ ,  $\lambda_{1,2}$ , and  $k_{1,2}$ .

Now we introduce the Dirac equation with dipole coupling on this Q-lattice geometry. The action for the spinor field interacting with the gauge field is:

$$S_D = \int d^4x \sqrt{-g} \bar{\zeta} (i\Gamma^a D_a - m_\zeta - ip\Gamma^{\mu\nu} F_{\mu\nu}) \zeta$$

where  $D_a = \partial_a + \frac{1}{4}(\omega_{\mu\nu})_a \Gamma^{\mu\nu} - iqA_a$  and  $\Gamma^{\mu\nu} F_{\mu\nu} = \frac{1}{2}\Gamma^{\mu\nu}(e_\mu)^a(e_\nu)^b F_{ab}$ , with  $(e_\mu)^a$  forming an orthonormal basis and  $(\omega_{\mu\nu})_a$  the spin connection 1-forms.

With the redefinition  $\zeta = (g_{tt}g_{xx}g_{yy})^{-1/4}F$  and Fourier transform  $F(z, k) \equiv (A_\alpha, B_\alpha)^T$  with  $\alpha = 1, 2$ , and using gamma matrices:

$$\Gamma^z = \sigma_3 \otimes \sigma_3, \quad \Gamma^t = i\sigma_1 \otimes \mathbf{1}, \quad \Gamma^x = \sigma_2 \otimes \sigma_1, \quad \Gamma^y = -\sigma_2 \otimes \sigma_2$$

the Dirac equation simplifies to:

$$(\partial_z \mp m_\zeta \sqrt{g_{zz}}) A_\alpha \pm \frac{(\omega + qA_t) \pm (-1)^\alpha k_x \sqrt{g_{xx}} \pm (-1)^\alpha k_y \sqrt{g_{yy}}}{\sqrt{g_{tt}g_{zz}}} A_\alpha + \frac{p \partial_z A_t}{\sqrt{g_{tt}g_{zz}}} B_\alpha = 0$$

$$(\partial_z \mp m_\zeta \sqrt{g_{zz}}) B_\alpha \mp \frac{(\omega + qA_t) \pm (-1)^\alpha k_x \sqrt{g_{xx}} \pm (-1)^\alpha k_y \sqrt{g_{yy}}}{\sqrt{g_{tt}g_{zz}}} B_\alpha + \frac{p \partial_z A_t}{\sqrt{g_{tt}g_{zz}}} A_\alpha = 0$$

At the horizon  $z = 1$ , we impose the ingoing boundary condition:

$$\begin{pmatrix} A_\alpha \\ B_\alpha \end{pmatrix} = c_\alpha \begin{pmatrix} 1 \\ i \end{pmatrix} (1-z)^{-i\omega/4\pi T}$$

Near the boundary, the Dirac field behaves as:

$$\begin{pmatrix} A_\alpha \\ B_\alpha \end{pmatrix} \approx a_\alpha z^{m_\zeta} \begin{pmatrix} 0 \\ 1 \end{pmatrix} + b_\alpha z^{-m_\zeta} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

The retarded Green's function is obtained holographically as  $a_\alpha = G_{\alpha\alpha'} b_{\alpha'}$ . To compute the boundary Green's function, we construct a basis of finite solutions  $(A_\alpha^I, B_\alpha^I)$  and  $(A_\alpha^{II}, B_\alpha^{II})$  due to coupling between the four Dirac components.

### III. Pseudo-Gap Phases and Duality on an Isotropic Q-Lattice

In condensed matter physics, poles ( $k = k_F$ ) and zeros ( $k = k_L$ ) in the Green's function of strongly correlated fermionic systems compete with each other. The "pole-zero mechanism" classifies different phases of such systems [38-42]. The phase classification criteria are:

- **Poles** (Non-)Fermi liquid phase
- **Zeros** Mott insulator phase
- **Coexistence of poles and zeros** Pseudo-gap phase

This mechanism was first applied in a holographic framework in [10] to characterize different phases. Here, we use it to probe the pseudo-gap phase in our holographic fermionic system with dipole coupling on Q-lattice geometry. This section explores isotropic Q-lattices ( $\lambda_1 = \lambda_2$  and  $k_1 = k_2$ ), where we can set  $k_y = 0$  without loss of generality. Anisotropic cases are discussed in the next section.

For definiteness, we fix  $m = 0$ ,  $q = 1$ , and work at extremely low temperature  $T \approx 0.00398$  throughout.

For  $p = 0$ , neither poles nor zeros appear in the determinant of the Green's function  $\det G_R$  because they cancel out (Fig. 1 [Figure 1: see original paper]). However, once dipole coupling is turned on, poles and zeros emerge in  $\det G_R$ , enabling phase classification via the pole-zero mechanism. Fig. 2 [Figure 2: see original paper] shows  $\det G_R$  versus  $k_x$  at  $\omega = 0$  for  $p = -4.5$  and  $p = 4.5$  with  $\lambda_1 = \lambda_2 = 0.5$  and  $k_1 = k_2 = 0.8$ . For  $p = -4.5$ , a pole appears at  $k_x = k_F \approx 1.222$ , indicating a (non-)Fermi liquid state, while for  $p = 4.5$ , a zero appears at the same momentum  $k_x = k_L \approx 1.222$ , indicating a Mott state. Clearly, a duality exists between zeros and poles under  $p \rightarrow -p$ , first revealed in [10].

When the dipole coupling is decreased to  $|p| = 0.1$ , both poles and zeros coexist in  $\det G_R$  (Fig. 3 [Figure 3: see original paper]), signaling a pseudo-gap phase. This duality persists under  $p \rightarrow -p$  (Fig. 3). Based on these observations, we conclude that (non-)Fermi liquid, Mott, and pseudo-gap phases emerge in fermionic systems with dipole coupling on Q-lattices.

Using the density of states (DOS)  $A(\omega)$ , we can determine the critical point  $p_c$  for the (non-)Fermi liquid to Mott phase transition and confirm that the Mott gap opens more readily in deep insulating phases than in metallic phases [35]. We now focus on how lattice constants  $k_{1,2}$  and amplitudes  $\lambda_{1,2}$  affect the pseudo-gap phase.

Through careful numerical calculations, we find that a pseudo-gap emerges when  $|p| \lesssim 0.605$  for  $\lambda_1 = \lambda_2 = 0.5$  and  $k_1 = k_2 = 0.8$ . In a deep insulating phase with  $\lambda_1 = \lambda_2 = 2$  and  $k_1 = k_2 = 1/2^{3/2}$ , the pseudo-gap phase appears for  $|p| \lesssim 0.335$ . Thus, the pseudo-gap region in  $p$ -space is suppressed in deep insulating phases.

For comparison, the pseudo-gap phase appears when  $|p| \lesssim 0.634$  in the RN-AdS black hole background (obtained by setting  $\lambda_1 = \lambda_2 = 0$ )<sup>1</sup>.

Before concluding this section, we discuss the duality between zeros and poles. With  $k_y = 0$ , the Dirac equations can be packaged into evolution equations:

$$\partial_z \xi_\alpha + \sqrt{g_{zz}} v_- \xi_\alpha + (-1)^\alpha k_x \frac{v_+ - (-1)^\alpha k_x}{\sqrt{g_{zz}}} \xi_\alpha = 0$$

where  $\xi_\alpha \equiv A_\alpha/B_\alpha$  and  $v_\pm = (\omega + qA_t) \pm p\sqrt{g_{tt}}\partial_z A_t$ . For massless fermions, the retarded Green's function is:

$$G(\omega, k) = \lim_{z \rightarrow 0} \xi_\alpha(z, \omega, k)$$

From the evolution equation, we find the symmetry:

$$G_{11}(\omega, k) = G_{22}(\omega, -k)$$

Introducing the reciprocal  $\tilde{\xi}_\alpha = 1/\xi_\alpha$ , we find it satisfies similar evolution equations with  $p \rightarrow -p$ . Combining these results reveals the duality between zeros and poles under  $p \rightarrow -p$ .

<sup>1</sup>We have set the gauge coupling constant  $g_F = 1$  here, which differs from the convention  $g_F = 2$  in [10]. Consequently, the charge  $q$  and dipole coupling  $p$  correspond to products  $g_F q$  and  $g_F p$  as the relevant quantities.

#### IV. Pseudo-Gap Phases and Duality on an Anisotropic Q-Lattice

We now investigate pseudo-gap phases and the duality between zeros and poles on anisotropic Q-lattices, with parameters  $\lambda_1 = 1$ ,  $\lambda_2 = 0.1$ , and  $k_1 = k_2 = 0.8$ .

First, we explore duality along the  $k_x$  direction (setting  $k_y = 0$ ). As shown in Fig. 4 [Figure 4: see original paper] and Fig. 5 [Figure 5: see original paper], (non-)Fermi liquid, Mott insulating, and pseudo-gap phases appear along  $k_x$  depending on the dipole coupling  $p$ . The duality persists, as understood through analysis similar to the previous section.

Similarly, we locate poles and zeros in  $\det G_R$  along the  $k_y$  direction (setting  $k_x = 0$ ) for  $p = 6$  and  $p = -6$ . We find  $k_y^F \approx 1.983$  for  $p = -6$  and  $k_y^L \approx 1.983$  for  $p = 6$ , confirming that duality holds in the  $y$  direction. However,  $k_x^F \neq k_y^F$  (and  $k_x^L \neq k_y^L$ ), reflecting the system's anisotropy.

We find that the pseudo-gap phase emerges along  $k_x$  for  $|p| \lesssim 0.393$ , while along  $k_y$  it appears for  $|p| \lesssim 0.860$ . Clearly, the anisotropic geometry produces an anisotropic pseudo-gap region. Along the more insulating direction ( $k_x$ ), the pseudo-gap region is suppressed, consistent with our isotropic Q-lattice results.

#### V. Conclusion and Discussion

Using the “pole-zero mechanism,” we have classified phases in holographic fermionic systems with dipole coupling on Q-lattice geometry. These phases include Fermi liquid, non-Fermi liquid, Mott phase, and pseudo-gap phase, depending on the dipole coupling strength. Varying the dipole coupling parameter  $p$  thus induces quantum phase transitions in our holographic system.

While previous work [35] used spectral functions to determine the critical value  $p_c$  for the (non-)Fermi liquid to Mott phase transition and examined how lattice

parameters  $\lambda_{1,2}$  and  $k_{1,2}$  affect Mott phase formation, we have further computed the determinant of the retarded Green's function to focus on pseudo-gap phase formation. We find that the pseudo-gap region is suppressed in deep insulating phases. For anisotropic Q-lattice geometry, we obtain an anisotropic pseudo-gap region that is also suppressed along the insulating direction. Another interesting result is that the duality between zeros and poles, previously found in [10], persists in both isotropic and anisotropic Q-lattice geometries and is independent of lattice parameters.

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## References

- [1] J. M. Maldacena, "The large N limit of superconformal field theories and supergravity," *Adv. Theor. Math. Phys.* 2 (1998) 231 [*Int. J. Theor. Phys.* 38 (1999) 1113].
- [2] S. S. Gubser, I. R. Klebanov and A. M. Polyakov, "A semiclassical limit of the gauge/string correspondence," *Nucl. Phys. B* 636 (2002) 99.
- [3] E. Witten, "Anti-de Sitter space and holography," *Adv. Theor. Math. Phys.* 2 (1998) 253.
- [4] S. S. Lee, "A Non-Fermi Liquid from a Charged Black Hole: A Critical Fermi Ball," *Phys. Rev. D* 79 (2009) 086006, [arXiv:0809.3402].
- [5] H. Liu, J. McGreevy and D. Vegh, "Non-Fermi liquids from holography," *Phys. Rev. D* 83 (2011) 065029 [arXiv:0903.2477].
- [6] T. Faulkner, H. Liu, J. McGreevy and D. Vegh, "Emergent quantum criticality, Fermi surfaces and AdS," *Phys. Rev. D* 83 (2011) 125002, [arXiv:0907.2694].
- [7] M. Cubrovic, J. Zaanen and K. Schalm, "String Theory, Quantum Phase Transitions and the Emergent Fermi-Liquid," *Science* 325 (2009) 439 [arXiv:0904.1993].
- [8] M. Edalati, R. G. Leigh, P. W. Phillips, "Dynamically Generated Gap from Holography: Mottness from a Black Hole," *Phys. Rev. Lett.* 106 (2011) 091602, [arXiv:1010.3238].
- [9] M. Edalati, R. G. Leigh, K. W. Lo, P. W. Phillips, "Dynamical Gap and Cuprate-like Physics from Holography," *Phys. Rev. D* 83 (2011) 046012, [arXiv:1012.3751].

- [10] J. Alsup, E. Papantonopoulos, G. Siopsis, and K. Yeter, “Duality between zeroes and poles in holographic systems with massless fermions and a dipole coupling,” [arXiv:1404.4010].
- [11] G. Vanacore, P. W. Phillips, “Minding the Gap in Holographic Models of Interacting Fermions,” Phys. Rev. D 90, 044022 (2014), [arXiv:1405.1041].
- [12] J. P. Wu, “Holographic fermions in charged Gauss-Bonnet black hole,” JHEP 1107 (2011) 106, [arXiv:1103.3982].
- [13] J. P. Wu, “Some properties of the holographic fermions in an extremal charged dilatonic black hole,” Phys. Rev. D 84 (2011) 064008, [arXiv:1108.6134].
- [14] W. J. Li, J. P. Wu, “Holographic fermions in charged dilaton black branes,” Nucl. Phys. B 867 (2013) 810-826, [arXiv:1203.0674].
- [15] N. Iizuka, N. Kundu, P. Narayan, S. P. Trivedi, “Holographic Fermi and Non-Fermi Liquids with Transitions in Dilaton Gravity,” JHEP 1201 (2012) 094, [arXiv:1105.1162].
- [16] J. P. Wu, “Holographic fermions on a charged Lifshitz background from Einstein-Dilaton-Maxwell model,” JHEP 1303 (2013) 083.
- [17] X. M. Kuang, E. Papantonopoulos, B. Wang and J. P. Wu, “Formation of Fermi surfaces and the appearance of liquid phases in holographic theories with hyperscaling violation,” JHEP 1411 (2014) 086 [arXiv:1409.2945].
- [18] L. Q. Fang, X. H. Ge, X. M. Kuang, “Holographic fermions in charged Lifshitz theory,” Phys. Rev. D 86 (2012) 105037, [arXiv:1201.3832].
- [19] L. Q. Fang, X. H. Ge, X. M. Kuang, “Holographic fermions with running chemical potential and dipole coupling,” Nucl. Phys. B 877 (2013) 807-824, [arXiv:1304.7431].
- [20] M. Alishahiha, M. Reza Mohammadi Mozaffar, A. Mollabashi, “Fermions on Lifshitz Background,” Phys. Rev. D 86 (2012) 026002 [arXiv:1201.1764].
- [21] D. Maity, S. Sarkar, B. Sathiapalan, R. Shankar and N. Sircar, “Properties of CFTs dual to Charged BTZ black-hole,” Nucl. Phys. B 839 (2010) 526-551, [arXiv:0909.4051].
- [22] J. P. Wu, H. B. Zeng, “Dynamic gap from holographic fermions in charged dilaton black branes,” JHEP 1204 (2012) 068, [arXiv:1201.2485].
- [23] J. P. Wu, “Emergence of gap from holographic fermions on charged Lifshitz background,” JHEP 04 (2013) 073.
- [24] J. P. Wu, “The charged Lifshitz black brane geometry and the bulk dipole coupling,” Phys. Lett. B 728 (2014) 450-456.
- [25] X. M. Kuang, B. Wang, J. P. Wu, “Dipole coupling effect of holographic fermion in the background of charged Gauss-Bonnet AdS black hole,” JHEP 07 (2012) 125, [arXiv:1205.6674].

- [26] X. M. Kuang, B. Wang, J. P. Wu, “Dynamical gap from holography in the charged dilaton black hole,” *Class. Quant. Grav.* 30 (2013) 145011, [arXiv:1210.5735].
- [27] L. Q. Fang, X. H. Ge, X. M. Kuang, “Holographic fermions with running chemical potential and dipole coupling,” *Nucl. Phys. B* 877 (2013) 807-824, [arXiv:1304.7431].
- [28] W. J. Li, H. Zhang, “Holographic non-relativistic fermionic fixed point and bulk dipole coupling,” *JHEP* 1111 (2011) 018, [arXiv:1110.4559].
- [29] S. R. Coleman, “Q balls,” *Nucl. Phys. B* 262 (1985) 263.
- [30] A. Donos, J. P. Gauntlett, “Holographic Q-lattices,” *JHEP* 1404 (2014) 040, [arXiv:1311.3292].
- [31] A. Donos, J. P. Gauntlett, “Novel metals and insulators from holography,” *JHEP* 1406 (2014) 007.
- [32] M. Blake, A. Donos, “Quantum Critical Transport and the Hall Angle,” [arXiv:1406.1659].
- [33] A. Donos, J. P. Gauntlett, “Thermoelectric DC conductivities from black hole horizons,” [arXiv:1406.4742].
- [34] Y. Ling, P. Liu, C. Niu, J. P. Wu, and Z. Y. Xian, “Holographic Superconductor on Q-lattice,” *JHEP* 02 (2015) 059, [arXiv:1410.6761].
- [35] Y. Ling, P. Liu, C. Niu, J. P. Wu, and Z. Y. Xian, “Holographic fermionic system with dipole coupling on Q-lattice,” *JHEP* 12 (2014) 149, [arXiv:1410.7323].
- [36] Y. Ling, P. Liu, C. Niu, J. P. Wu, and Z. Y. Xian, “Holographic Entanglement Entropy Close to Quantum Phase Transitions,” [arXiv:1502.03661].
- [37] Y. Ling, P. Liu, C. Niu, J. P. Wu, “Building a doped Mott system by holography,” [arXiv:1507.02514].
- [38] T. D. Stanescu, P. W. Phillips, and T. Choy, “Theory of the Luttinger surface in doped Mott insulators,” *Phys. Rev. B* 75, 104503 (2007), [arXiv:cond-mat/0602280].
- [39] I. Dzyaloshinskii, “Some consequences of the Luttinger theorem: The Luttinger surfaces in non-Fermi liquids and Mott insulators,” *Phys. Rev. B* 68, 085113 (2003).
- [40] S. Hong and P. W. Phillips, “Towards the standard model for Fermi arcs from a Wilsonian reduction of the Hubbard model,” *Phys. Rev. B* 86, 115118 (2012), [arXiv:1110.0440 [cond-mat.str-el]].
- [41] S. Sakai, Y. Motome, and M. Imada, “Evolution of Electronic Structure of Doped Mott Insulators: Reconstruction of Poles and Zeros of Green’s Function,” *Phys. Rev. Lett.* 102, 056404 (2009), [arXiv:0809.0950v1 [cond-mat.str-el]].

[42] S. Sakai, Y. Motome, and M. Imada, “Doped high-Tc cuprate superconductors elucidated in the light of zeros and poles of the electronic Green’s function,” *Phys. Rev. B* 82, 134505 (2010), [arXiv:1004.2569 [cond-mat.str-el]].

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